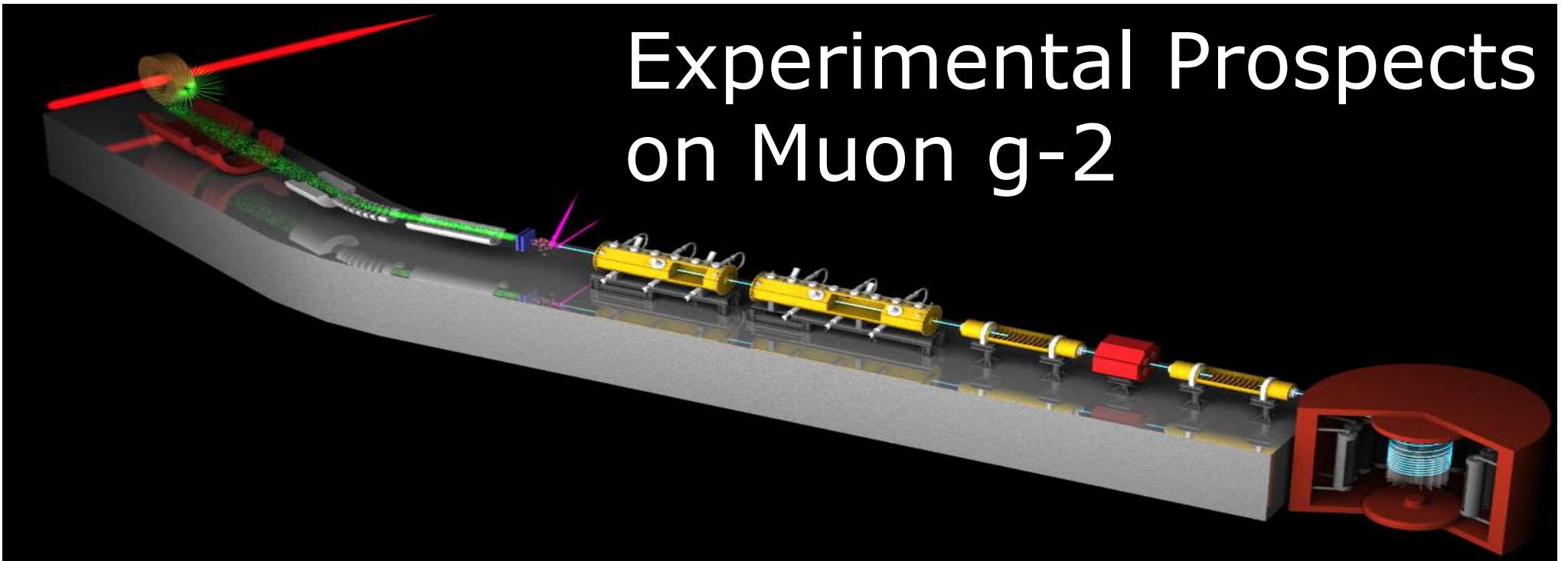


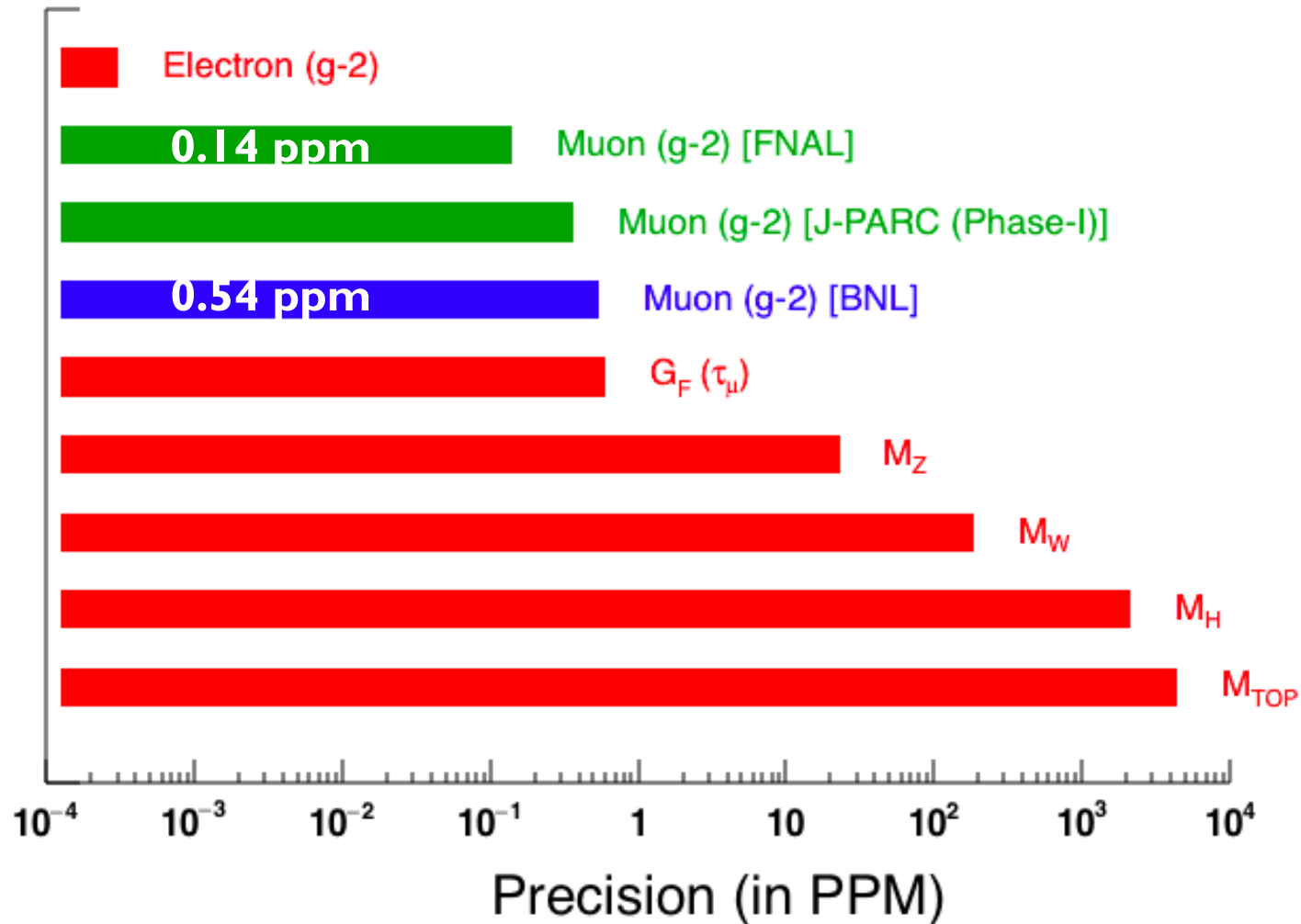
Experimental Prospects on Muon $g-2$



Mark Lancaster

University College London





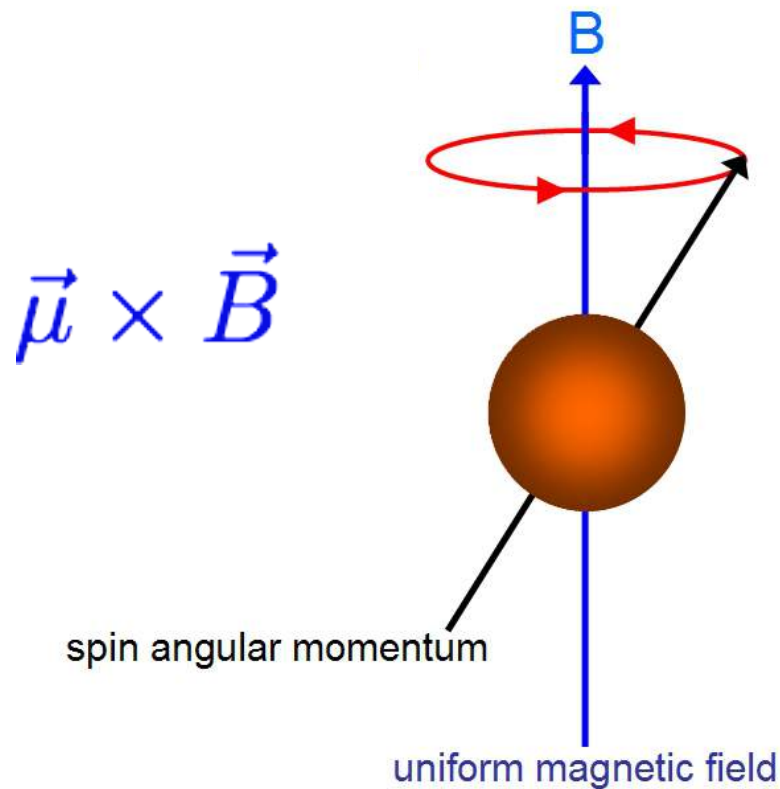


“Never measure anything but frequency”

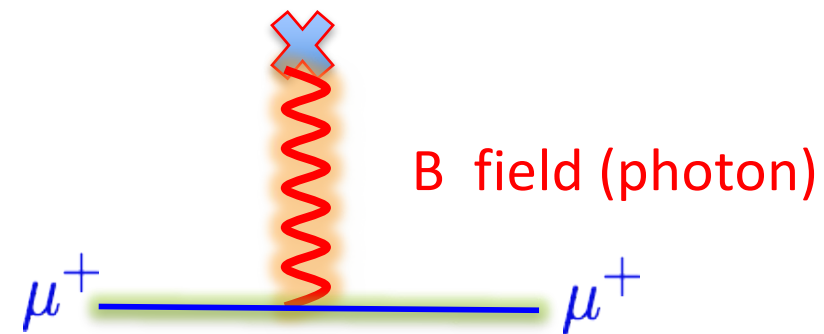
I. Rabi

$$\vec{\mu} = g \frac{Qe}{2m} \vec{s}$$

Interaction between
magnetic moment (spin) with B-field.



Spin precesses around B at
a frequency determined by "g"



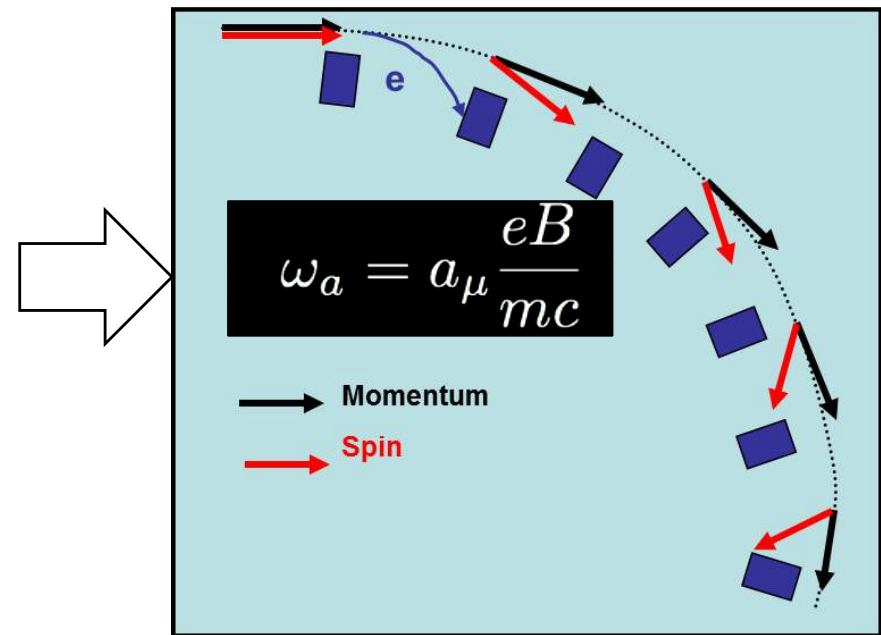
Particle in a circular storage ring (B-field): two frequencies:

$$\omega_S = \frac{geB}{2mc} + (1 - \gamma) \frac{eB}{\gamma mc} \qquad \omega_C = \frac{eB}{mc\gamma}$$

Spin vector of muon rotates slightly quicker than Momentum vector.
For a 1.5T field spin rotates in 144ns and momentum in 149ns.

$$\begin{aligned} \omega_a &= \omega_S - \omega_C \\ &= \left(\frac{g - 2}{2} \right) \frac{eB}{mc} = a \frac{eB}{mc} \end{aligned}$$

$$f_a = 228 \text{ kHz}$$

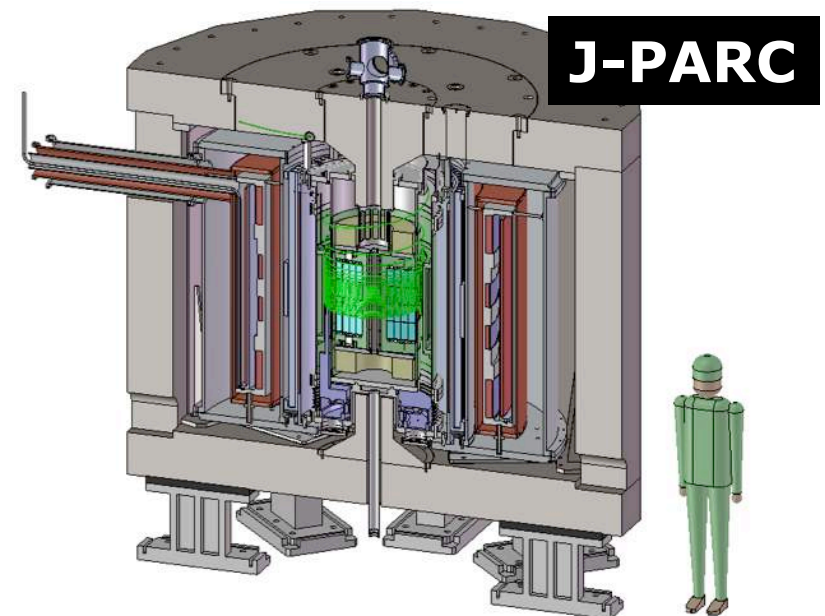


But real beams are not all on the same perfect circular orbit and can have a (small) transverse velocity component.

These imperfection causes beam to diverge vertically.

Two approaches:

- cancel the divergence with an electric quadrupole field (CERN, BNL, FNAL)
- minimise the divergence by reducing the beam p_T (J-PARC)

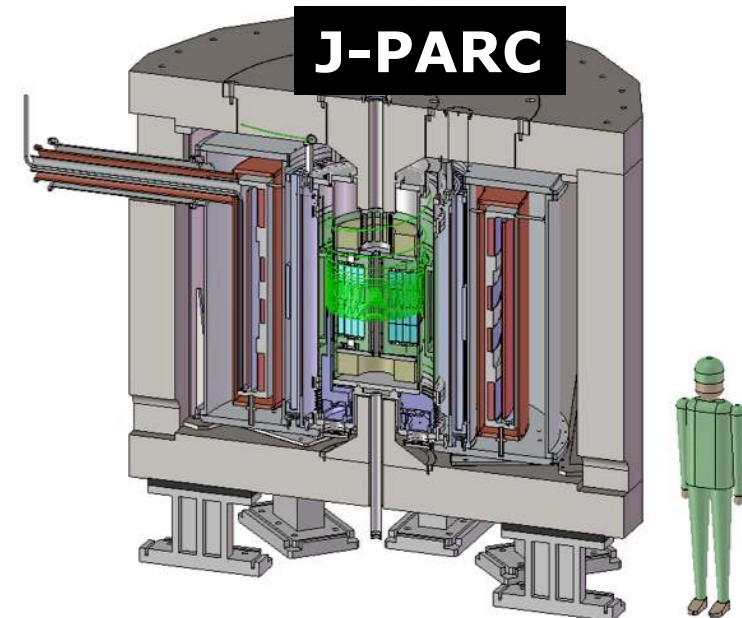




FNAL

3.094 GeV muons
1.45 T, 14m bespoke magnet
Focussing quadrupoles
Kicker magnets
Emittance: 1000pimm

0.3 GeV muons
3T, 66cm MRI magnet
 $\Delta p_T/p_T = 1e-5$



Apparatus and hence systematics are very different

$$\omega_a = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

**FNAL: MAKE ZERO BY
CHOOSING "MAGIC" γ**

**J-PARC: MAKE ZERO
BY HAVING $E=0$**

$$a_\mu = \frac{\omega_a m B}{e}$$

Both expts need to measure two quantities

- B field
- ω_a

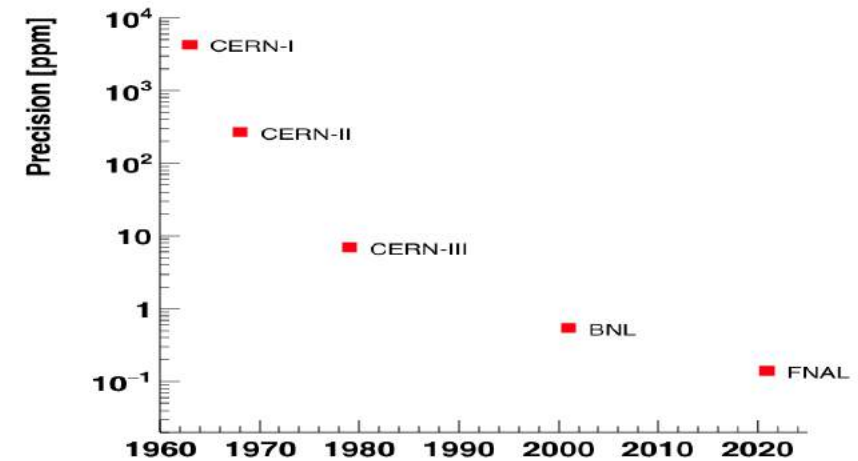
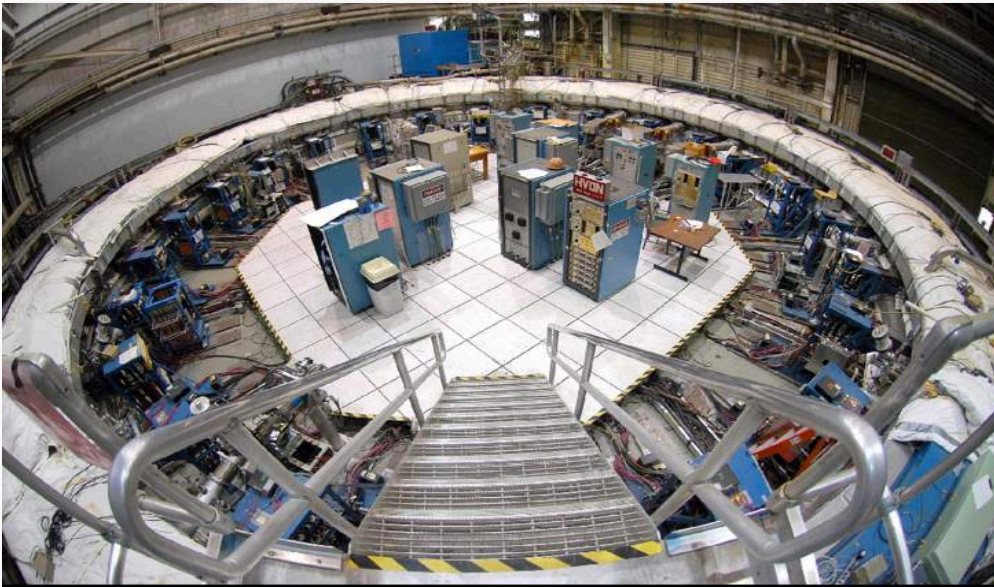
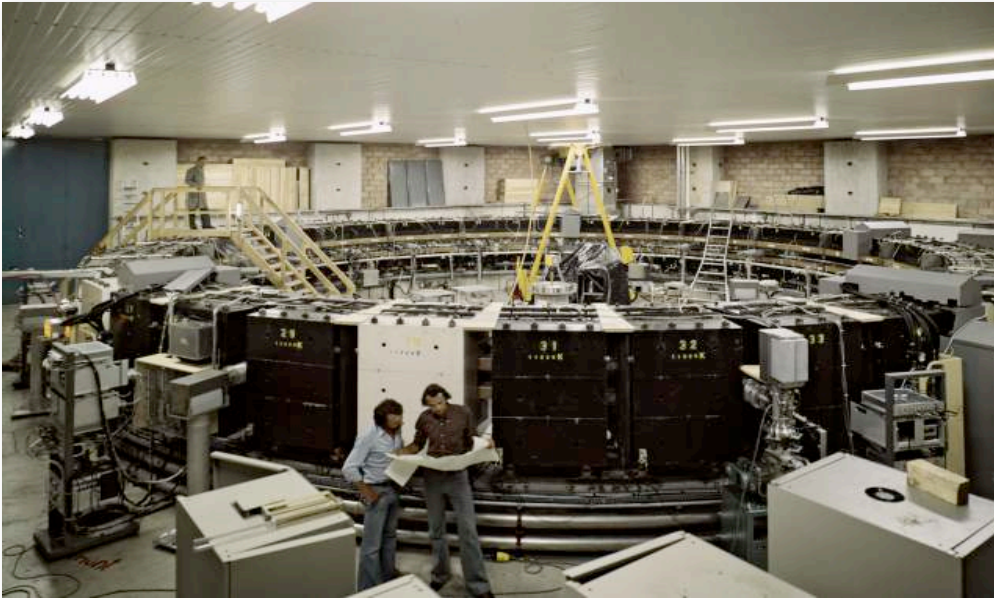
To better than 0.1 ppm

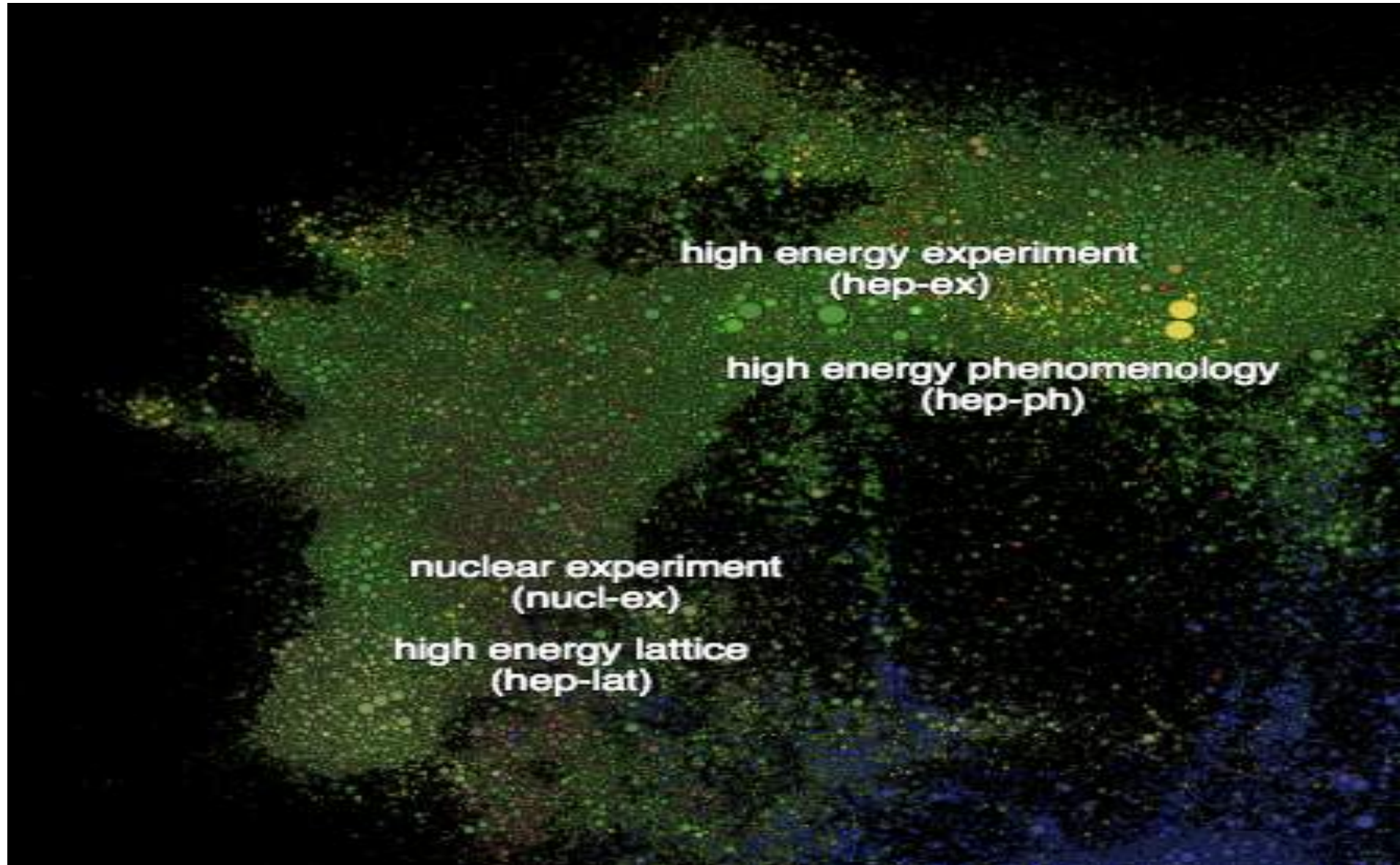
B is measured using NMR in terms of the proton Larmor frequency : ω_p

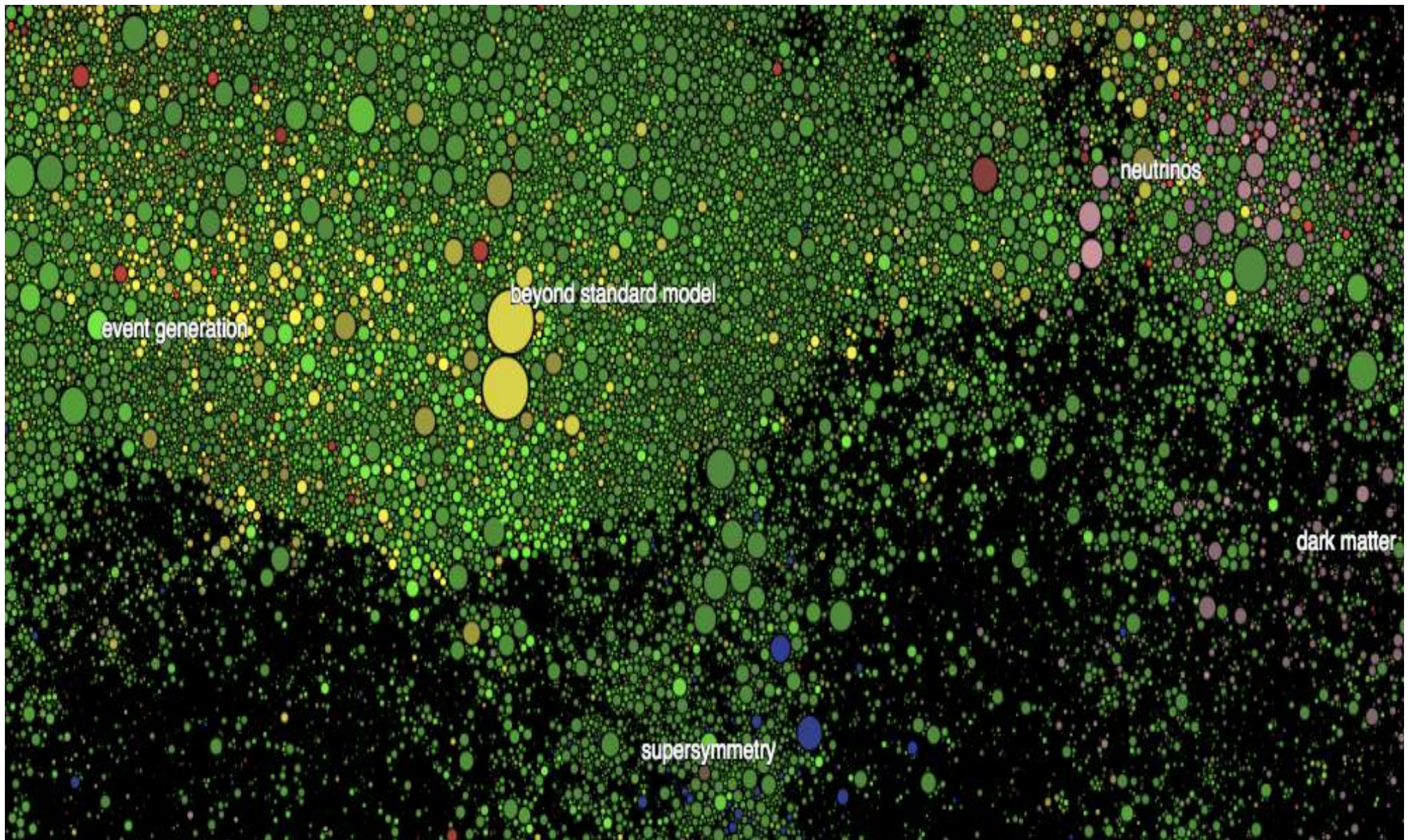
$$a_\mu = \frac{\omega_a/\omega_p}{\lambda_+ - \omega_a/\omega_p} ; \lambda_+ = \mu_{\mu^+}/\mu_p$$

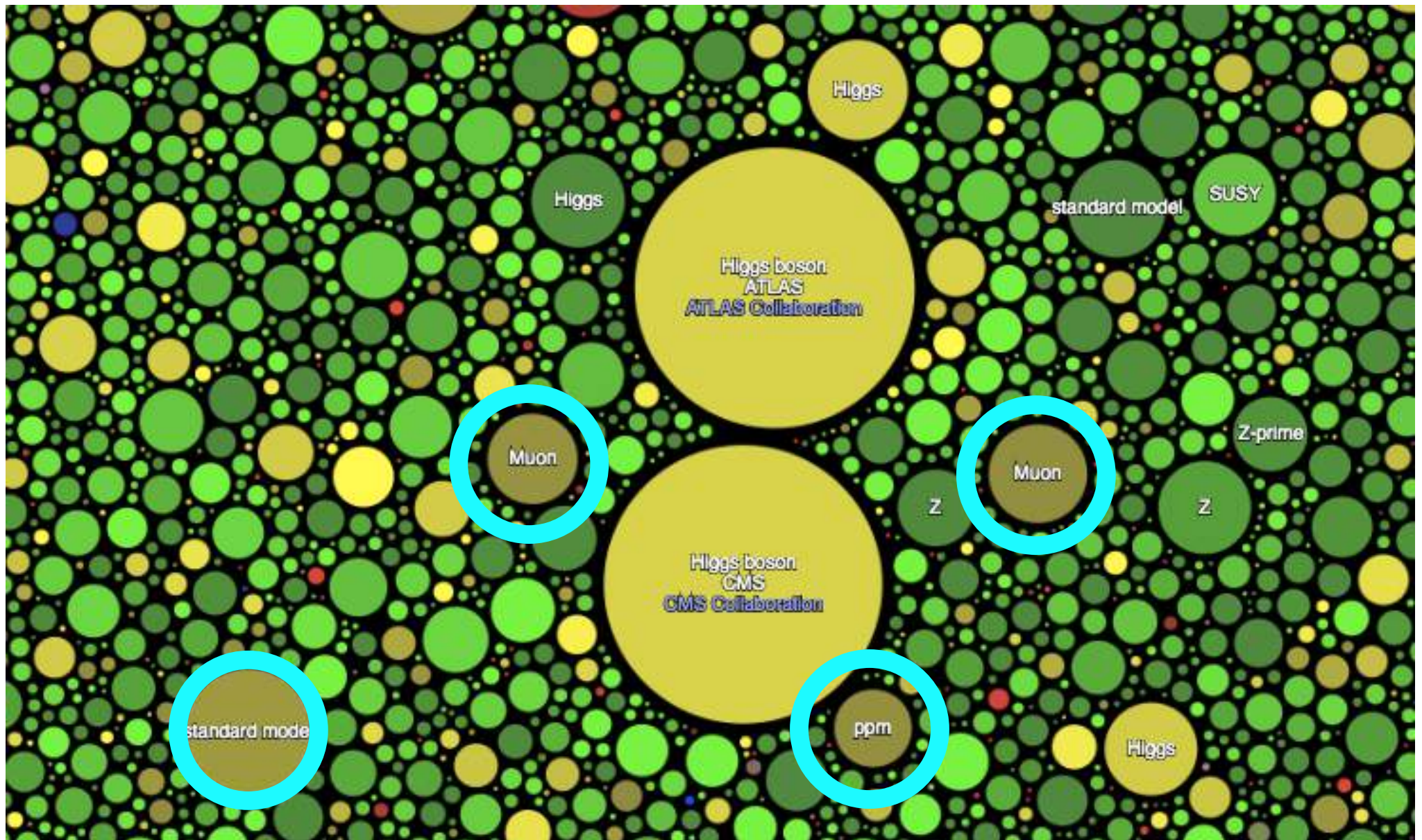
λ_+ measured from muonium hyperfine structure

Uncertainty in a_μ determined by precision of ω_p and ω_a measurements



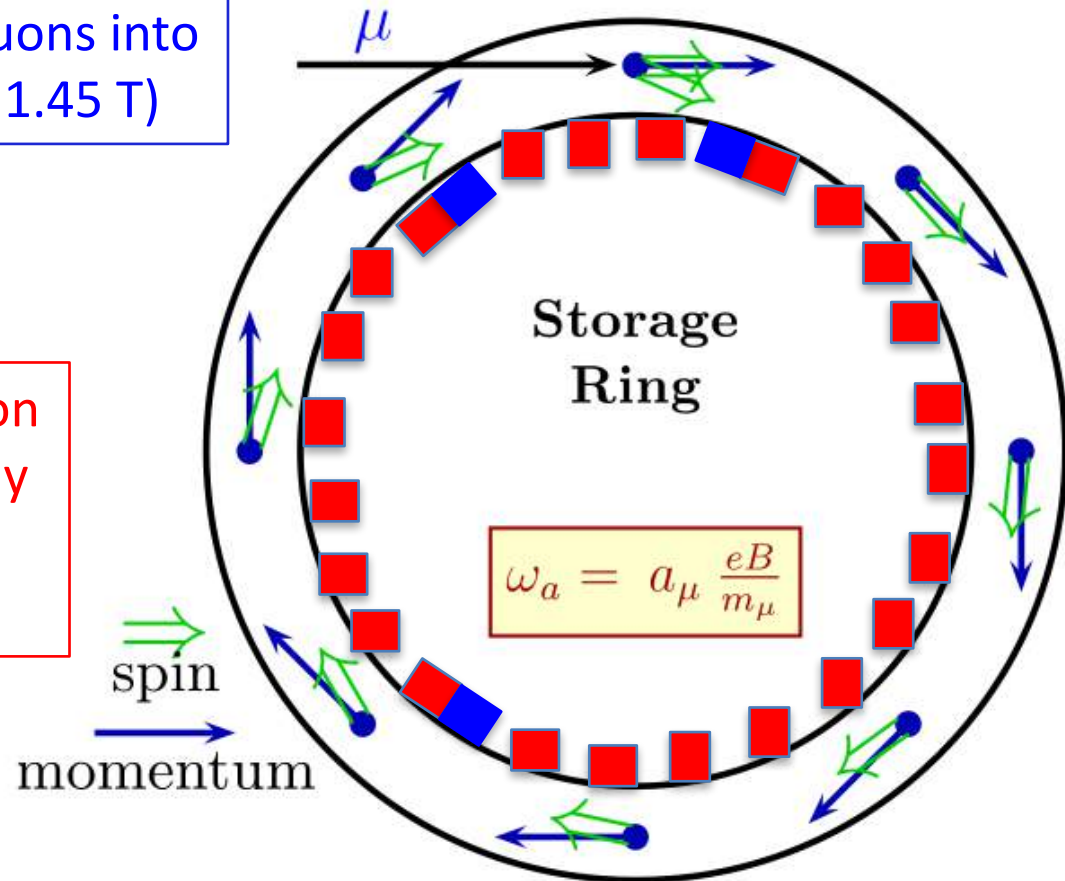






Inject 3.09 GeV muons into
a storage ring ($B = 1.45$ T)

Exploit property that direction
of e^+ from μ^+ decay is strongly
correlated with μ^+ spin
for highest energy e^+



24 calorimeters and 3 straw trackers measure e^+ for $O(1$ ms) for spills
separated by 10ms.

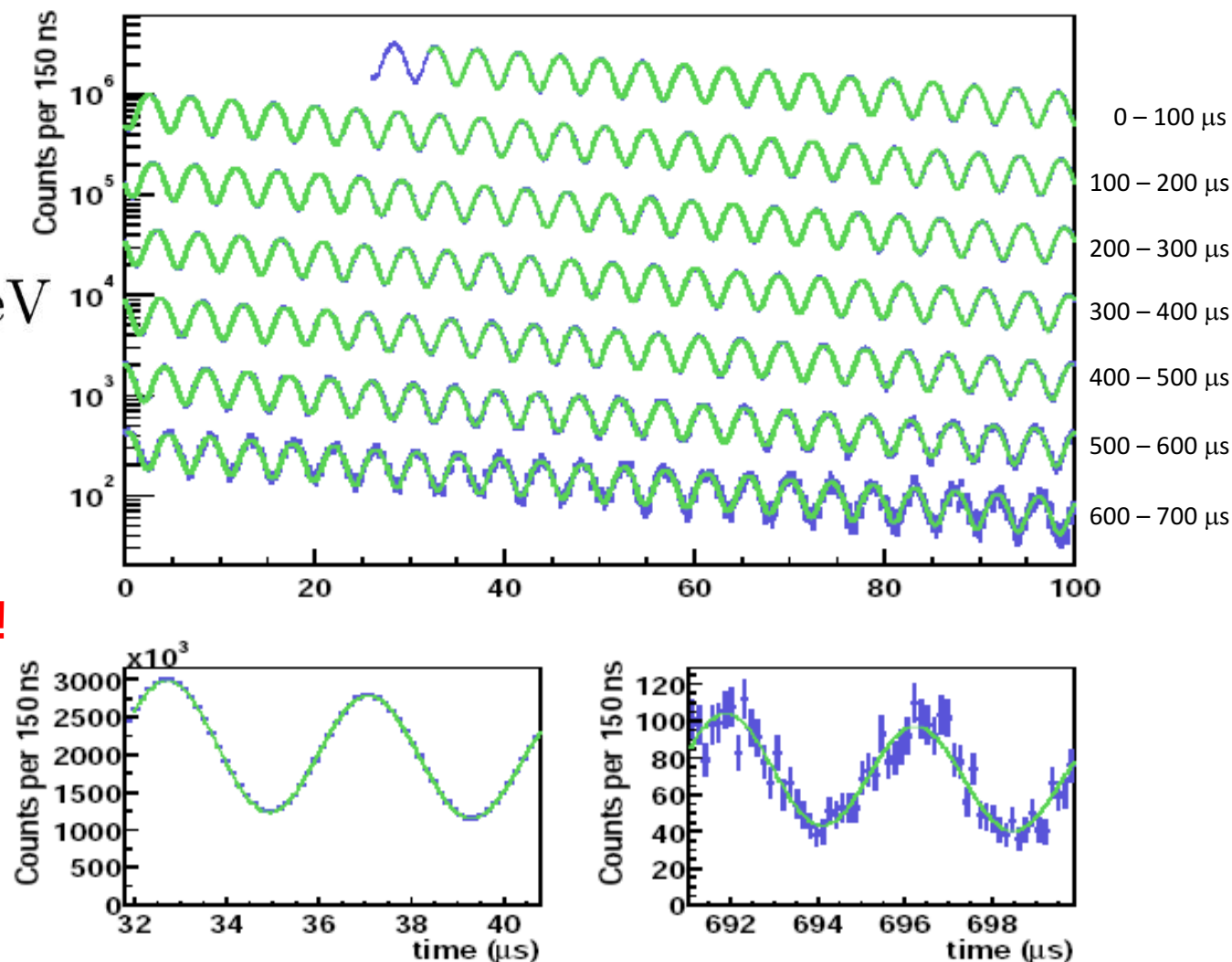
16,000 stored 3.09 GeV muons from 10^{12} protons per spill.

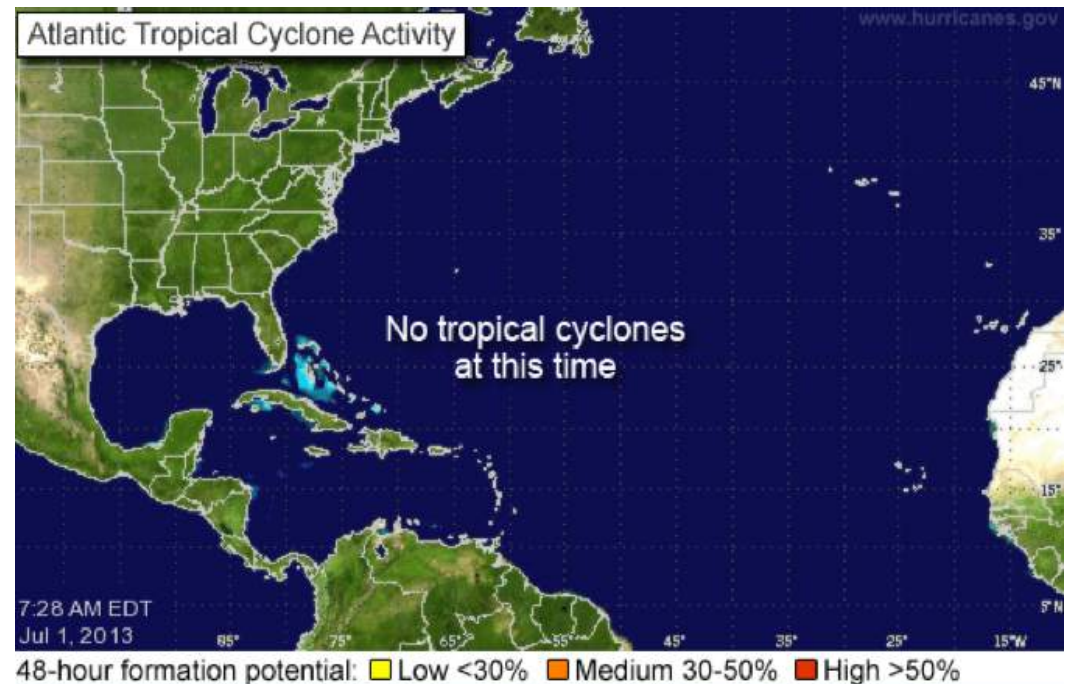
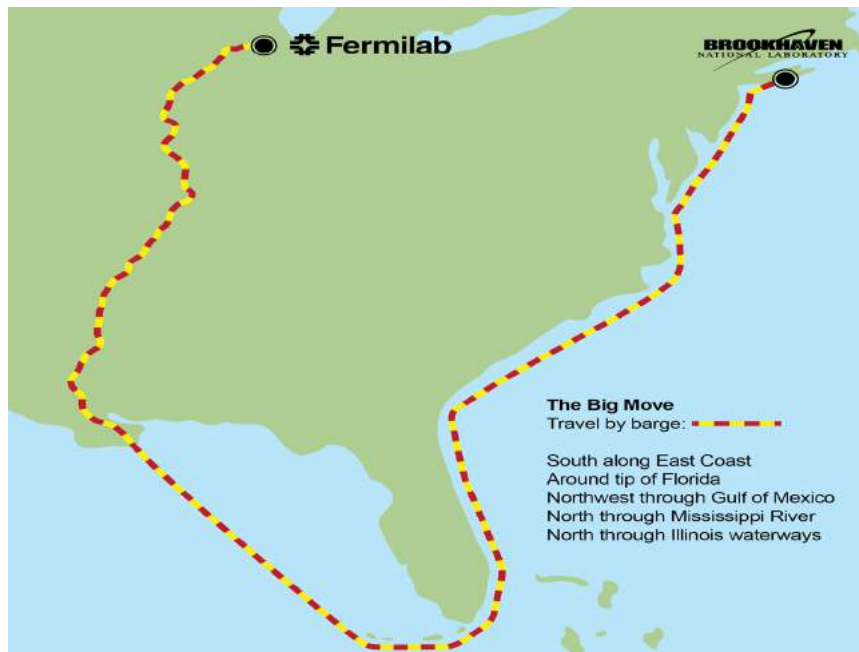
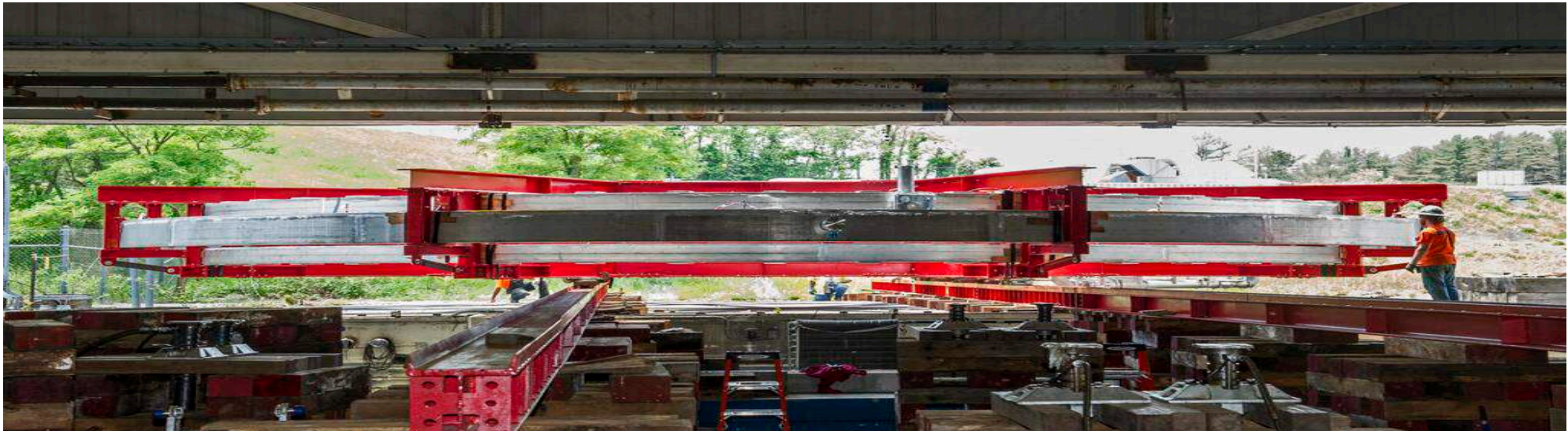


$$N_e(t) \simeq N_0 e^{-\frac{t}{\gamma\tau}} [1 - A \cos(\omega_a t + \phi_a)]$$

$E_{e^+} > 1.8 \text{ GeV}$

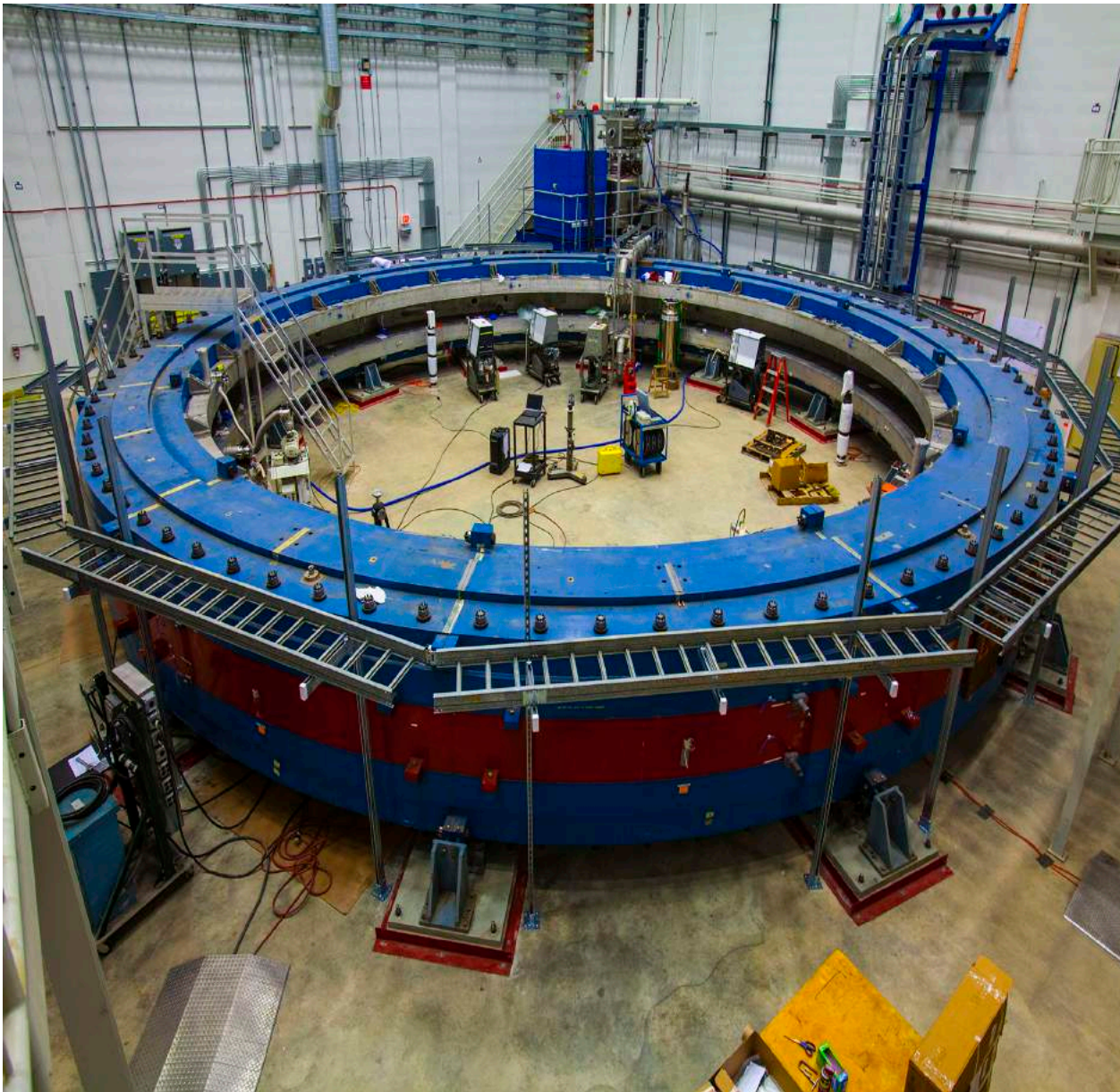
Need approx
100B muons !

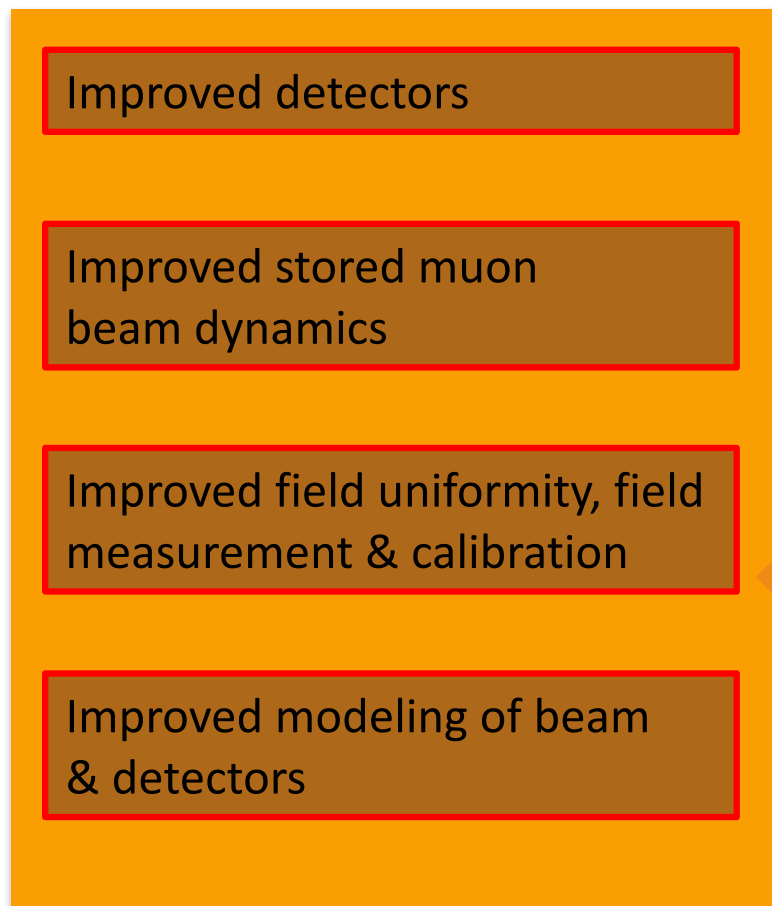
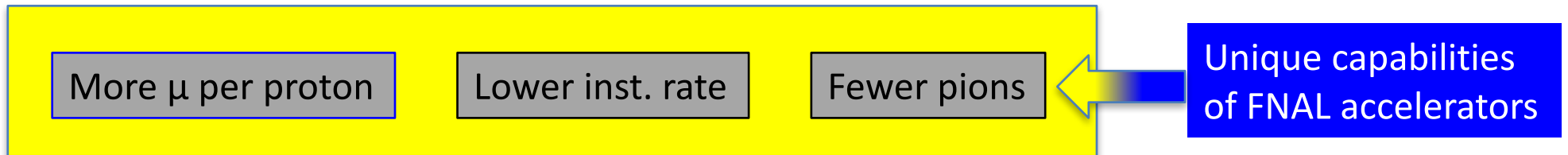












BNL $\rightarrow$ FNAL

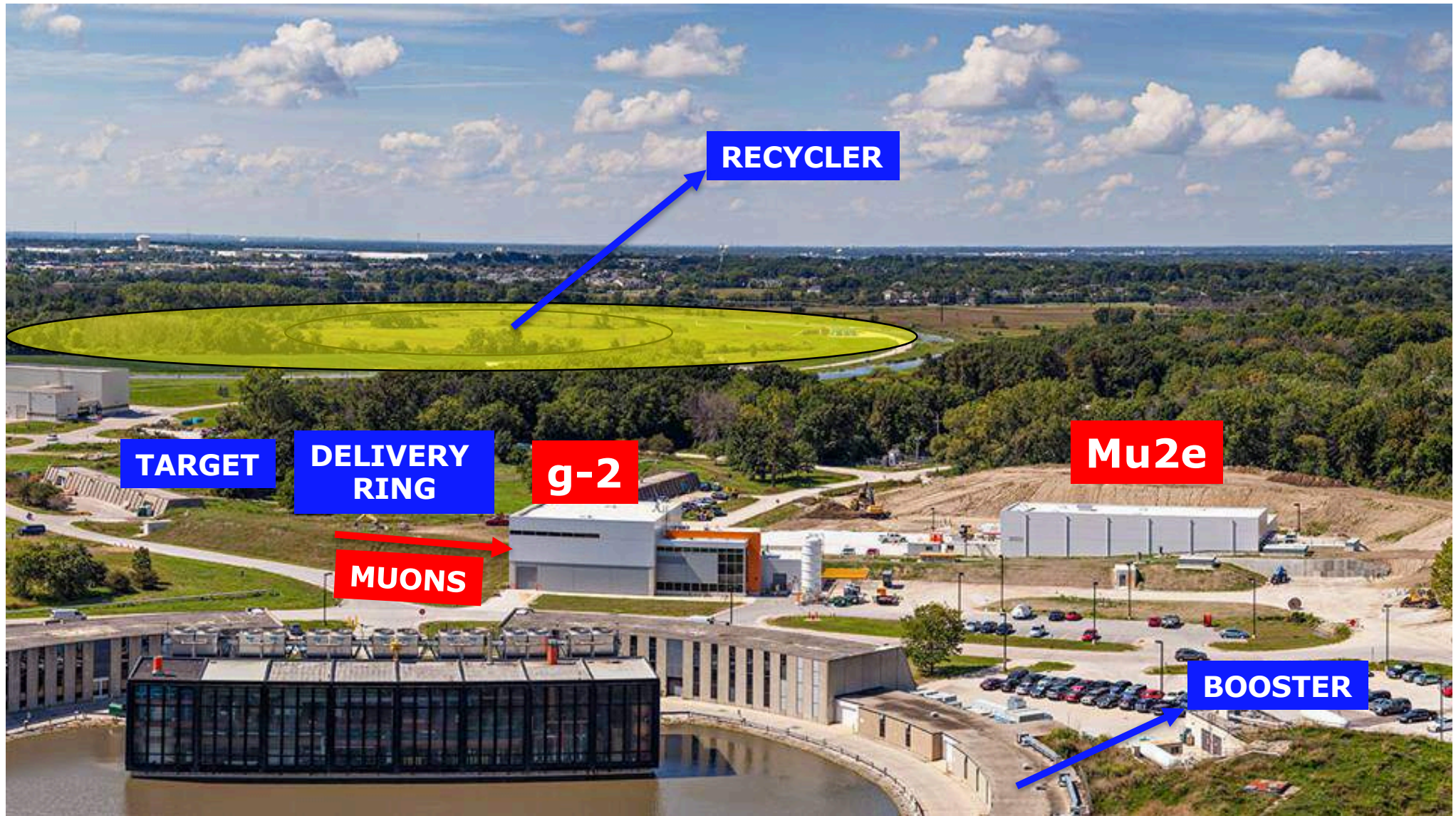
$[54 \text{ (stat.)} \oplus 33 \text{ (syst.)} \rightarrow 11 \text{ (stat.)} \oplus 11 \text{ (syst.)}] \times 10^{-11}$

0.54 ppm $\rightarrow$ 0.14 ppm

New / improved technologies

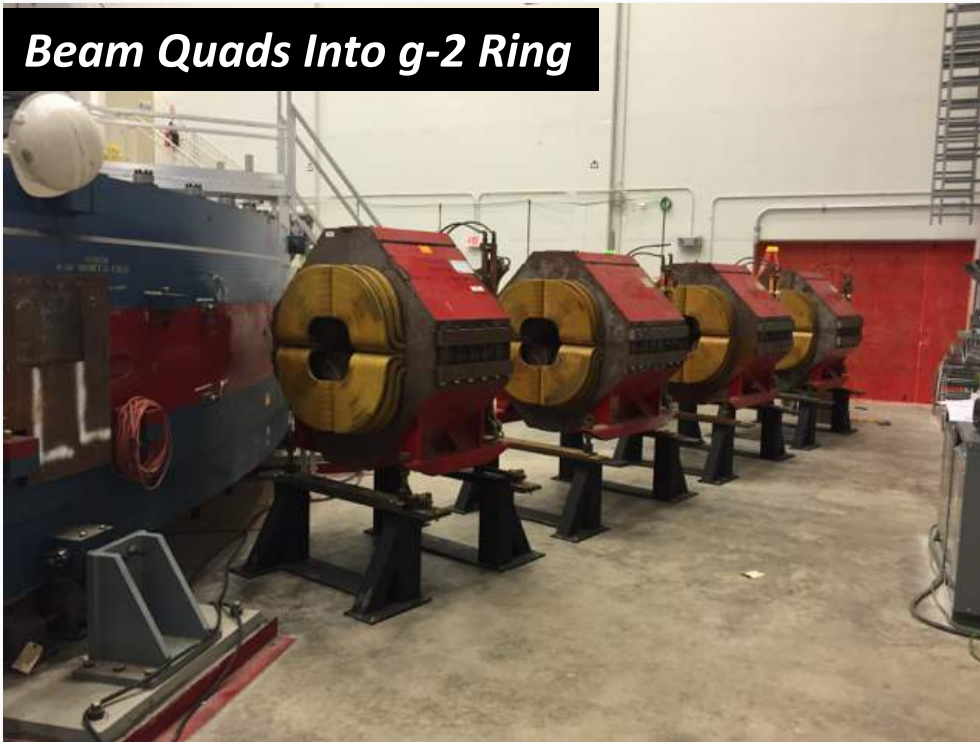
Additional collaborators

Building on wealth of experience from BNL E821 & other expts

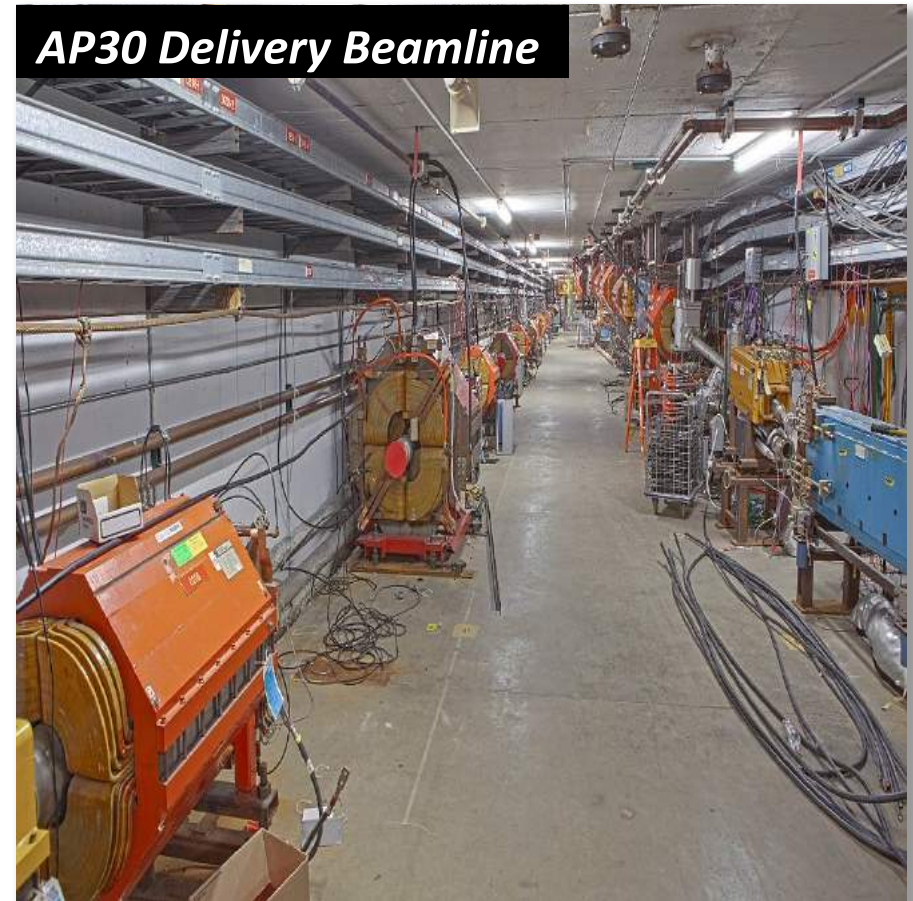


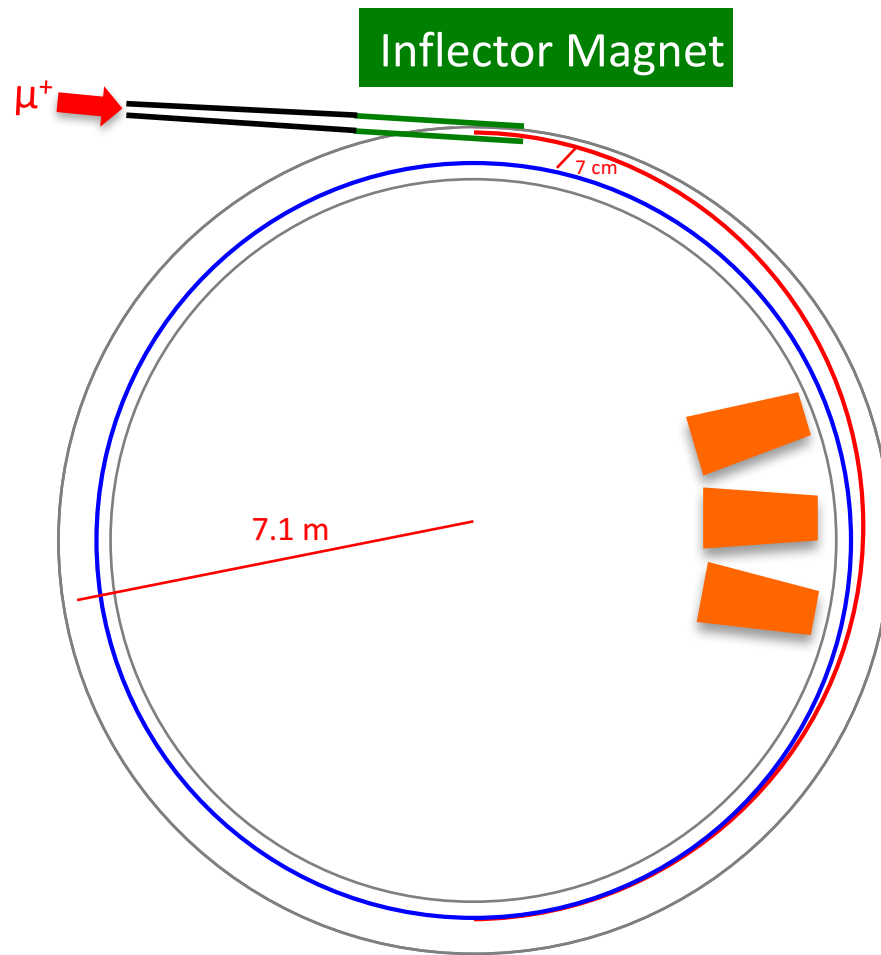
Beam infrastructure 90% complete
First beams (low muon intensity) from April 2017

Beam Quads Into g-2 Ring



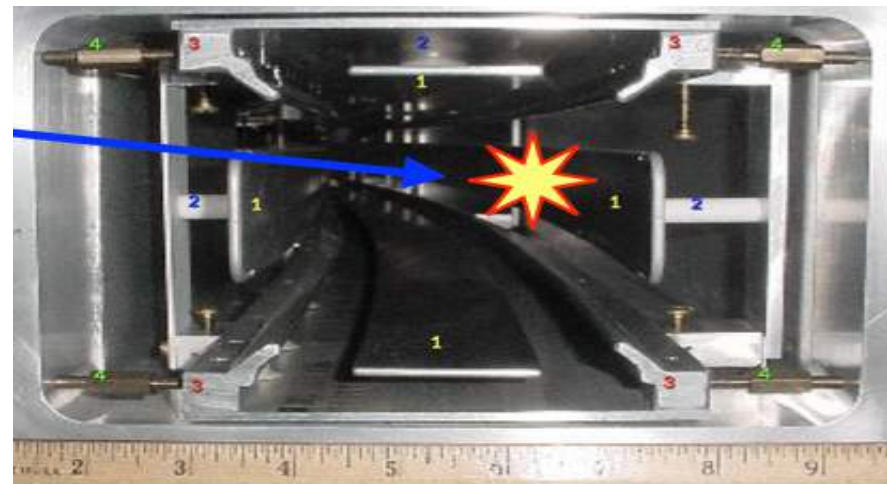
AP30 Delivery Beamline

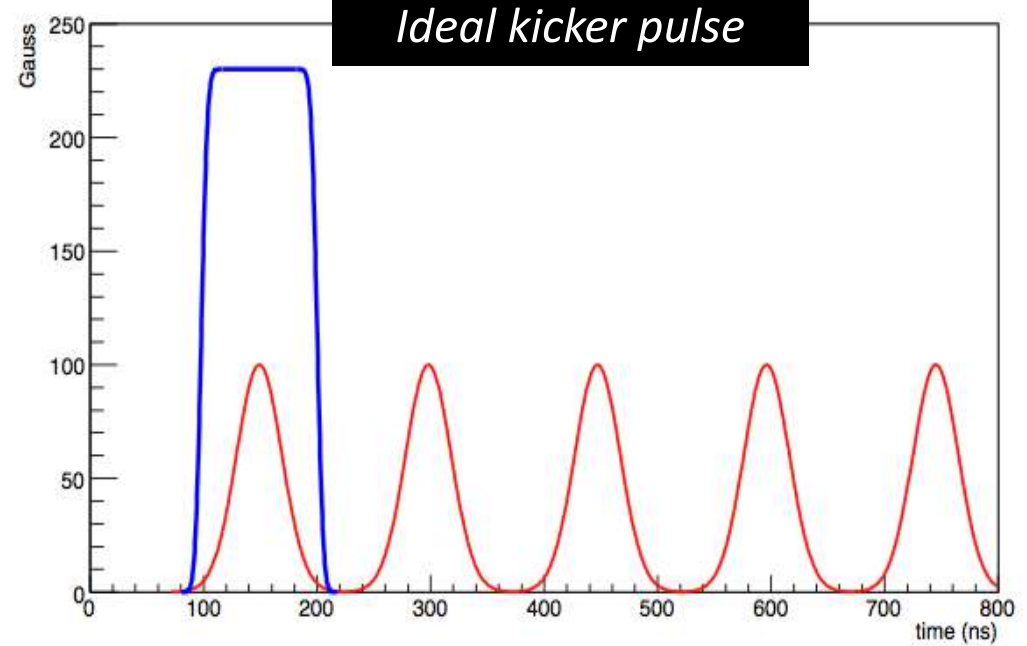
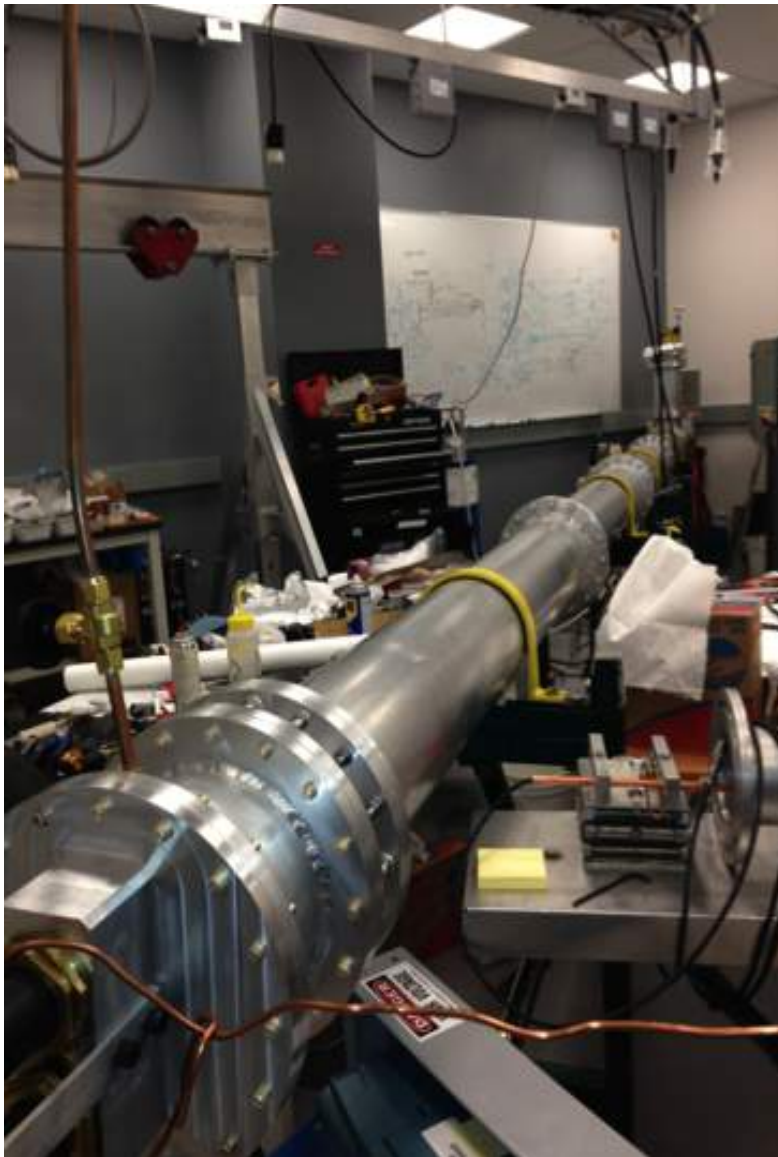




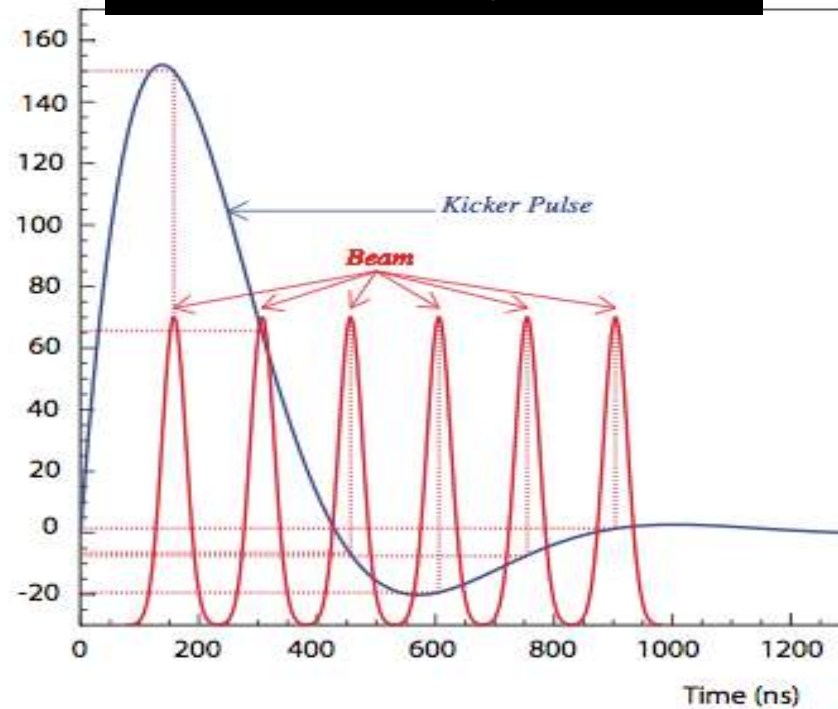
Beam doesn't enter on the correct orbit and needs a kick to get there !

Kicker magnets

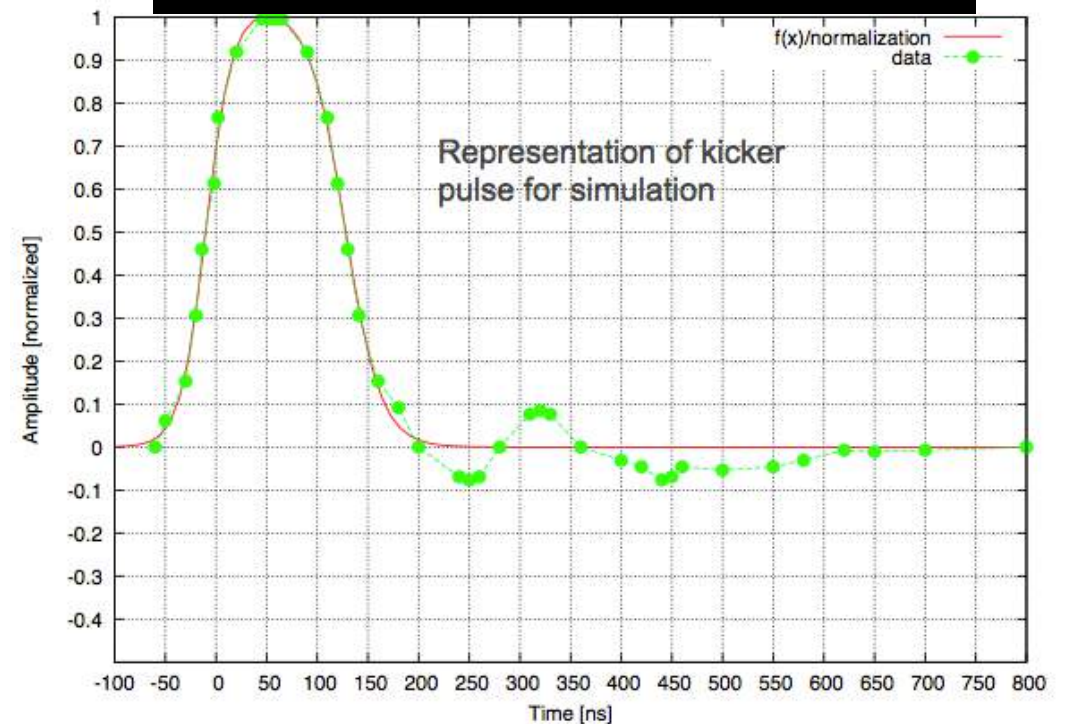


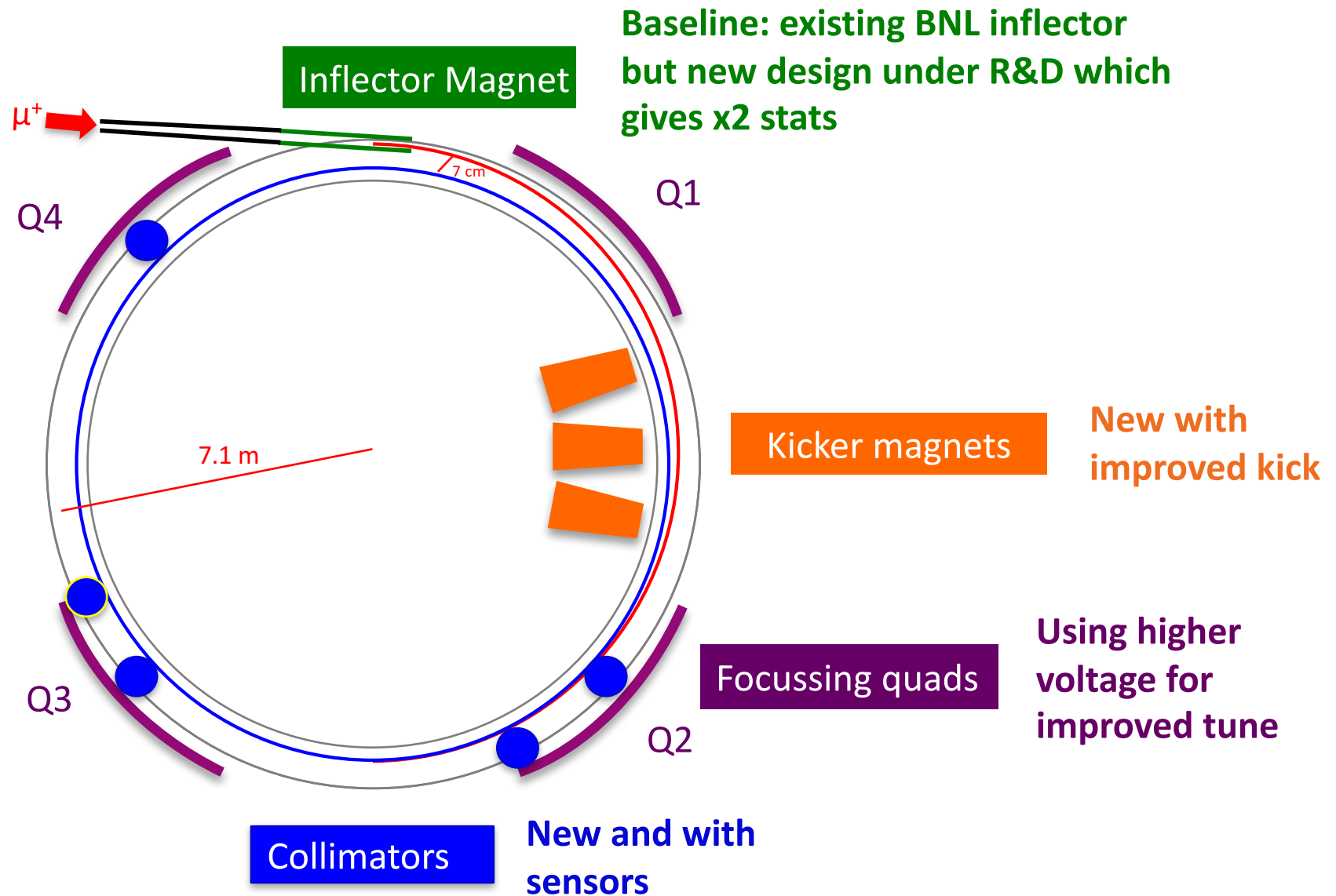


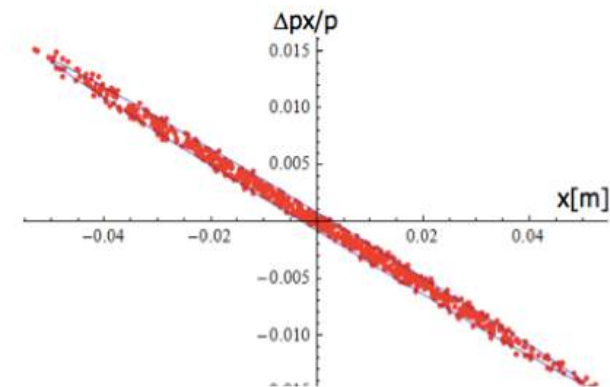
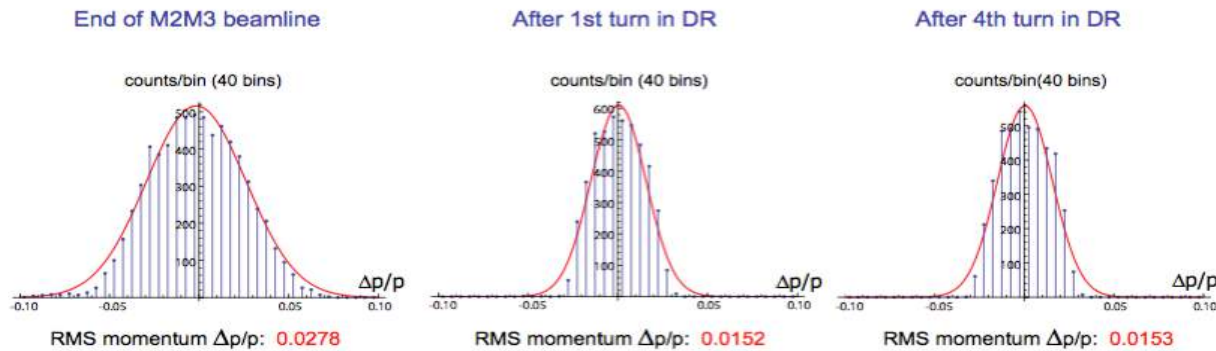
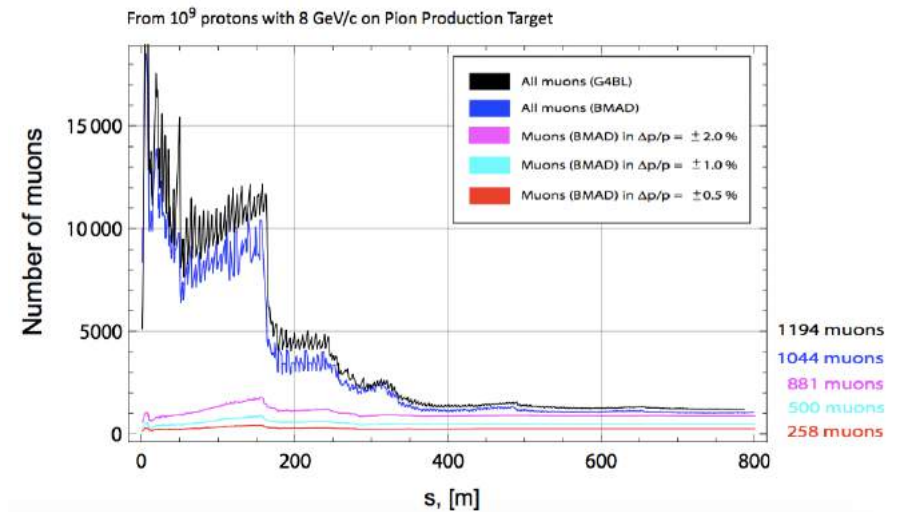
BNL kicker pulse



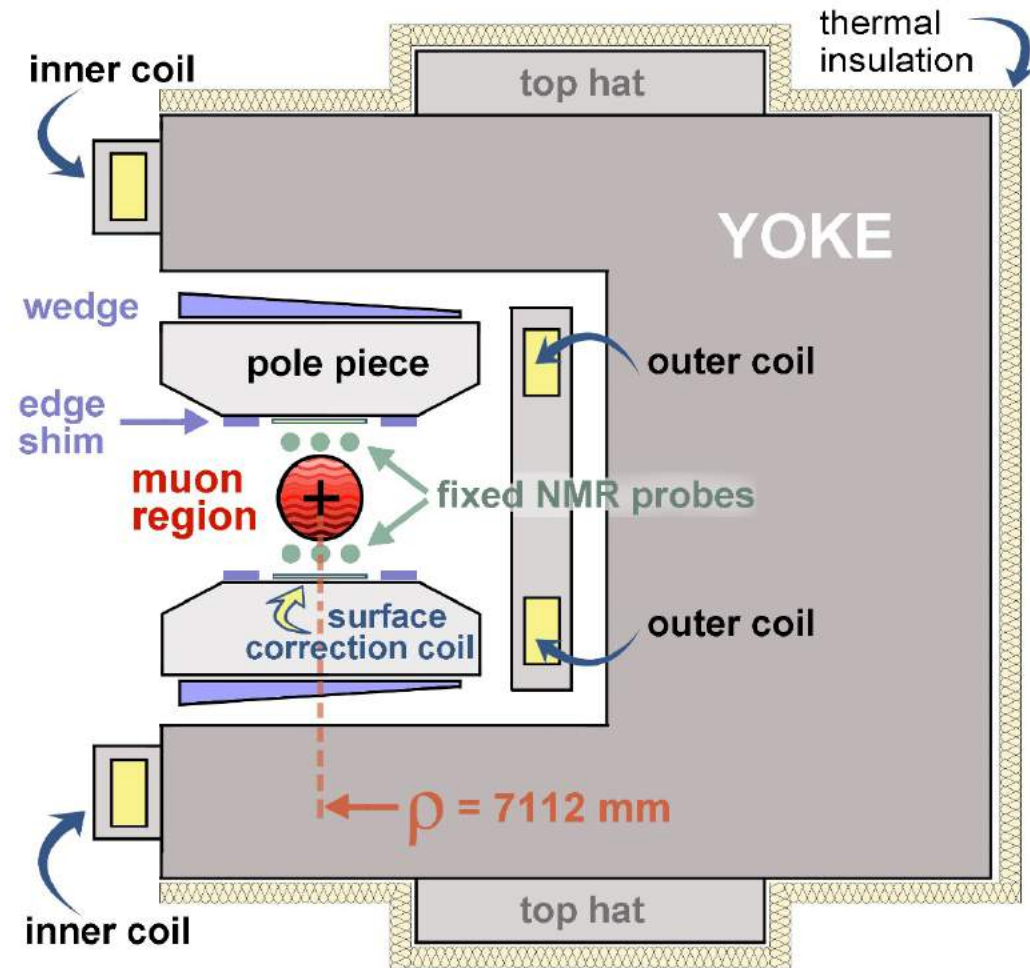
New FNAL (Cornell) kicker pulse



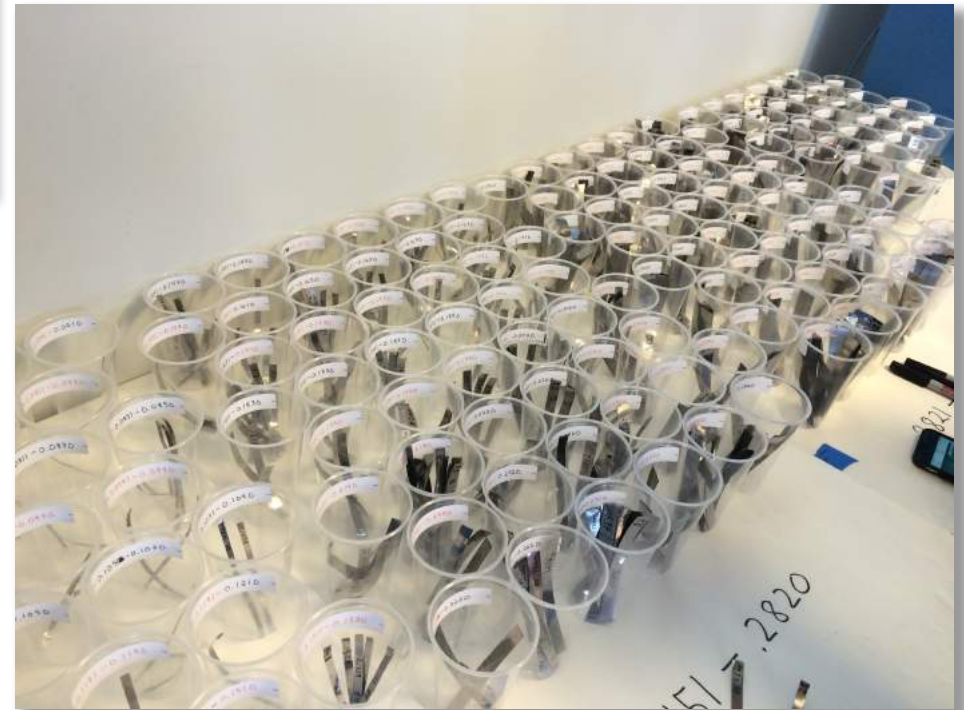


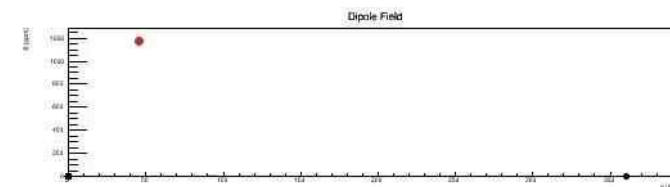
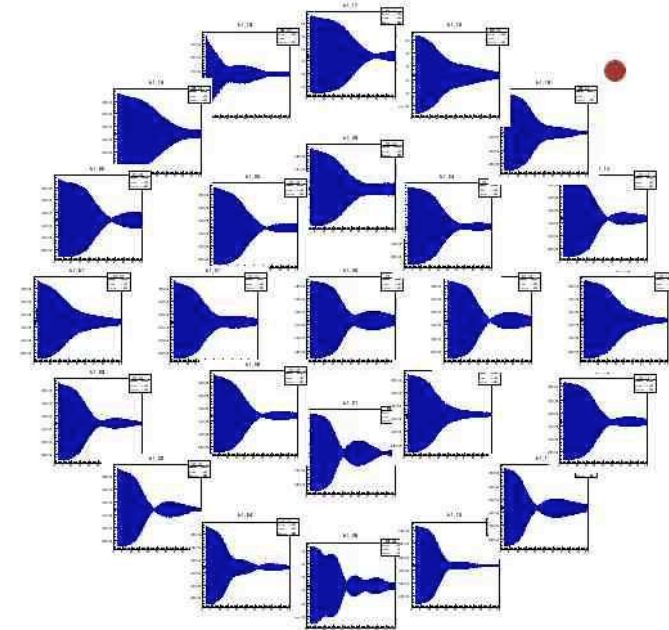


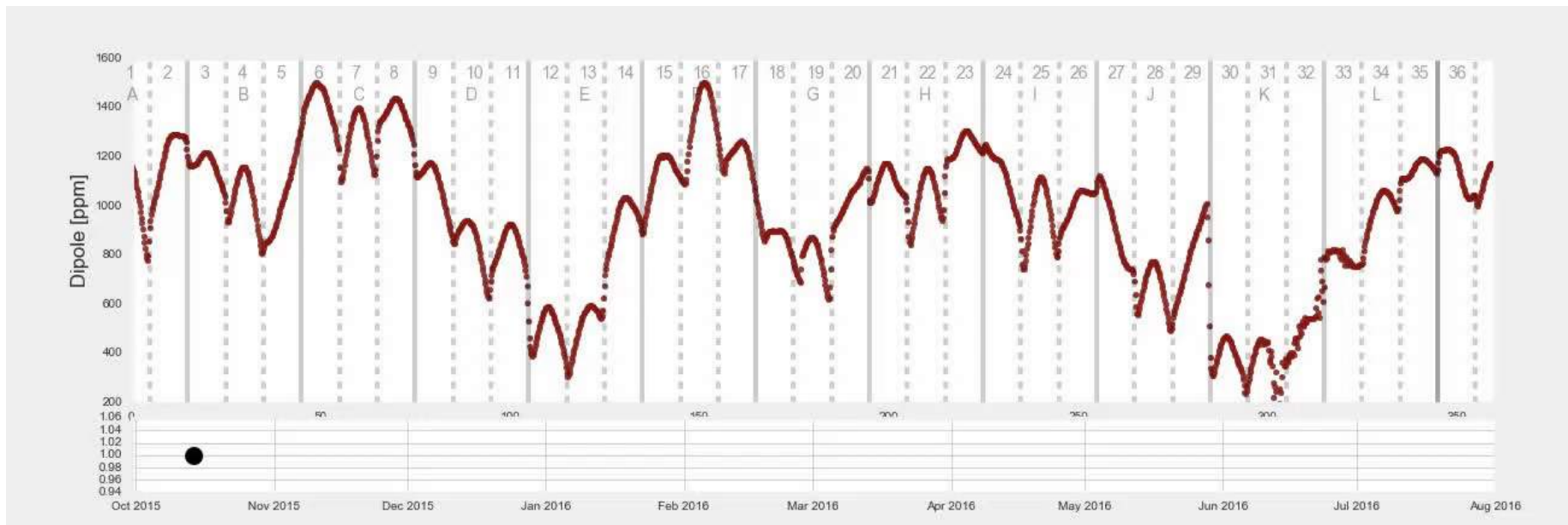
100 active surface coils



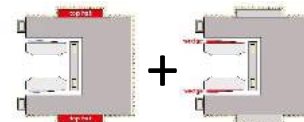
Yoke : 26 tons to 125 microns....







Poles

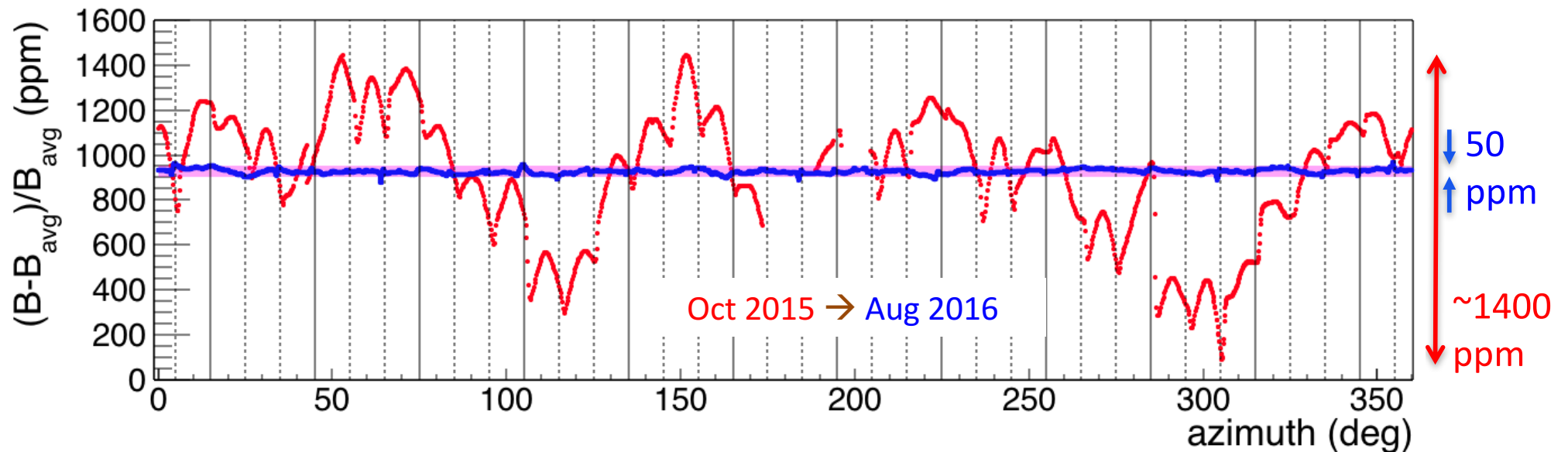


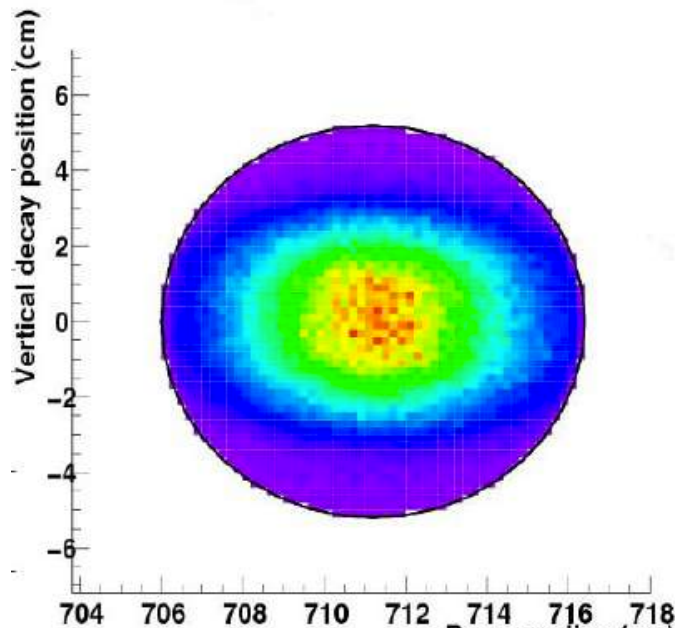
Top hats & wedges



Surface foils

Field uniformity x30 improved in a year and now x4 better than achieved at BNL after first shimming round.

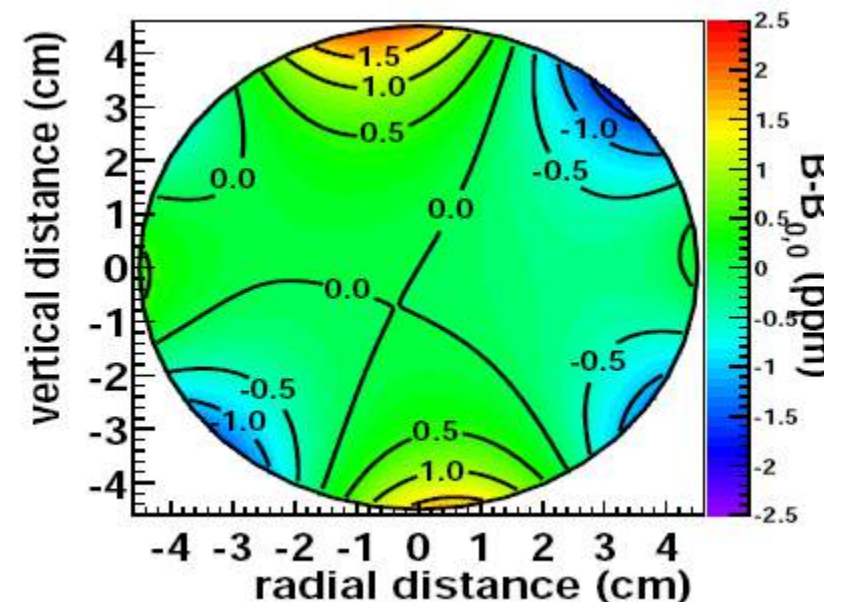
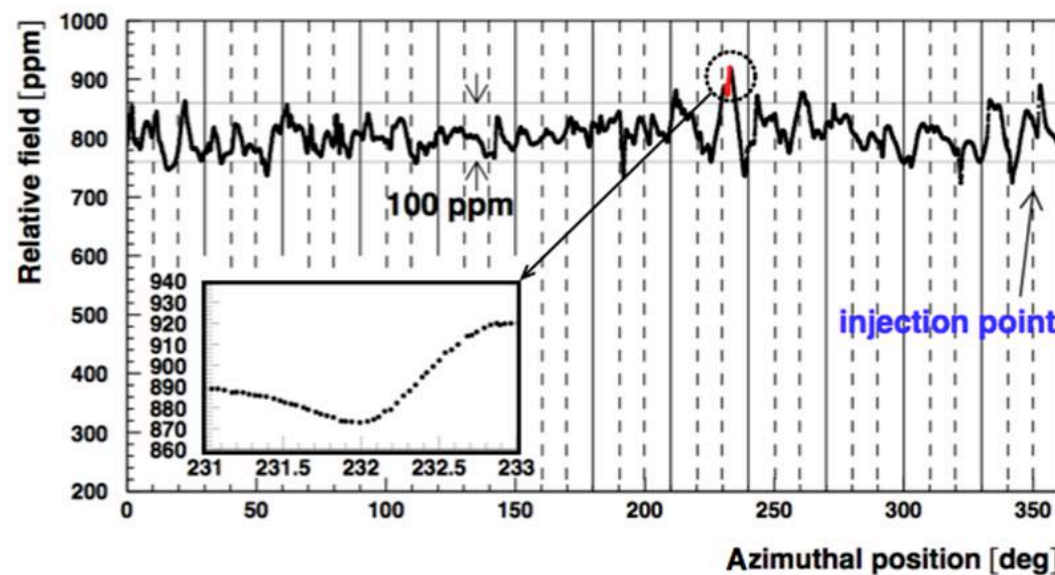




Muons are distributed over storage volume

B-field is not uniform over this volume

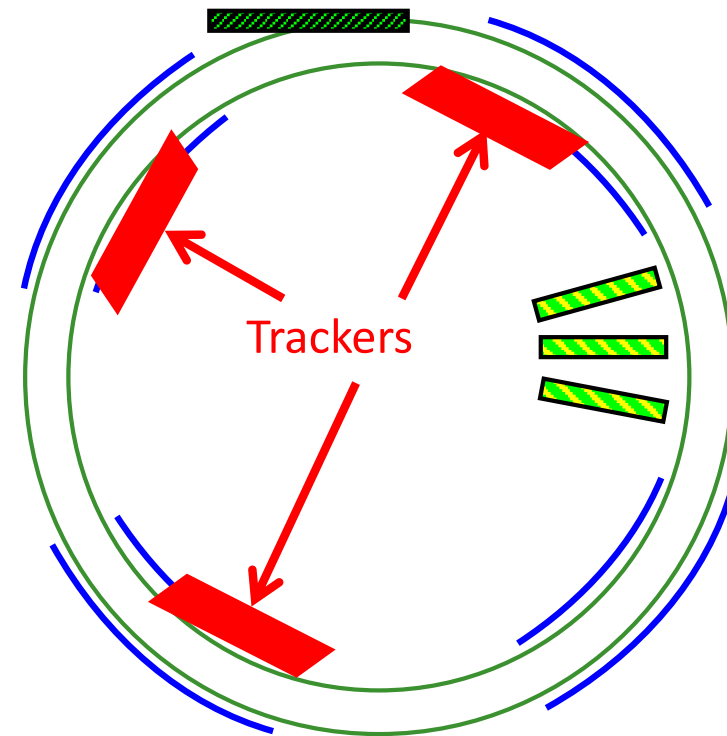
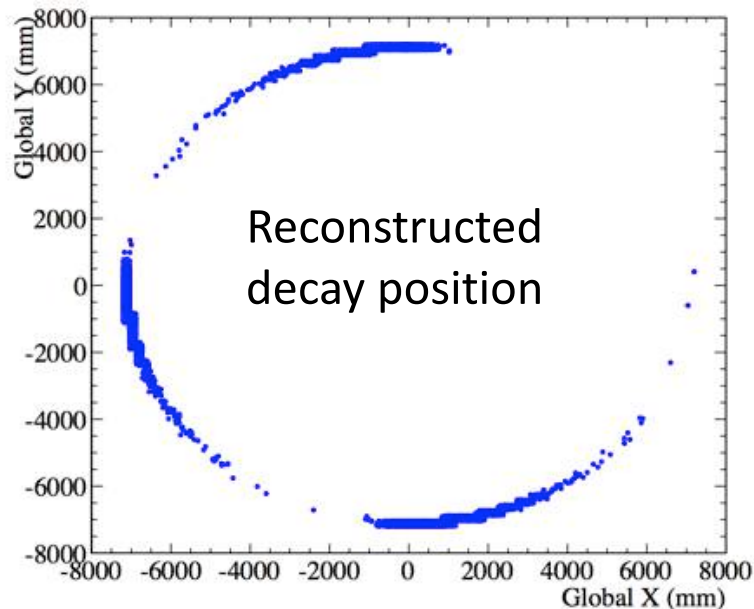
Need to convolute the two.

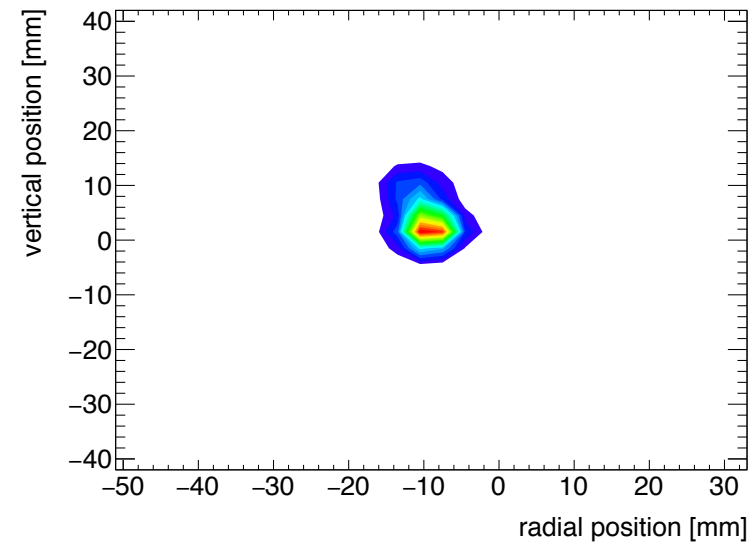
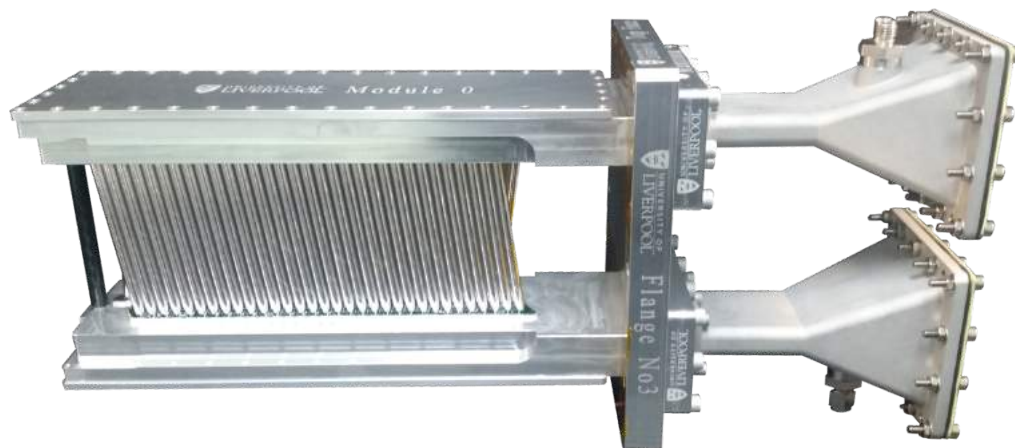
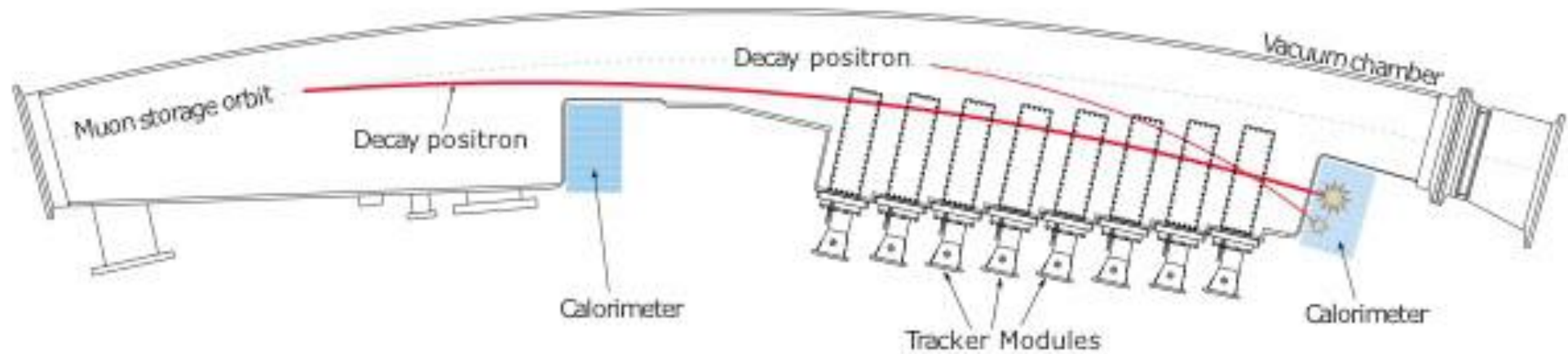


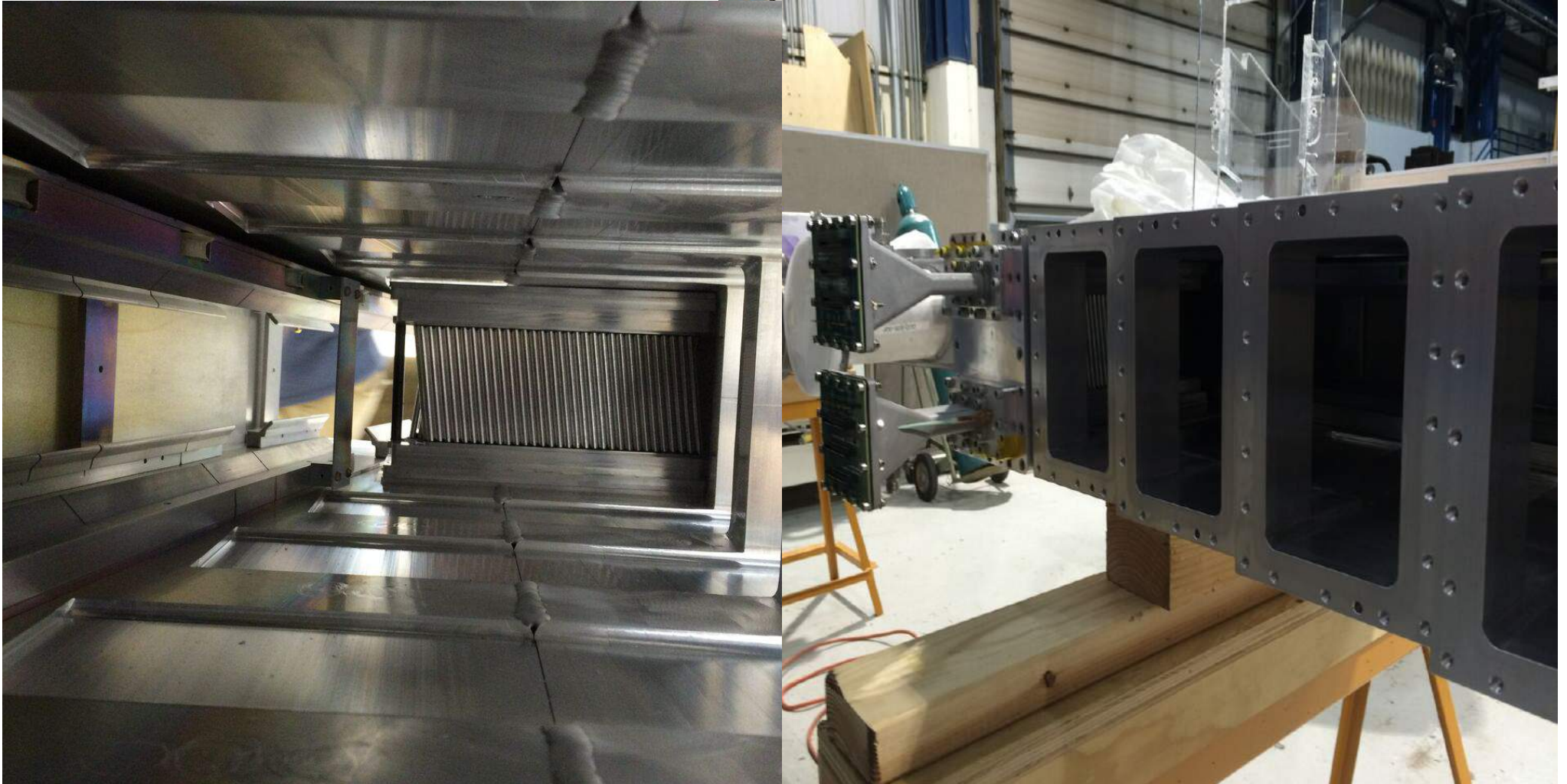
Measure beam profile

Identify pileup and muons lost from beam

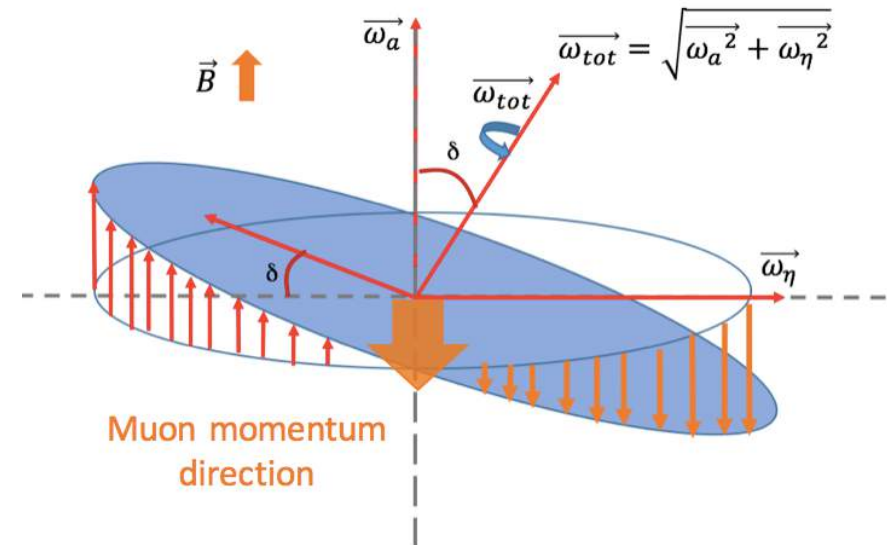
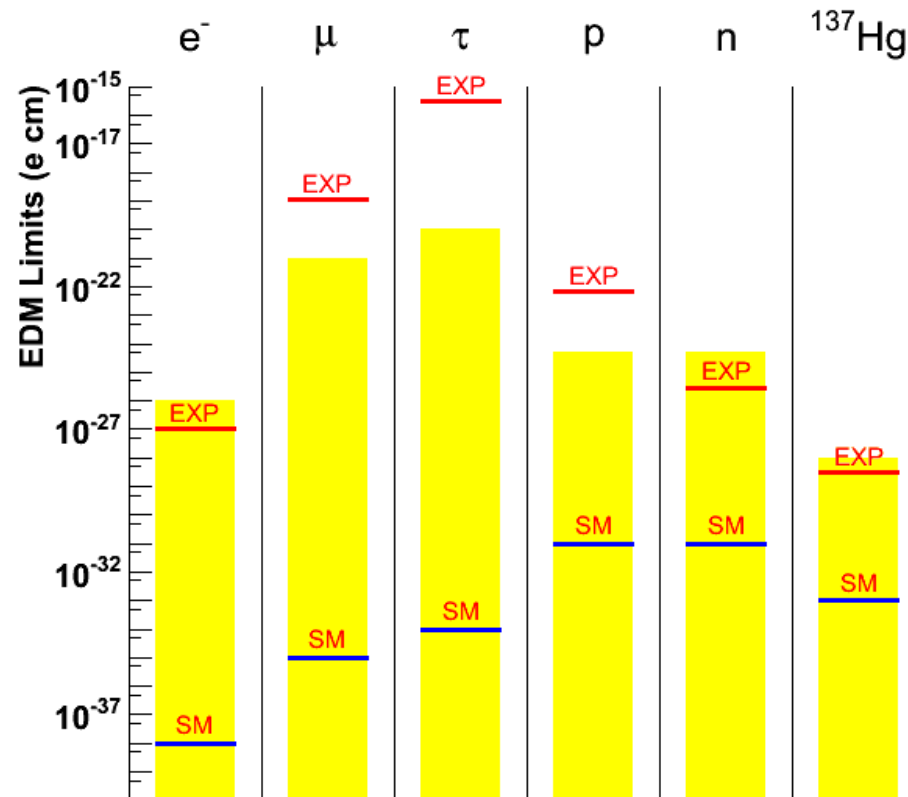
Measure EDM







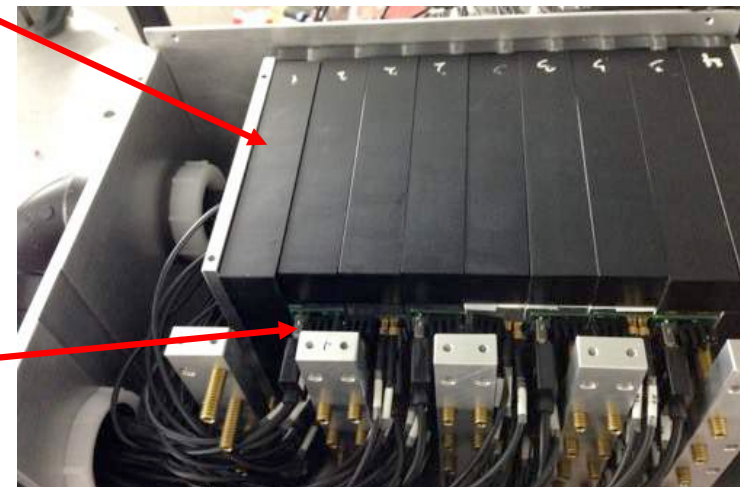
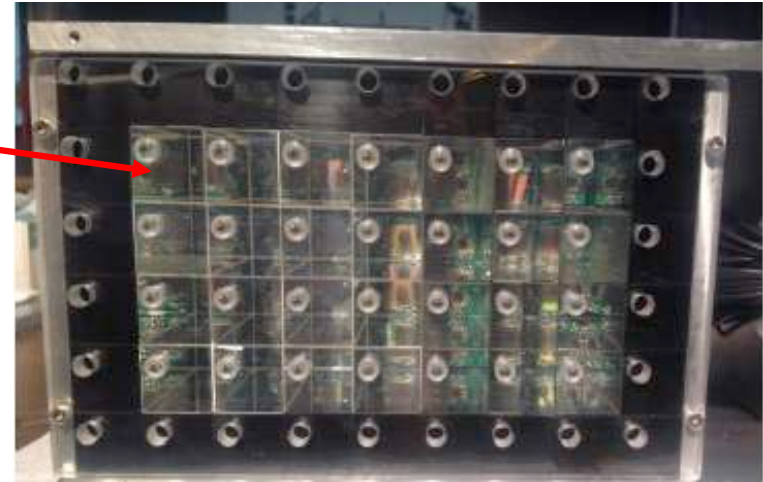
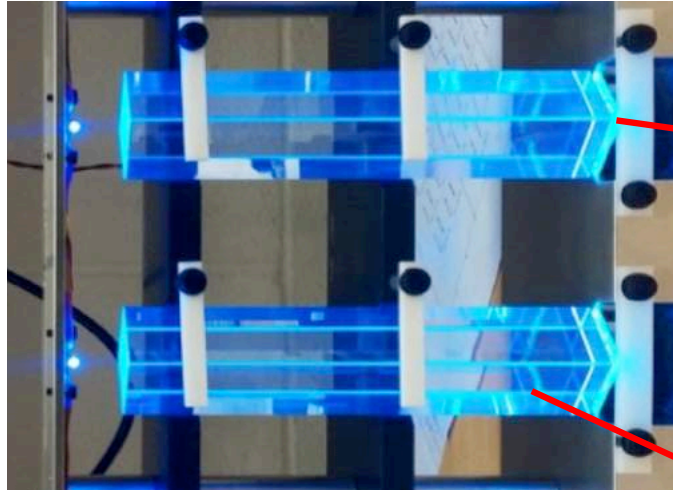
Essentially zero in SM : any observation is new physics



Expect several billion events in the trackers and so reach 10^{-21} vs 2×10^{-19} at BNL

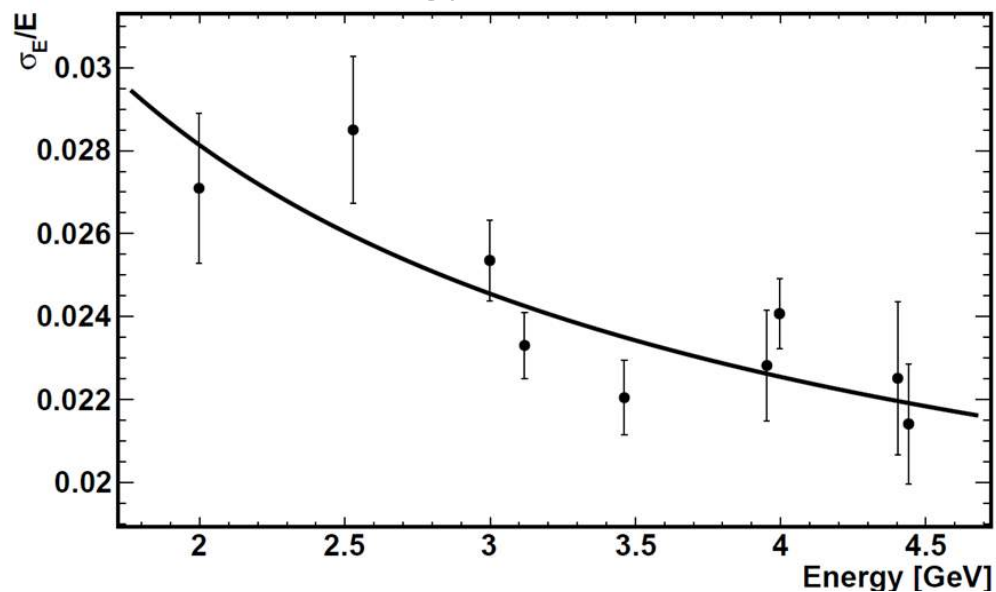
Needs non mass-scaling BSM effects to be in expt's reach given e^- EDM limit

50 MeV resolution at 2 GeV and pulse separation < 5ns.

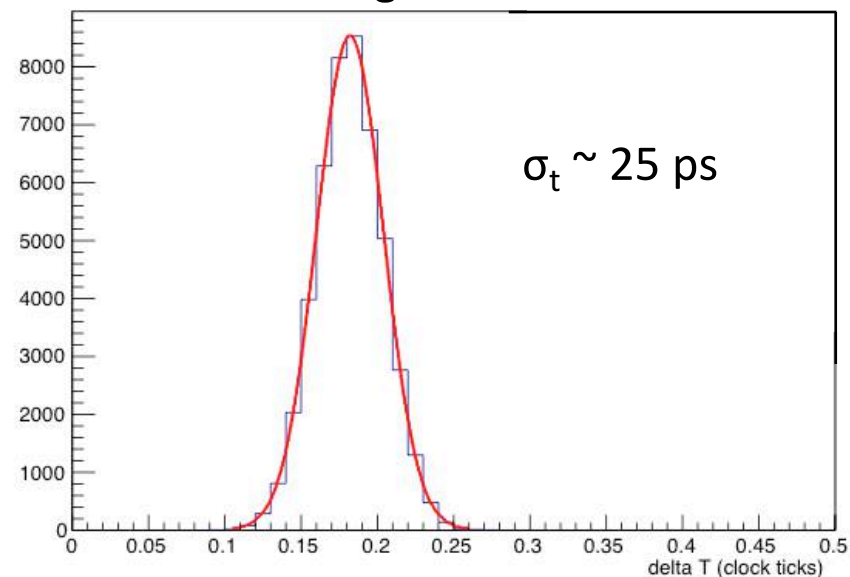


Energy Resolution

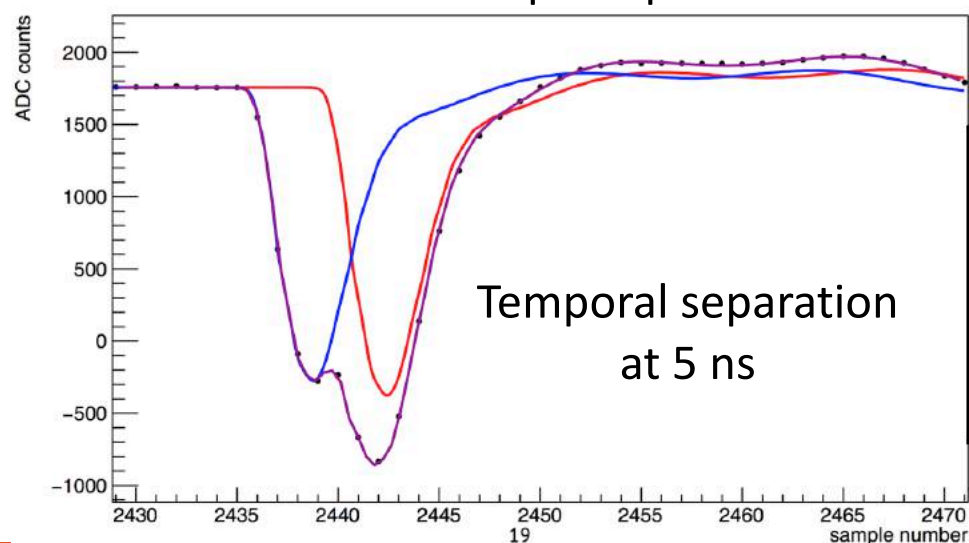
[NIM A 783 \(2015\),](#)



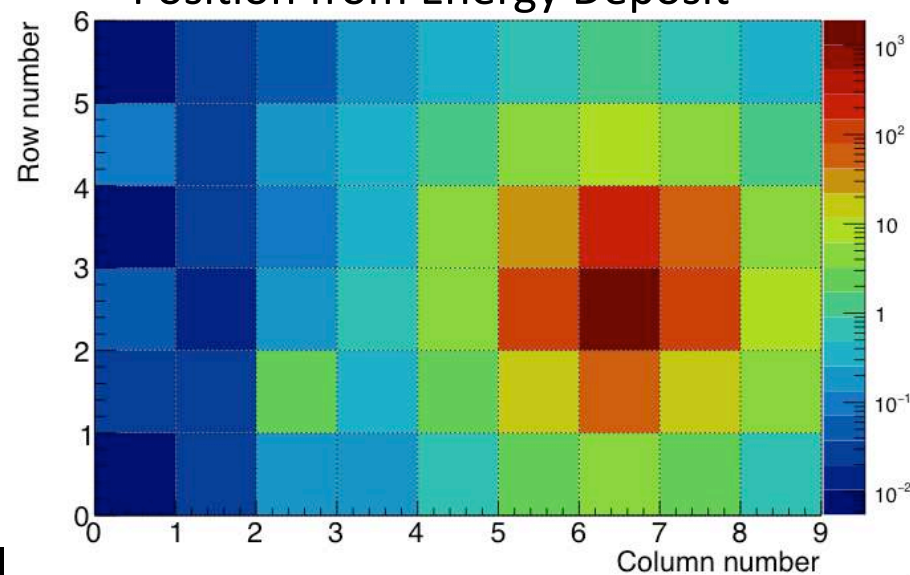
Timing Resolution



Electron pile-up



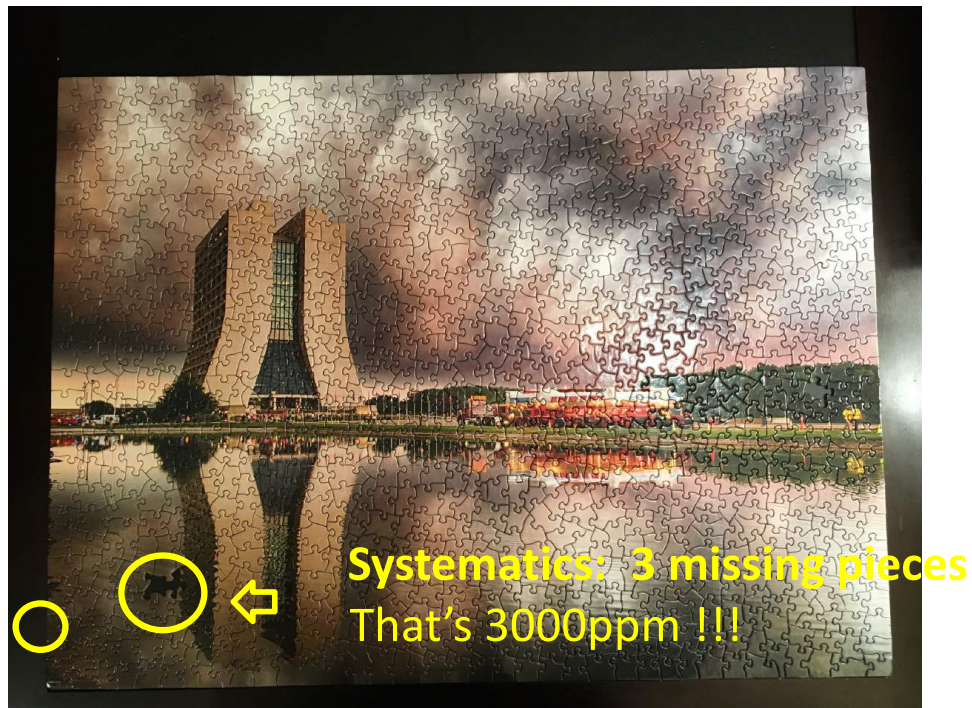
Position from Energy Deposit

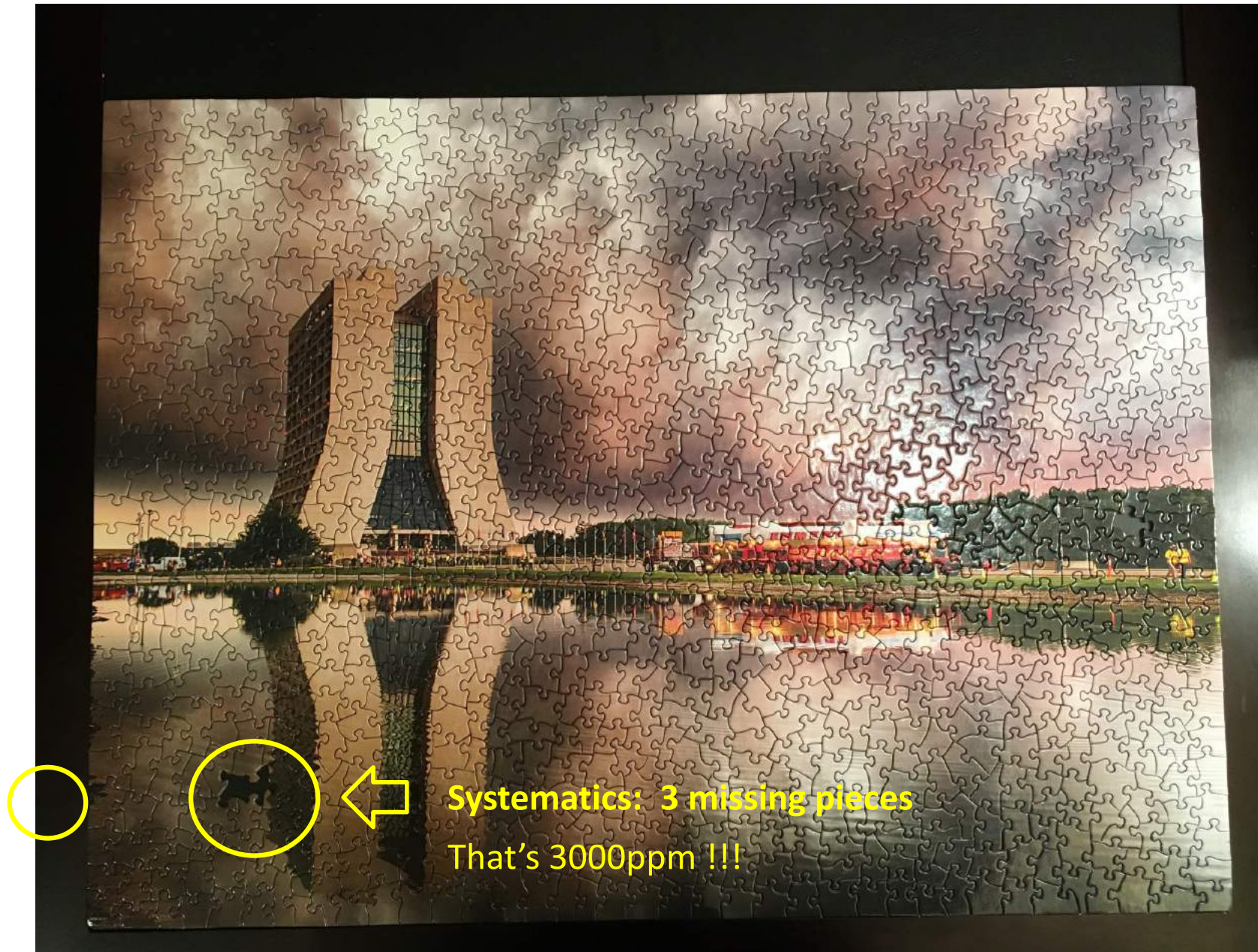


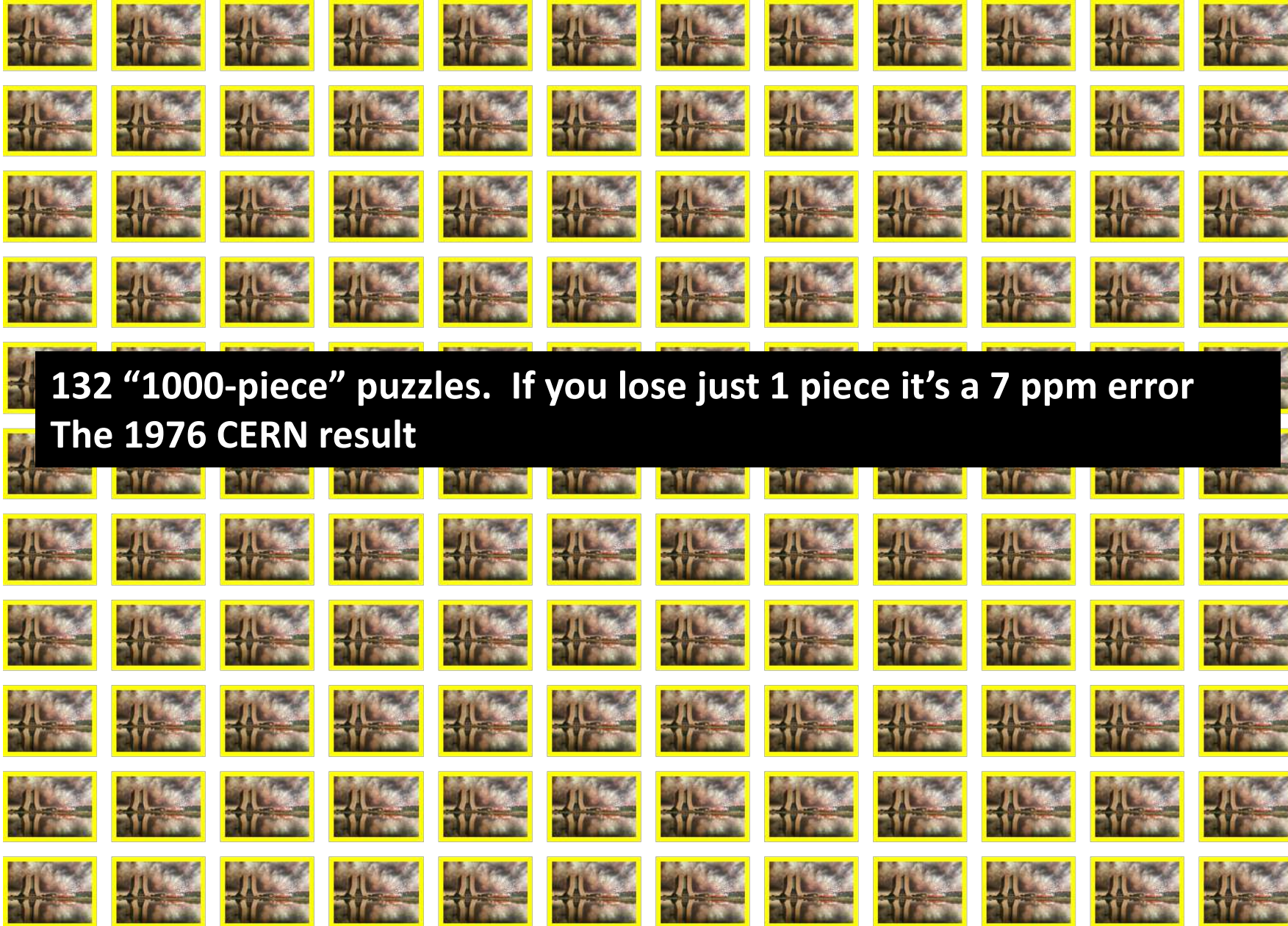
1st beam is expected in April with first muon data to be accumulated towards the end of 2017.

BNL-level statistics by mid-2018 and by 2020 x20 the statistics

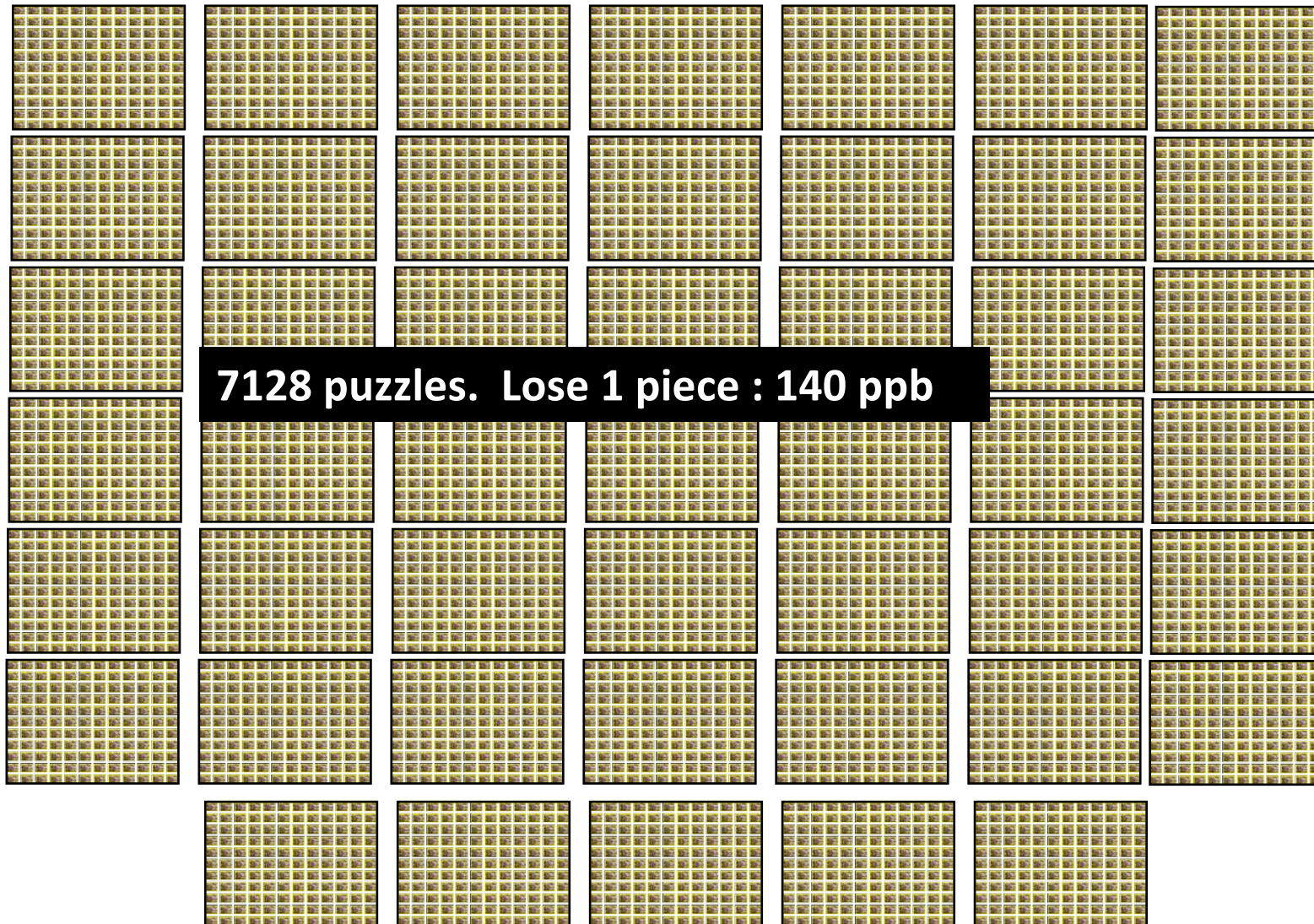
Expectation is to publish 3 results with 100%, 50% and 25% of BNL precision

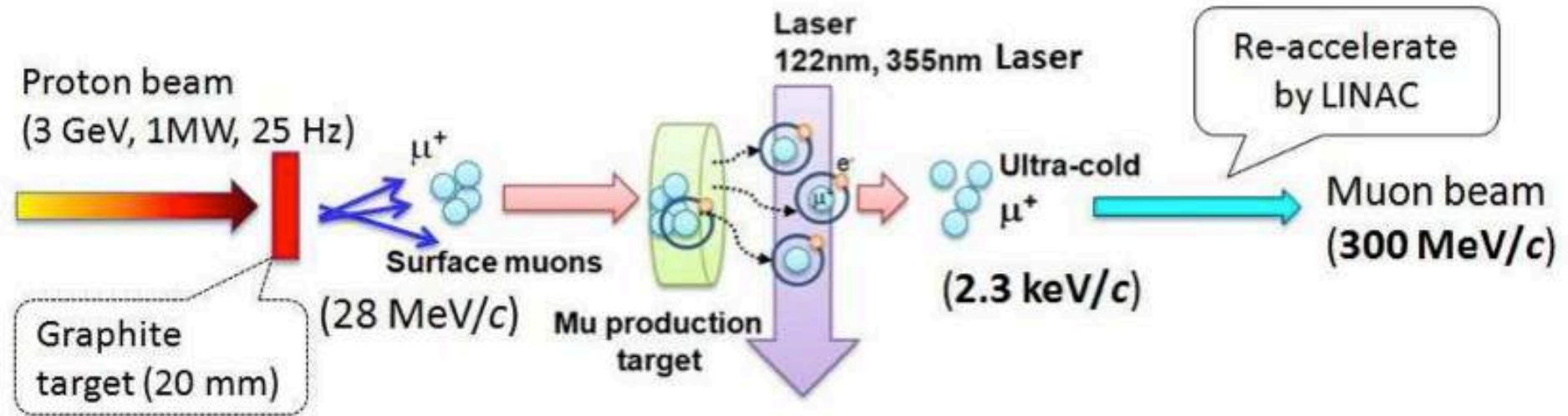






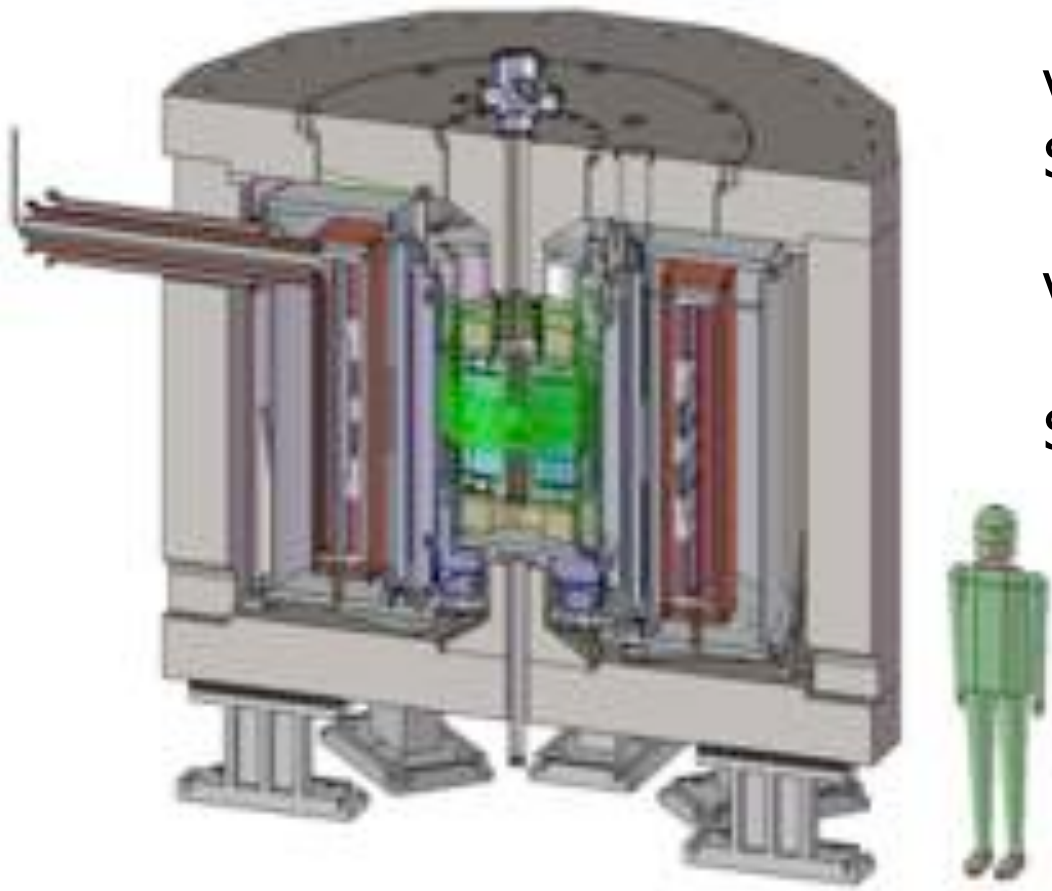
132 “1000-piece” puzzles. If you lose just 1 piece it’s a 7 ppm error
The 1976 CERN result





Requires several innovations to achieve 10^6 muons/sec

- production of sufficient muonium using special materials
- pulsed 100 μ J VUV lasers to ionise muonium
- muon linac keeping $\Delta p_T/p_T < 1e-5$: world's 1st muon accelerator !



Very precise tracking using
Si detectors

Very uniform field (MRI magnet)

Spiral 3D beam injection !

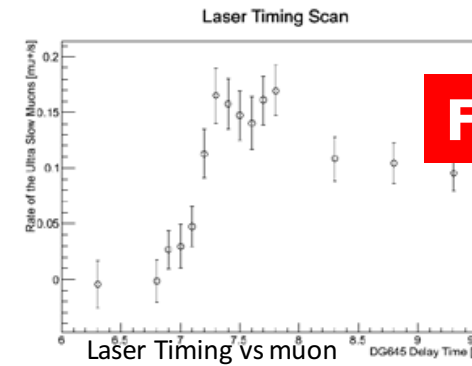
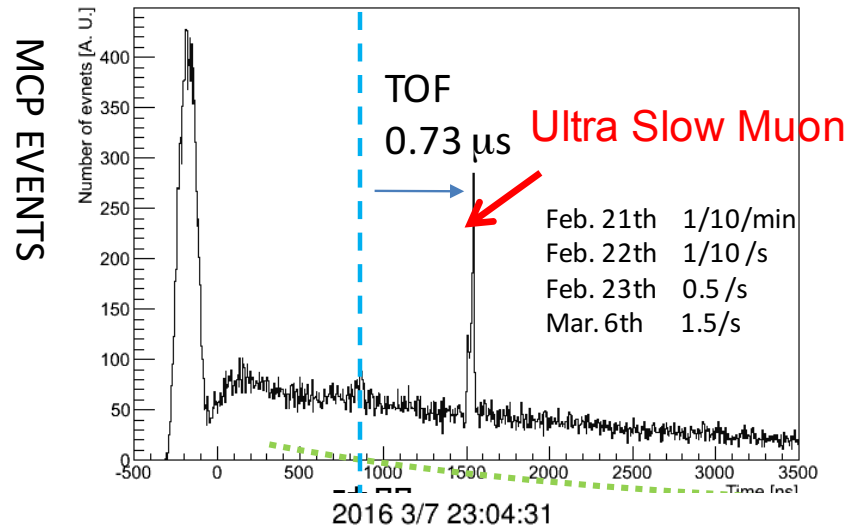


Observation of Ultra Slow Muons @U-Line

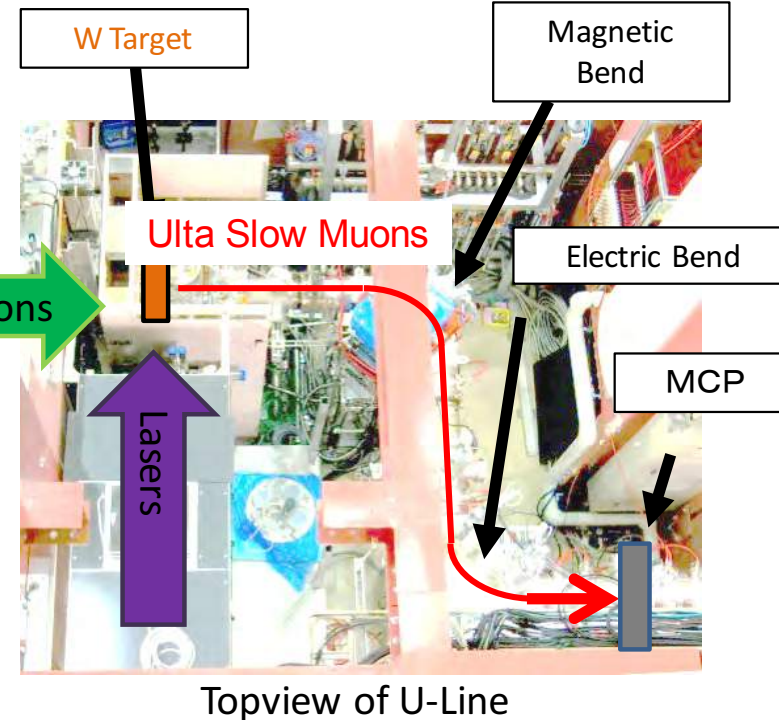
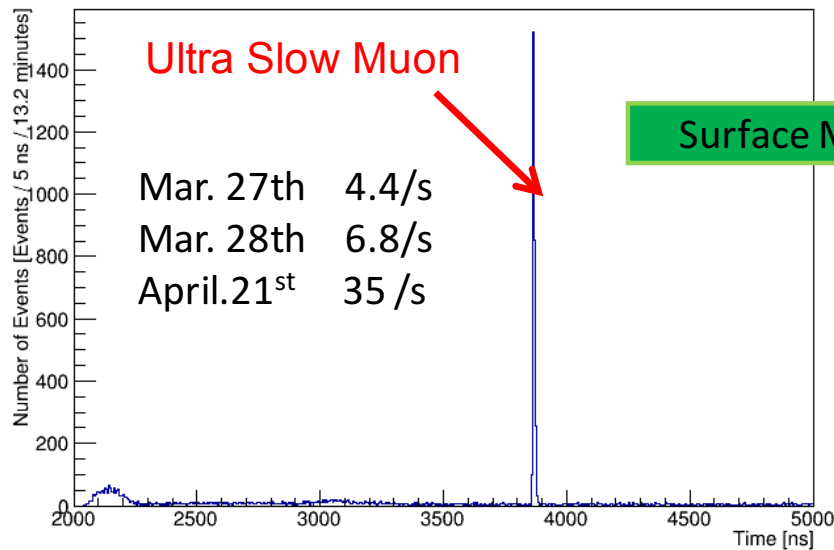
ULTRASLOW
MUON
MICROSCOPE

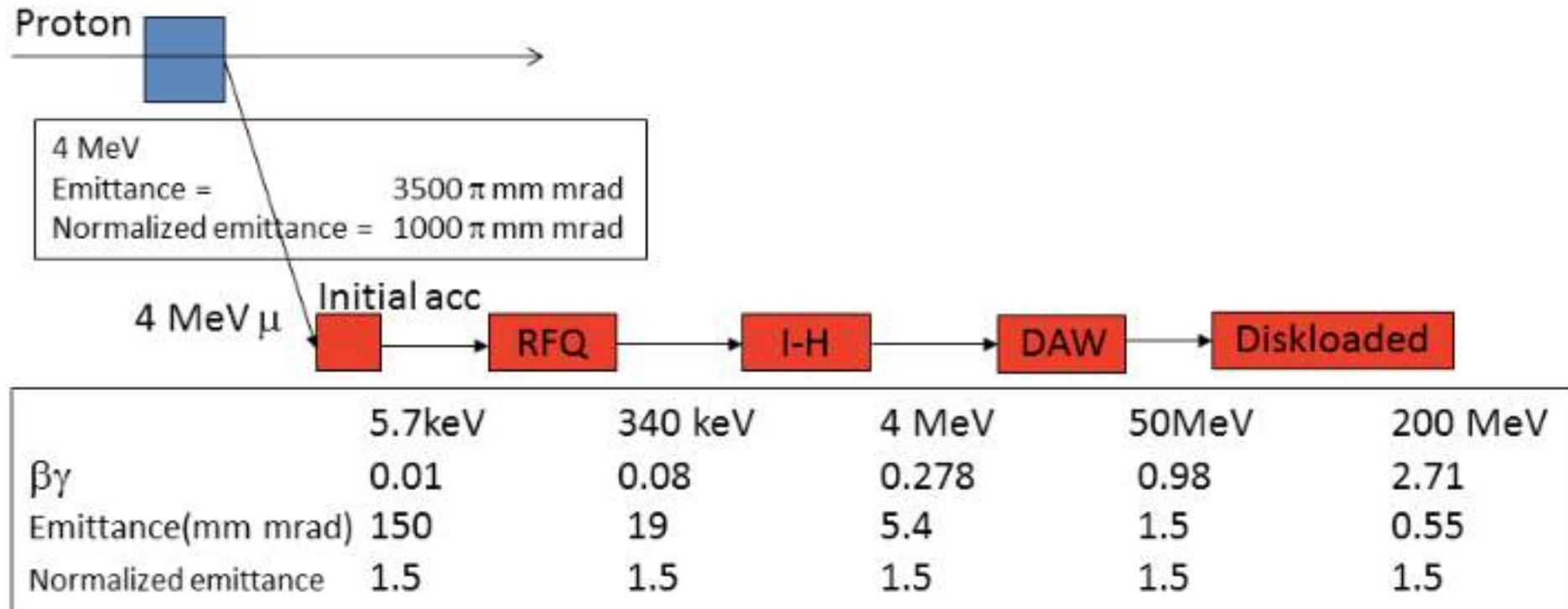


Events of the MCP



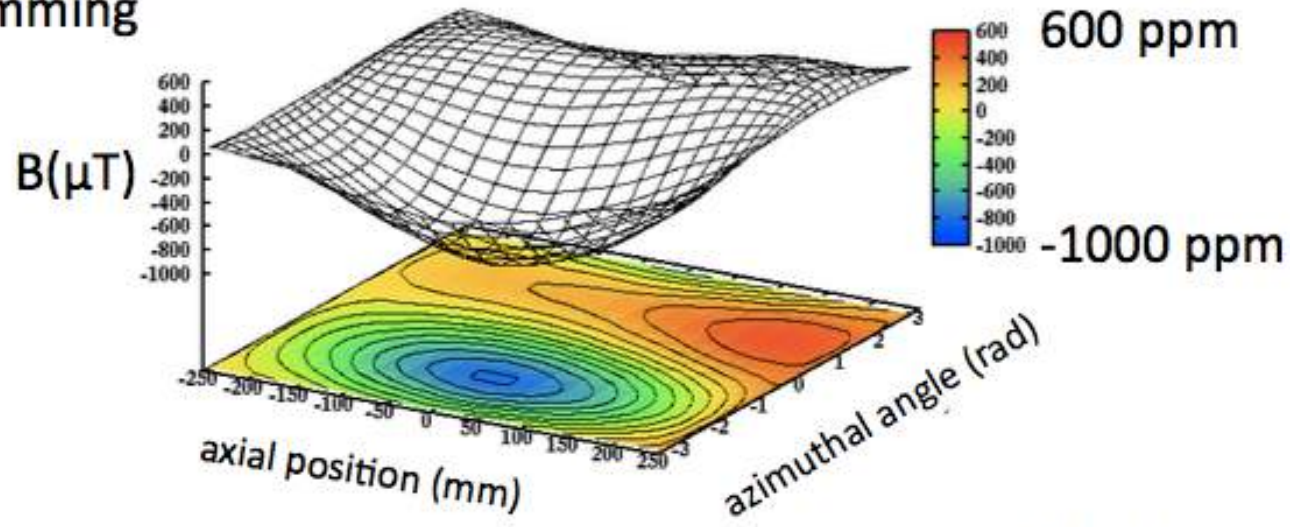
Feb 2016



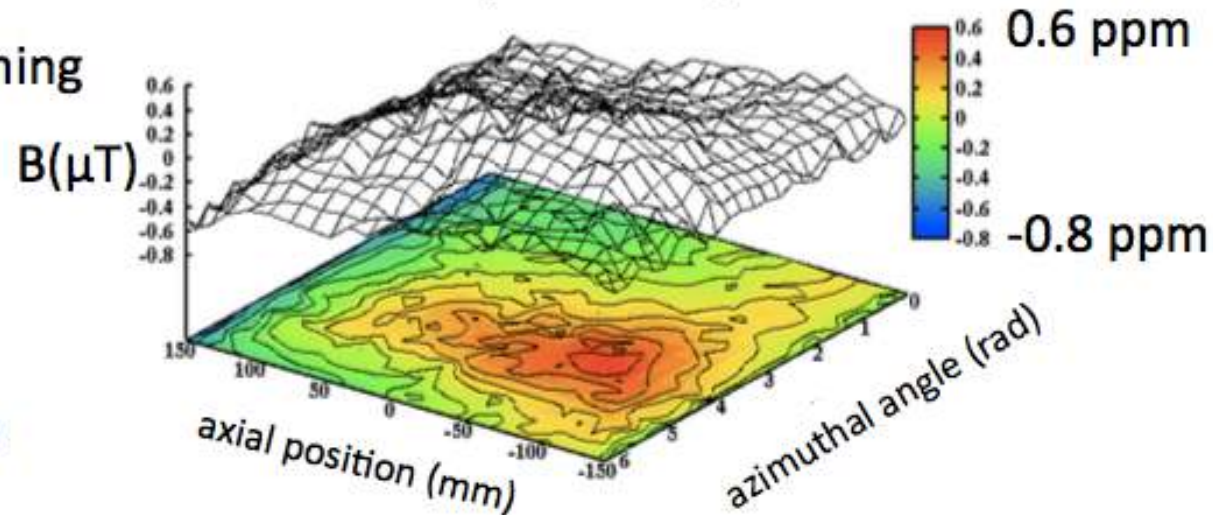


Tests of 1st two acceleration stages completed.

Before shimming



After shimming



$r = 140 \text{ mm}$

30

R&D phase being completed in next year

Funds for most of construction are secured.

Expect data taking to begin after FNAL g-2 i.e. 2020.

Initial sensitivity at 0.37 ppm (stat) reducing to 0.1 ppm (stat)
i.e. similar to FNAL 0.1 ppm (stat) [0.1 ppm (syst)]

This will provide a crucial measurement with completely different systematic effects compared to the FNAL measurement.

“If you enjoy doing difficult experiments, you can do them, but it is a waste of time and effort because the result is already known” : **Pauli**



"No experiment is so dumb, that it should not be tried" : **Gerlach**

E821 Error	Size [ppm]	Plan for the E989 $g - 2$ Experiment	Goal [ppm]
Absolute field calibrations	0.05	Special 1.45 T calibration magnet with thermal enclosure; additional probes; better electronics	0.035
Trolley probe calibrations	0.09	Absolute cal probes that can calibrate off-central probes; better position accuracy by physical stops and/or optical survey; more frequent calibrations	0.03
Trolley measurements of B_0	0.05	Reduced rail irregularities; reduced position uncertainty by factor of 2; stabilized magnet field during measurements; smaller field gradients	0.03
Fixed probe interpolation	0.07	More frequent trolley runs; more fixed probes; better temperature stability of the magnet	0.03
Muon distribution	0.03	Additional probes at larger radii; improved field uniformity; improved muon tracking	0.01
Time-dependent external B fields	—	Direct measurement of external fields; simulations of impact; active feedback	0.005
Others	0.10	Improved trolley power supply; trolley probes extended to larger radii; reduced temperature effects on trolley; measure kicker field transients	0.05
Total	0.17		0.07

E821 Error	Size [ppm]	Plan for the E989 $g - 2$ Experiment	Goal [ppm]
Gain changes	0.12	Better laser calibration; low-energy threshold; temperature stability; segmentation to lower rates; no hadronic flash	0.02
Lost muons	0.09	Running at higher n -value to reduce losses; less scattering due to material at injection; muons reconstructed by calorimeters; tracking simulation	0.02
Pileup	0.08	Low-energy samples recorded; calorimeter segmentation; Cherenkov; improved analysis techniques; straw trackers cross-calibrate pileup efficiency	0.04
CBO	0.07	Higher n -value; straw trackers determine parameters	0.03
E-Field/Pitch	0.06	Straw trackers reconstruct muon distribution; better collimator alignment; tracking simulation; better kick	0.03
Diff. Decay	0.05 ¹	better kicker; tracking simulation; apply correction	0.02
Total	0.20		0.07