## <u>Franco Bedeschi,</u> INFN – Pisa INO Annual Symposium Pisa, March 2018

periment at FNZ

Theory progress Experiment

Introduction

History of

The Muon g-2

### Conclusions

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# Magnetic moment: classical description

v/2



★ Magnetic moment of current loop  $\mu = I A = I \pi r^2$ 

Current from single particle:

$$i = qv/(2\pi r)$$

$$i = qv/(2\pi r) \cdot \pi r^2 = qr$$

Relation to angular momentum

$$> S = mrv = 2m/q \cdot \mu$$
$$> \mu = q/(2m) \cdot S$$



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## Magnetic moment proportional to spin also for elementary particles, .... but quantum mechanics kicks in

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# **Basic definitions**

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Magnetic moment relation to point-like particle spin different from classical phys.
 Tree level QED : g = 2 for all leptons
 Explained by Dirac in 1928

$$\vec{\mu}_S = g \frac{q}{2m} \vec{S}$$



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Higher orders (1)



# Radiative corrections (challenging!) change the picture a \neq 0

Schwinger (1948): 1 loop correction



 $a_{\mu} = \frac{\alpha}{2\pi}$ 





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### QED calculations becomes more complex:

- ightarrow 1 loop → 1 diagram
- ▶ 2 loop → 7 diagrams
- > 3 loop → 72 diagrams
- → 4 loop → 891 diagrams

analytic calculation

- analytic calculation
- analytic calculation
- numerical calculation
- > 5 loop → > 12,000 diagrams numerical calculation
   Contribution irrelevant compared to current experimental errors
   ◆ Higher order corrections depend on lepton mass



# Other corrections



 $a_{\mu}$  is affected by loops with W/Z or quarks (hadrons)



Weak contribution small and precisely calculated

► Had VP and Had LBL are hard .... however

Improvements and new approaches expected



Contributions of virtual heavier particles (including new physics!) scale with lepton mass squared





New physics effects similar to weak contributions

eg. SUSY gives relevant contributions from  $\chi^{\pm} e \chi^0$  not strongly bounded by LHC



Presently a<sup>exp</sup> – a<sup>th</sup> ~ (245 ± 81) x 10<sup>-11</sup> (Kinoshita, Jul. 2014)
 Experimental precision close to new physics effects
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### Experimental summary



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Improved measurement of the μ anomalous magnetic moment:  $a_{\mu} = (g_{\mu}-2)/2$ 

Best previous measurement BNL-E821 (1997-2001)

 $a_{\mu}^{\exp} = (11659208.9(5.4)_{stat}(3.3)_{syst}(6.3)_{tot}) \times 10^{-10}$ 

Error statistics limited

G. W. Bennett et al.,PRL 92, 161802 (2004).L. Roberts, Chinese Phys. C34, 741 (2010).

 $\blacktriangleright$  Difference wrt. SM ~ 3 $\sigma$  (theory error ~ 5 x 10<sup>-10</sup>)

Goal of new FNAL experiment (E989) (x4 better)

 $\succ$  σ<sub>tot</sub> = (1.2 stat. ⊕ 1.3 syst.) x 10<sup>-10</sup> = 1.6 x 10<sup>-10</sup>

Assuming same central values (exp. & theory):

► SM – exp. difference:

 $\blacksquare \sim 5\sigma$  if no improvement in theoretical determination

 $\sim 8\sigma$  if theory improved by x2

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## $a_{\mu}$ proportional to difference between precession and rotation frequency





# How it works: $\omega_a$



Inject polarized muons into the ring

Observe decay electrons

Count electrons above energy threshold (1.9 GeV optimal)



Harder electron spectrum when spin is aligned with momentum



Figure 2: Distribution of electron counts versus time for 3.6 billion muon decays from the E821 experiment. The data are wrapped around modulo  $100 \,\mu s$  [9].

$$N(t) = N_0 e^{-\frac{t}{\gamma\tau}} \left[1 + A\cos(\omega_a t + \phi)\right]$$

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### **\*** B measured with NMR probes (precision $\sim 10 \text{ ppb}$ )

- $\sim \omega_p = \text{free proton precession frequency} \propto \mathbf{B}^2$
- Probes in several fixed positions and on trolley that can move around the ring
  - What matters is average field around ring

Max deviation 15 ppm demonstrated in ring section with laminations







★ The whole measurement is reduced to the measurement of two frequencies:  $\omega_a$  and  $\omega_p$ ▶ With a little math:  $a_{\mu} = \frac{\omega_a / \omega_p}{\lambda - \omega_a / \omega_p}$ 

# \* $\lambda = \mu_{\mu}/\mu_{p}$ is the ratio of the magnetic moments of the muon and the proton

Measured with 120 ppb (26 ppb indirect) precision with spectroscopy of muonic hydrogen like atoms in a magnetic field monitored with NMR probes

W. Liu et al, Phys. Rev. Lett. 82, 711 (1999)

S. Karshenboim and V. Ivanov, Can. J. Phys. 80, 1305 (2002)

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## Most relevant: calorimeter gain variations within muon fill

<b>Improving</b> ω <sub>a</sub>							
E821 Error	Size	Plan for the New $g-2$ Experiment	Goal				
	[ppm]		[ppm]				
Gain changes	0.12	Better laser calibration and low-energy threshold	0.02				
Lost muons	0.09	Long beamline eliminates non-standard muons	0.02				
Pileup	0.08	Low-energy samples recorded; calorimeter segmentation	0.04				
CBO	0.07	New scraping scheme; damping scheme implemented	0.04				
${\cal E}$ and pitch	0.05	Improved measurement with traceback	0.03				
Total	0.18	Quadrature sum	0.07				

Coherent Betatron Oscillations

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# Calorimetry (1)



**\***24 stations **Fast:** Crystals PbF<sub>2</sub> Cherenkov SiPM readout Laser calibration Reduce systematics









Energy resol. ~ 3% Optimized for good timing Timing resolution ▶ 25 ps intrinsic Digitizer bin 1.25 nsec Pile up Resolve up to 4.5 ns separation



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# Calibration system



Light from 6 blue lasers distributed to all calorimeter cells Source monitor: tracks laser intensity variations Local monitor: tracks distribution chain variations

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# Source monitor



### Monitor laser fluctuations:

- $\succ$  Fast reference  $\rightarrow$  PIN diodes
- Slow reference  $\rightarrow$  NaI + Am source



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Local monitor



### Ratio of return light from calorimeter and direct pulse from source monitor (~250 nsec separation)





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Test beam results







Engineering run



### First results with short engineering run June 2017



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The muon anomaly has great history and interest.

- Crucial test of higher order calc. and can signal new physics
- Lots of new theory work started including major lattice projects
- Ring, detector and beam for planned FNAL experiment are complete
  - Physics quality data taking is in progress now
- Superb laser calibration system from INFN!
  - > Impossible without strong INO support  $\rightarrow$  THANKS!
- First results are close .....
  - > 1 x BNL data by summer 2018









# MORE SLIDES

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### Connected with other measurement of great interest











+ exp.  $x 10^{-10}$  $= 2.3x 10^{-10}$ 

 $p = 3.7 \times 10^{-10}$ = 4.4x10<sup>-10</sup> = 3.3x10<sup>-10</sup>

## $10^{-10} \text{ JN'09}$ = 4.0x10<sup>-10</sup> 10<sup>-10</sup> PRV'09 = 2.6x10<sup>-10</sup>

✓ PRV'09:  $(11'659'184.4 \pm 5.1) \times 10^{-10} \rightarrow 11'659'181.9 \pm 4.2$  (Davier16) INO Annual Symposium, Pisa - March 2018 F. Bedeschi, INFN-Pisa



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a)

**g-2** 

b)

# Correlation with $\mu \rightarrow e\gamma$





 However: strong correlation of individual diagrams does not imply strong correlation of the sum! Strong correlations for strong parameter constraints or domination of certain diagrams

[Kersten,Park,DS,Velasco-Sevilla '14]









### Measurements of g-2 started in 1957

# Continuous evolution of the technique until now

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# Garwin/Lederman (1957)



### First experiments

#### Magnetic resonance

 $g = 2.00 \pm 0.10$ 

#### LETTERS TO TH

<sup>4</sup> Their arguments are as follows: From the He<sup>6</sup> recoil experiment and from Eq. (A-4) of reference 1 one concludes that  $(|C_A|^2+|C_A'|^2)/(|C_T|^2+|C_T'|^2) \leq \frac{1}{3}$ . Hence, by comparing Eq. (16) of reference 3 [see also Eq. (A-6) of reference 1], one concludes that the present large asymmetry is possible only if both conservation of parity and invariance under charge conjugation are violated



PHYSICAL REVIEW

#### VOLUME 109, NUMBER 3

FEBRUARY 1, 1958

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#### Magnetic Moment of the Free Muon\*†

T. COFFIN, R. L. GARWIN,<sup>‡</sup> S. PENMAN, L. M. LEDERMAN, AND A. M. SACHS  $a_{\mu} = 0.00113 \pm 0.00014$ (Received October 1, 1957)

The magnetic moment of the positive  $\mu$  meson has been measured in several target materials by a magnetic resonance technique. Muons were brought to rest with their spins parallel to a magnetic field. A radio-frequency pulse was applied to effect a spin reorientation which was detected by counting the decay electrons emerging after the pulse in a fixed direction. Results are expressed in terms of a g factor which for a spin  $\frac{1}{2}$  particle is the ratio of the actual moment to  $e\hbar/2m_{\mu}c$ . The most accurate result obtained in a CHBr<sub>3</sub> target, is that  $g=2(1.0026\pm0.0009)$  compared to the theoretical prediction of g=2(1.0012). Less accurate measurements yielded  $g=2.005\pm0.005$  in a copper target and  $g=2.00\pm0.01$  in a lead target.

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**CERN-I** (1964)

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123005.



### Precession in magnetic field

G. CHARPAK, et al. 16 Giugno 1965 Il Nuovo Oimento Serie X. Vol. 37, pag. 1241-1363

 $\sigma_{a\mu}/a_{\mu} = 1.9 \rightarrow 0.43 \%$ 

#### The Anomalous Magnetic Moment of the Muon.

G. CHARPAK (\*), F. J. M. FARLEY, R. L. GARWIN (\*\*), T. MULLER (\*\*\*), J. C. SENS and A. ZICHICHI

CERN - Geneva

(ricevuto il 18 Settembre 1964)

Summary. — The anomalous part of the gyromagnetic ratio,  $\mathbf{a} = \frac{1}{2}(g-2)$ of the muon has been measured by determining the precession  $\theta = \mathbf{a}\omega_0\overline{B}t$  for 100 MeV/c muons as a function of storage time t in a known static magnetic field of the form  $B=B_0(1+ay+by^2+cy^2+dy^4)$ . The result is  $\mathbf{a}_{exp} = (1162\pm5)\cdot 10^{-6}$  compared with the theoretical value  $\mathbf{a}_{th} = \alpha/2\pi + 0.76\alpha^2/\pi^2 = 1165\cdot 10^{-6}$ . This agreement shows that the muon obeys standard quantum electrodynamics down to distances  $\sim 0.1$  fermi. Details are given of the methods used to store muons for  $\sim 10^3$  turns in the field, and of measuring techniques and precautions necessary to achieve the final accuracy. Some of the methods of orbit analysis, magnet construction shimming and measurement, polarization analysis, and digital timing electronics may be of more general interest.



#### Farley, Sens, Charpak, Muller, Zichichi 6-m g-2 magnet

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# ♦ CERN-II: muon storage ring → $\sigma_{a\mu}/a_{\mu} = 265$ ppm ♦ CERN-III: magic mom./electr. quads → $\sigma_{a\mu}/a_{\mu} = 7.3$ ppm



S van der Meer, F J M Farley, M Giesch, R Brown, J Bailey, <u>E Picasso</u> and H Jöstlein

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# ★ Extremely good storage ring magnet! → B uniformity ★ AGS higher statistics then CERN → σ<sub>aµ</sub>/a<sub>µ</sub> = 5 → 0.5 ppm



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- Ring magnet from BNL!
- 20x more muons
- Much cleaner beam
- Better calorimeter
- Tracking stations added
- Better B field measurements
- Miscellaneous improvements on systematics

# Plan for error ~ 0.14 ppm



# FNAL muon beam





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$$\alpha^{-1}(ac \ Josephson) = 137.035\ 987\ 5\ (43)$$
 [31 ppb]

$$\alpha^{-1}(quantum Hall) = 137.036\ 003\ 0\ (25)$$
 [18 ppb]

 $\alpha^{-1}$ (*neutron wavelength*) = 137.036 007 7 (28) [21 *ppb*]

 $\alpha^{-1}(atom interferometry) = 137.036\ 000\ 0\ (11)\ [7.7\ ppb]$ 

 $\alpha^{-1}$ (*Rb on optical lattice*) = 137.035 999 049 (90) [0.66 *ppb*]







•  $a_{\mu}$  may be expressed as

$$a_{\mu} = a_{\mu}(\mathsf{QED}) + a_{\mu}(\mathsf{EW}) + a_{\mu}(\mathsf{had}),$$

where

$$a_\mu({\sf QED}) = {\sf A}_1 + {\sf A}_2(m_\mu/m_e) + {\sf A}_2(m_\mu/m_ au) + {\sf A}_3(m_\mu/m_e,m_\mu/m_ au)$$

• Feynman-Dyson rules enables us to write *A<sub>i</sub>* as a power series

$$A_{i} = A_{i}^{(2)}\left(\frac{\alpha}{\pi}\right) + A_{i}^{(4)}\left(\frac{\alpha}{\pi}\right)^{2} + A_{i}^{(6)}\left(\frac{\alpha}{\pi}\right)^{3} + \dots, \ i = 1, 2, 3,$$

with finite expansion coefficients.

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- $a_{\mu}$  (QED) including mass-dependent terms, is known up to n = 10.  $a_{\mu}^{(2)}(QED) = 0.5$   $a_{\mu}^{(4)}(QED) = 0.765\ 857\ 425\ (17)$   $a_{\mu}^{(6)}(QED) = 24.050\ 509\ 96\ (32)$   $a_{\mu}^{(8)}(QED) = 130.877\ 4\ (61)$  ( $A_{1}^{(8)}$  is updated)  $a_{\mu}^{(10)}(QED) = 751.77\ (93)$  ( $A_{1}^{(10)}$  is updated)
  - $\tau$ -loop contribution to  $a^{(8)}_{\mu}$  (QED) is calculated by

A. Kurz, T. Liu, P. Marquard, M. Steinhauser, arXiv:1407.0267 (2014)

 Leading contribution to a<sup>(12)</sup><sub>µ</sub>(QED) will come from diagrams which contain one light-by-light subdiagram and three vacuum-polriztion loops. A crude estimate gives

$$a^{(12)}_{\mu}(QED)(lpha/\pi)^6 \sim 0.08 imes 10^{-11}.$$

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At present it is derived mostly from experimental data related to hadronic vacuum polarization. Recent evaluations are
 a (had yp) = 6949 1 (37.2) cm (21.0) red × 10<sup>-11</sup>

$$a_{\mu}(\text{had.vp}) = 0.943.1 (07.2)_{exp}(21.0)_{rad} \times 10^{-11}$$
  
 $a_{\mu}(\text{had.vp.NLO}) = -98.4 (0.6)_{exp}(0.4)_{rad} \times 10^{-11}$ 

$$a_{\mu}$$
(had.vp.NNLO) = 12.4 (10) × 10<sup>-11</sup>

$$a_{\mu}$$
(had.lbyl) = 116 (40) × 10<sup>-11</sup>

$$a_{\mu}$$
(had.lbyl.NLO) = 3 (2) × 10<sup>-11</sup>

K. Hagiwara, R. Liao, A. D. Martin, D. Nomura, T. Teubner, J. Phys. G 38, 085003 (2011) [arXiv:1105.3149]
A. Kurz, T. Liu, P. Marquard, M. Steinhauser, PLB 734, 144 (2014)
J. Prades et al., in *Lepton Dipole Moments*, eds. B. L. Roberts and W. J. Marciano (World Scientific, Singapore, 2009), p.303.

G. Colangelo, M. Hoferichter, A. Nyffeler, M. Passera, P. Stoffer, PLB 735, 90 (2014)

Electroweak contribution has been calculated up to 2-loop order:

$$a_{\mu}({
m EW}) =$$
 154 (2)  $imes$  10<sup>-11</sup>.

K. Fujikawa, B.W. Lee, A.I. Sanda, PRD 6, 2923 (1972). A. Czarnecki, B. Krause, W.J. Marciano, PRL 76, 3267 (1996). M. Knecht, S. Peris, A. Perrottet, E. de Rafael, J. High Energy Phys. 11 (2002) 003. A. Czarnecki, W.J. Marciano, A. Vainshtein, PRD 67, 073006 (2003).

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Improved radiative corrections in MC

4 flavor lattice calculations presently 5 times worse, but are improving. arXiv:1311.3885v1 15 Nov '13

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# Potential theory improvements HLbL



#### ✤ Had. LbL:

- Use dispersion relations to connect Had LbL contributions to experimental results.
  - G. Colangelo et al., 'Towards a data-driven analysis of hadronic light-by-light scattering', Phys. Lett. B738, (2014) 6 (10 Nov. 2014)
  - G. Colangelo et al., 'Dispersion relation for hadronic light-by-light scattering and the muon g-2', PoS CD15 (2016) 008





▶ Need γγ production or decay to 2γ → x2 theory error reduction expected
 ▶ Lattice calculations also started (Tom Blum 2014: arXiv:1407.2923)







# FNAL beam wrt. BNL

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Beam improved recycling pbar source:

- x20 total # muons
  x6-12 #muons/proton on target
  x4 fill frequency
- Statistical error on  $a_{\mu}$ : 5.4 x 10<sup>-10</sup>  $\rightarrow$  1.2 x 10<sup>-10</sup>
- Removed pion flash
  - $\blacksquare L_{decay} 90 \text{ m} \rightarrow 2000 \text{ m}$
- Fast muon kicker

Turns off before one turn





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# B field systematics



#### Mostly more and better probes/temperature stability

E821 Error	Size	Plan for the E989 $g - 2$ Experiment	Goal
DINL	[ppm]	<b>FINAL</b>	[ppm]
Absolute field	0.05	Special 1.45 T calibration magnet with thermal	
calibrations		enclosure; additional probes; better electronics	0.035
Trolley probe	0.09	Absolute cal probes that can calibrate off-central	
calibrations		probes; better position accuracy by physical stops	
		and/or optical survey; more frequent calibrations	0.03
Trolley measure-	0.05	Reduced rail irregularities; reduced position uncer-	
ments of B <sub>0</sub>		tainty by factor of 2; stabilized magnet field during	
		measurements; smaller field gradients	0.03
Fixed probe	0.07	More frequent trolley runs; more fixed probes;	
interpolation		better temperature stability of the magnet	0.03
Muon distribution	0.03	Additional probes at larger radii; improved field	
		uniformity; improved muon tracking	0.01
Time-dependent	_	Direct measurement of external fields;	
external B fields		simulations of impact; active feedback	0.005
Others	0.10	Improved trolley power supply; trolley probes	
		extended to larger radii; reduced temperature	
		effects on trolley; measure kicker field transients	0.05
Total	0.17		0.07

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# Tracking system





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