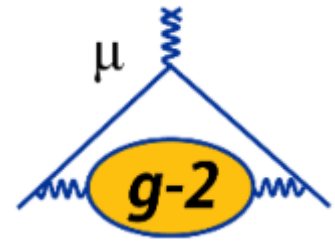




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# The g-2 Experiment at Fermilab



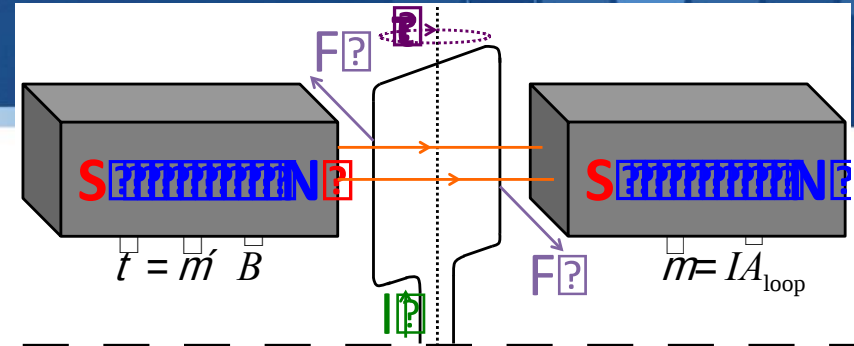
**Barry King. On behalf of the  
Muon g-2 Collaboration.  
August 3rd 2018.**

# Magnetic dipole moments lead to spin precession.



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## Classical Picture



## Quantum Picture

**g-factor:**

$$\vec{\mu} = g \frac{e}{2m_{\mu}c} \vec{S}$$

**Dirac Equation for EM potential:**

$$\hat{e} \hat{g}^m (\nabla_m + ieA_m) - m \psi = 0$$

- Spin-1/2 point particles
- Leads to Pauli Theory
- Predicts  $g = 2$

**Larmor Precession (particle rest frame):**

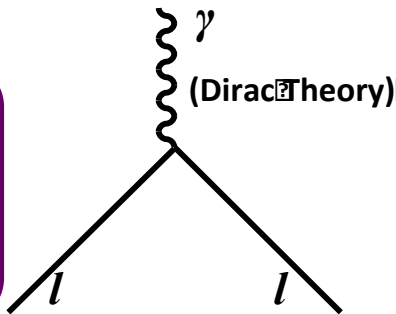
$$\frac{d\vec{S}}{dt} = \vec{\tau} = g \left( \frac{q}{2m} \right) \vec{S} \times \vec{B}$$

## Quantum Field Theory Picture

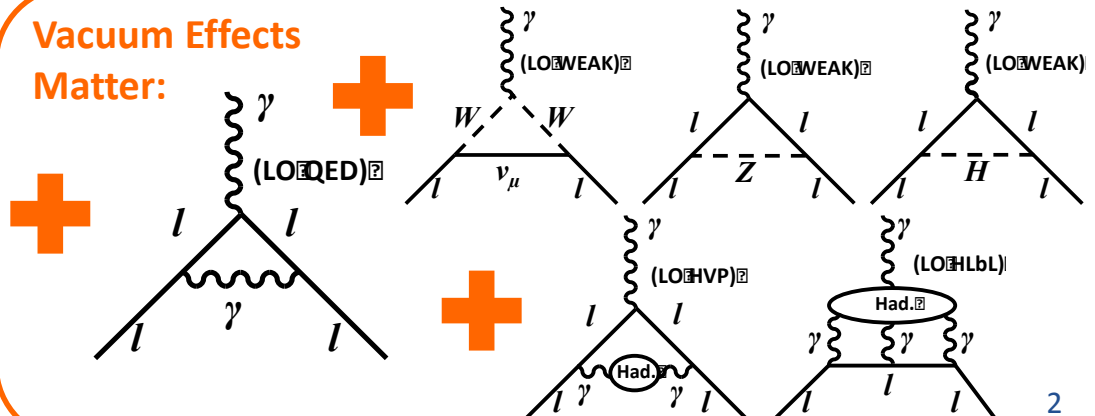
**Anomaly:**

$$a_0 \frac{g-2}{2}$$

- Predicts  $g \neq 2$



**Vacuum Effects**  
**Matter:**

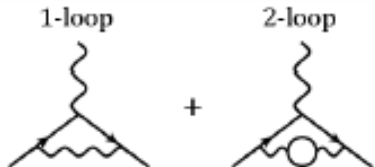
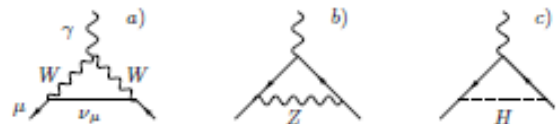
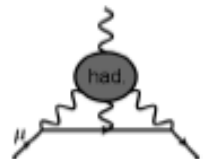
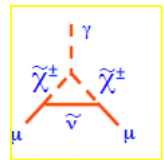


# Standard Model Prediction.

Sensitivity of muons to new physics is  $\sim \frac{m_\mu^2}{m_e^2} \sim 40,000$  greater than electrons.

The Standard Model determination of  $a_\mu$

$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{had, VP}} + a_\mu^{\text{had, LbL}} + a_\mu^{\text{BSM??}}$$

|      |                                                                                     |                                                  |                                                                            |
|------|-------------------------------------------------------------------------------------|--------------------------------------------------|----------------------------------------------------------------------------|
| QED  |    | Known to <b>five-loop</b><br>(12,672 diagrams)   | 99.99% of $a_\mu^{\text{SM}}$ $\sim 0.001\%$ of $\delta a_\mu^{\text{SM}}$ |
| EW   |    | Known to <b>two-loop</b><br>(with $m_H$ known)   | 0.0001% of $a_\mu^{\text{SM}}$ $\sim 0.2\%$ of $\delta a_\mu^{\text{SM}}$  |
| HVP  |   | Non-perturbative<br>(data input + lattice)       | 0.006% of $a_\mu^{\text{SM}}$ $\sim 47\%$ of $\delta a_\mu^{\text{SM}}$    |
| HLbL |  | Non-perturbative<br>(data input + model/lattice) | 0.0001% of $a_\mu^{\text{SM}}$ $\sim 53\%$ of $\delta a_\mu^{\text{SM}}$   |
| BSM  |  | ???????                                          |                                                                            |

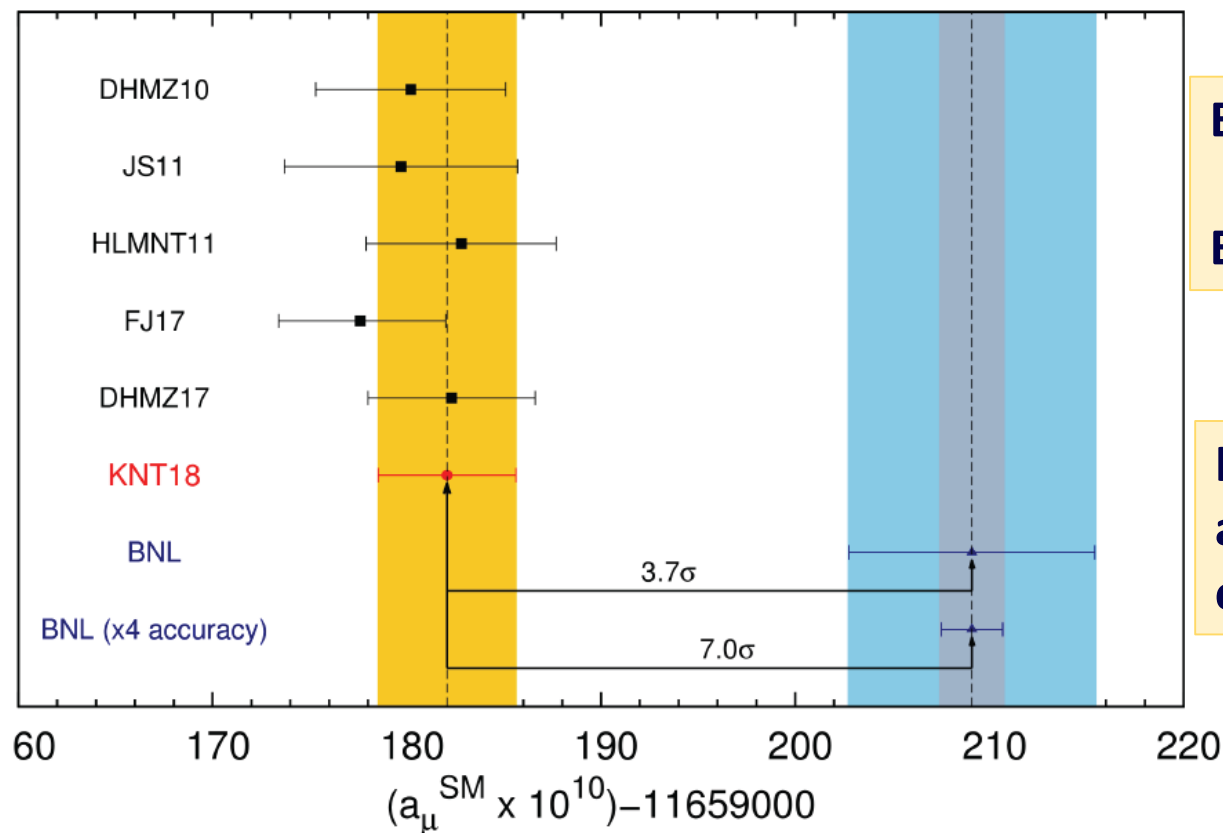


$$a_{\mu}^{\text{SM}} = 11\,659\,182.05 (3.56) \times 10^{-10} \text{ (Theory Total)}$$

$$a_{\mu}^{\text{EX}} = 11\,659\,208.9 (6.3) \times 10^{-10} \text{ (World Average)}$$

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = 26.85 (7.26) \times 10^{-10} > 3\sigma \text{ discrepancy}$$

The discrepancy between the latest SM prediction and the result from the Brookhaven experiment (E821) is greater than  $3\sigma$



E821 error: 540 ppb.

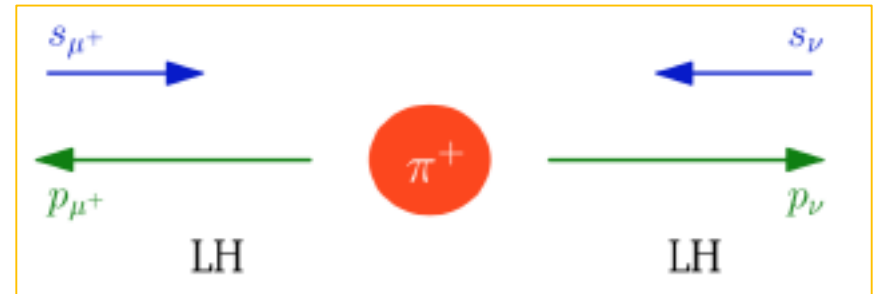
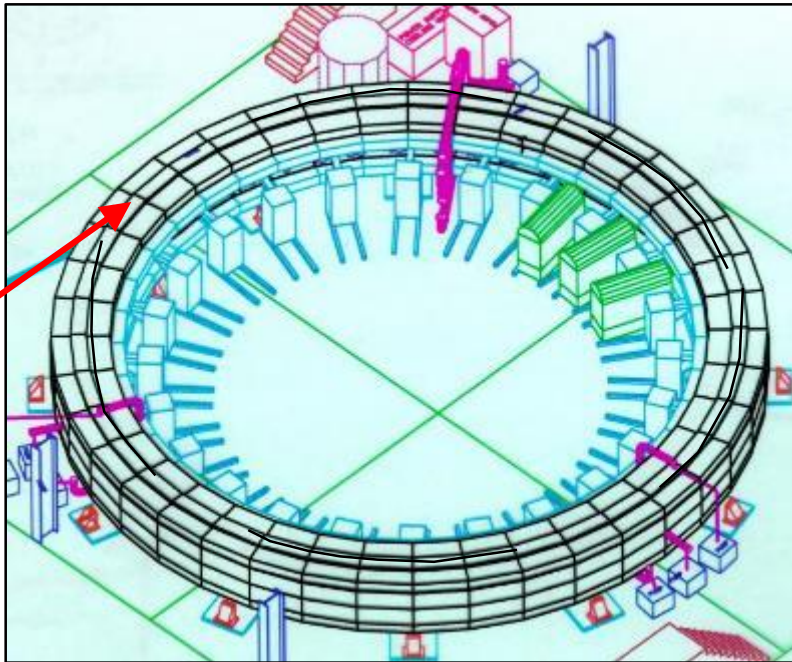
E989 goal: 140 ppb.

If central value persists,  
achieving the Fermilab design  
error will give  $\sim 7\sigma$  difference.



# Muon Spin Dynamics in a Storage Ring.

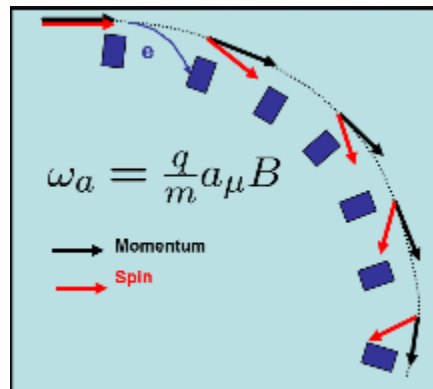
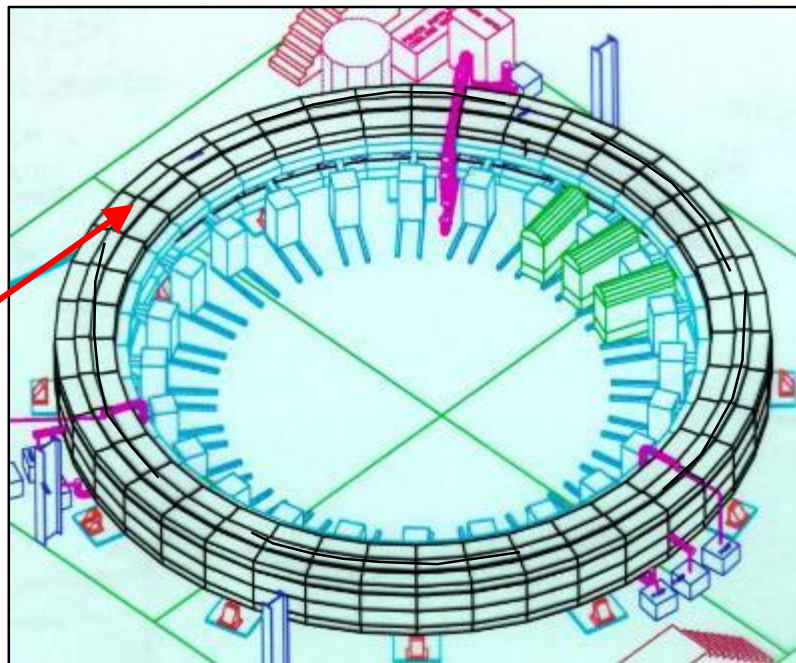
## 1) Inject polarized muon source

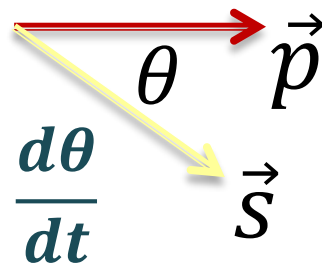


The muons circulate with an angular frequency:

$$\omega_c = \frac{eB}{\gamma m}$$

# Muon Spin Dynamics in a Storage Ring.





$$\omega_a = \frac{d\theta}{dt}$$

Muon spin precesses in the vertical external magnetic field of  $B = 1.45$  Tesla (Lamor Precession).

$$\omega_s = \frac{geB}{2m} + (1 - \gamma) \frac{eB}{\gamma m}$$

$$\omega_a = \omega_s - \omega_c = \left( \frac{g}{2} - 1 \right) \frac{eB}{m} = a_\mu \frac{eB}{m}$$

Measure two quantities in g-2

Muon spin precession relative to momentum in cyclotron is directly proportional to  $a_\mu$



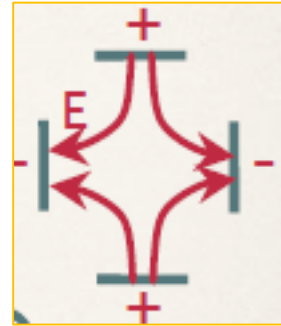
# Muon Spin Dynamics in a Storage Ring.

We would like to use electrostatic quadrupoles for vertical focussing of the muon beam.

This introduces an extra term into the formula for  $\omega_a$

$$\omega_a = \frac{e}{m} \left\{ a_\mu B - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\beta \times E}{c} \right\}$$

$\swarrow$   
 $\sim 0$

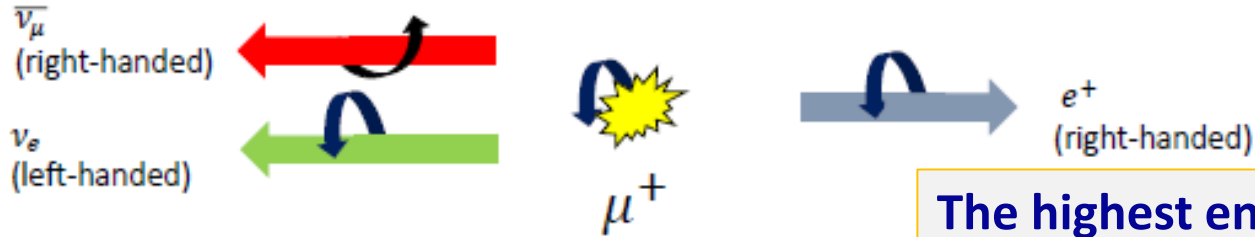


Use muons of **specific momentum** such  $\gamma = \gamma_{magic} = \sqrt{1 + \frac{1}{a_\mu}} = 29.3$

Muon momentum = 3.094 GeV.  
Lifetime dilated to  $\sim 64.4 \mu\text{secs}$ .



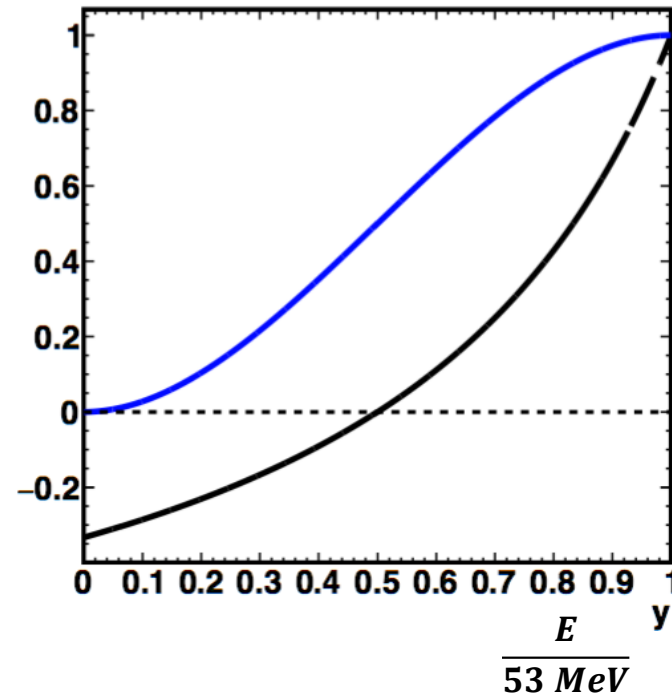
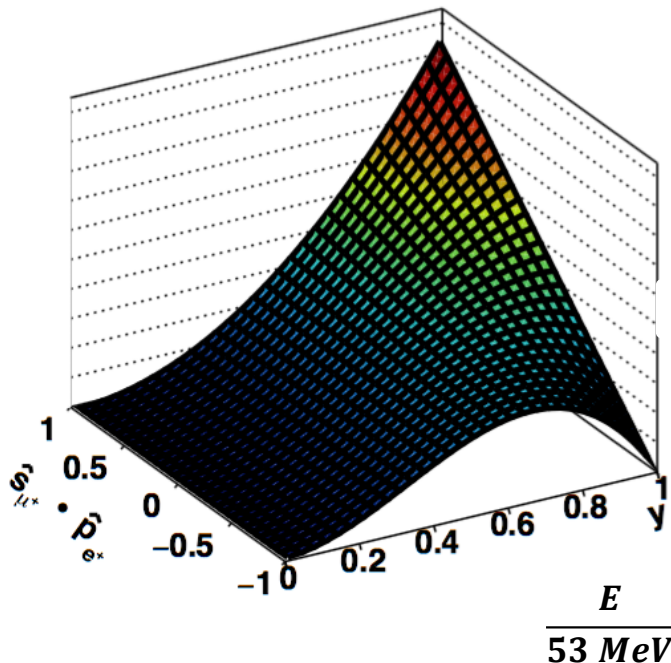
# Decay positron distribution in the muon rest frame



The highest energy positrons  
are emitted in the direction of  
the muon spin.

$N(E)$   
 $A(E)$

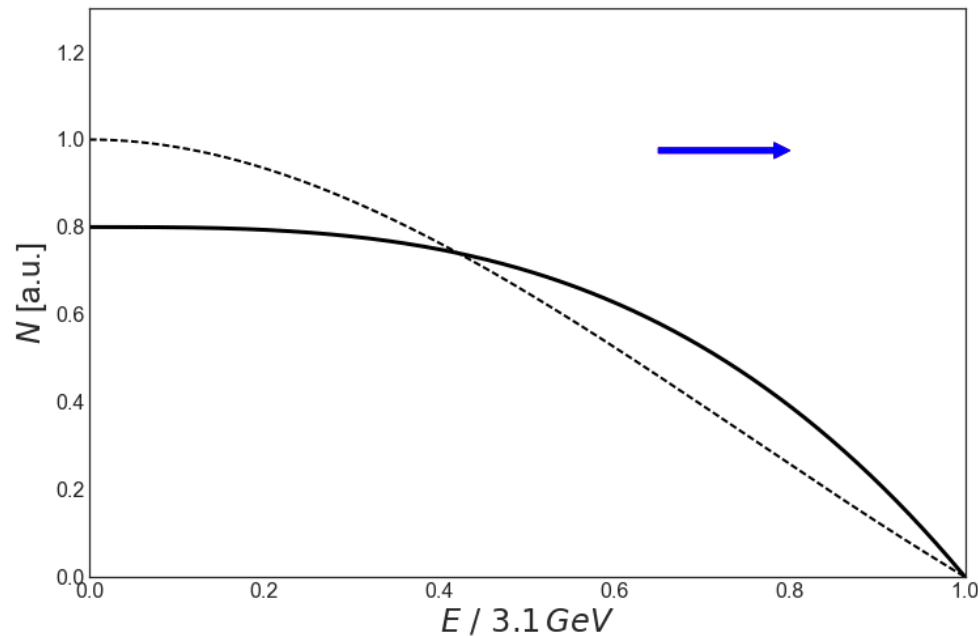
$$\frac{d^2 N}{dE d \cos(\theta)} \propto N(E)[1 + A(E) \cos(\theta)]$$





# Decay positron distribution in the lab frame

As the spin vector rotates relative to the momentum vector the decay positron energy distribution alters:



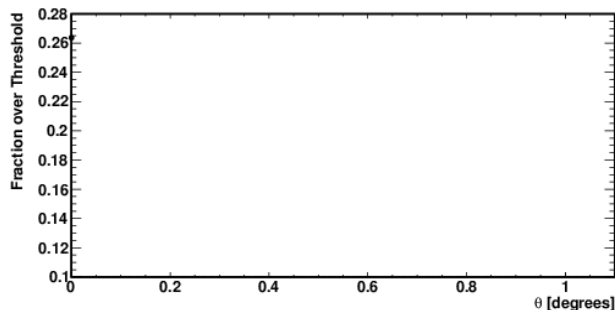
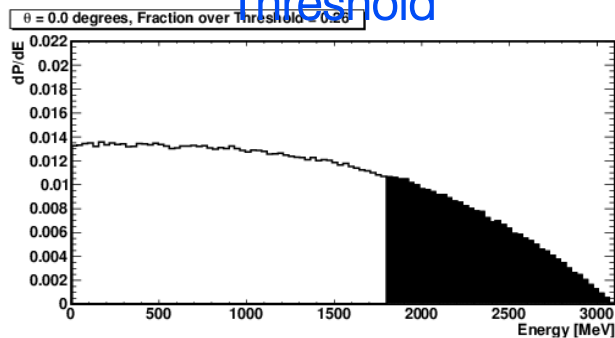
Can use the observed number of decay positrons above some energy threshold to measure  $\omega_a$ :



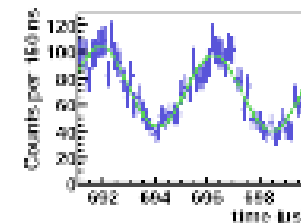
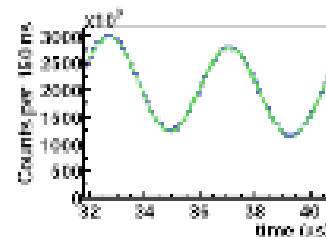
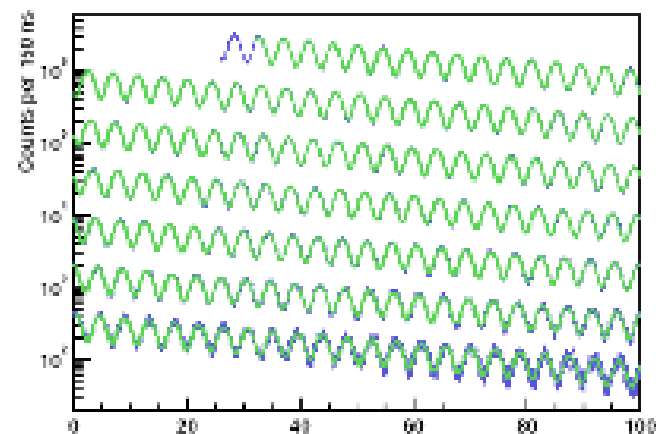
# Spin Precession in g-2 Ring

- Higher energy positrons emitted preferentially in direction of muon spin
- Threshold Energy Cut in calorimeters
- Results in sinusoidally oscillating energy deposition

Fraction of  $e^+$   
above  
Threshold



Result from E821  
Brookhaven experiment.





# What g-2 actually measures.

It is possible to rearrange  $a_\mu = \frac{\omega_a m_\mu}{eB}$  in terms of precisely known ratios:

The g-2 experiment then measures  $\omega_a$   
and  $\omega_p$  (measure the magnetic field via precession of free protons)

$$a_m = \frac{\frac{g_e}{2} \frac{m_m}{m_e} \frac{W_a}{\langle W_p \rangle}}{\frac{m_e}{m_p}}$$

The diagram shows the equation for  $a_m$  with various terms enclosed in colored boxes:  $g_e$  in a blue box,  $m_m$  in an orange box,  $W_a$  in a yellow box,  $m_e$  in an orange box,  $\langle W_p \rangle$  in a yellow box,  $m_e$  in a green box, and  $m_p$  in a green box. A purple arrow points from the text 'Average magnetic field seen by muons measured with NMR' to the  $\langle W_p \rangle$  term in the denominator.

Average magnetic  
field seen by muons  
measured with NMR

$$\hbar\omega_p = 2\mu_p |\vec{B}|$$

$$g_e = -2.002\,319\,304\,361\,82(52) \text{ (0.00026 ppb)}$$

$$m_\mu/m_e = 206.768\,2826(46) \text{ (22 ppb)}$$

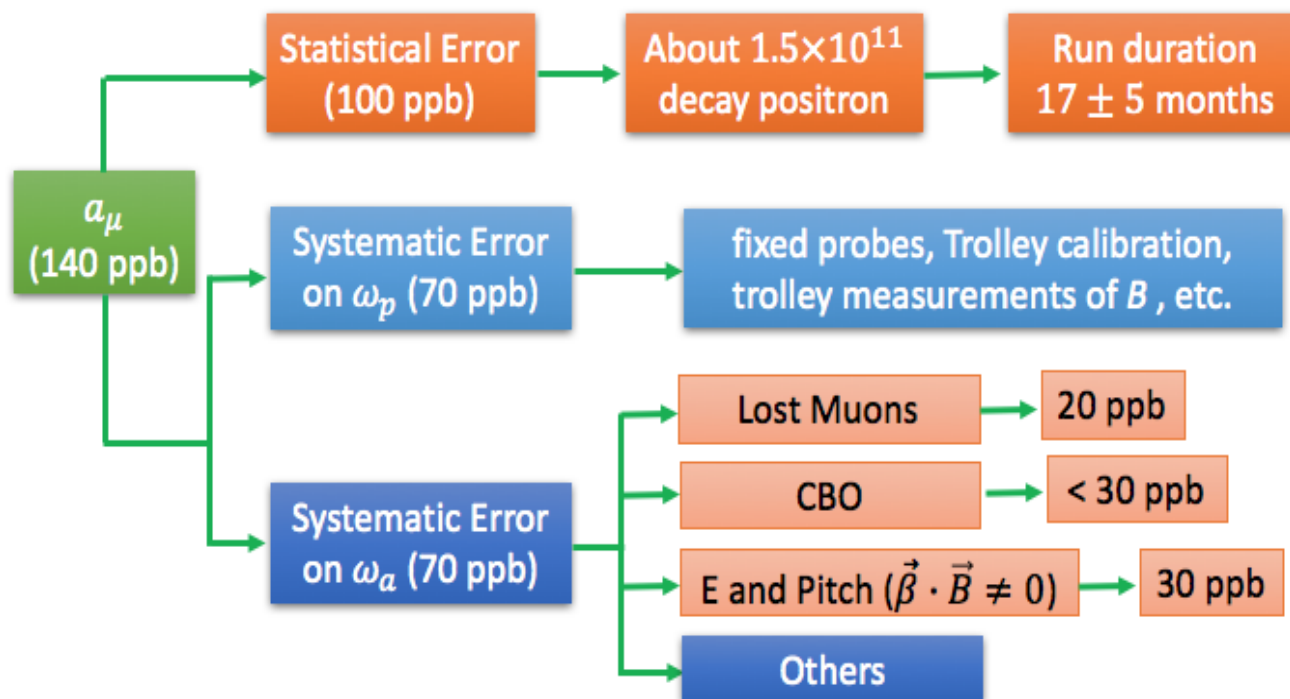
$$\mu_e/\mu_p = -658.210\,6866(20) \text{ (3.0 ppb)}$$

Fermilab Experiment  $a_\mu$  total error goal is 140 ppb



# How to obtain a more precise measurement.

- Increase statistics by a factor of  $> 20$  and reduce systematics by a factor of  $\sim 3$  w.r.t BNL experiment



More beam !!!

Better Uniform  
Magnetic Field!!!

Better  
 $\omega_a$  measurement !!!

# Systematics on $\omega_a$

The goal of the Fermilab experiment is to **reduce the systematic error on  $\omega_a$  180  $\rightarrow$  70 ppb**

- Improved Calorimeters
- New Laser control system
- New Tracker to give accurate beam profile and position.

| Category      | E821<br>[ppb] | E989 Improvement Plans                                  | Goal<br>[ppb] | <u>Key element:</u> |                        |
|---------------|---------------|---------------------------------------------------------|---------------|---------------------|------------------------|
| Gain changes  | 120           | Better laser calibration<br>low-energy threshold        | 20            | Laser               | Largest<br>improvement |
| Pileup        | 80            | Low-energy samples recorded<br>calorimeter segmentation | 40            | Calo + Laser        |                        |
| Lost muons    | 90            | Better collimation in ring                              | 20            | Calo + Laser        |                        |
| CBO           | 70            | Higher $n$ value (frequency)                            | < 30          | Inflector + Kicker  |                        |
|               |               | Better match of beamline to ring                        |               |                     |                        |
| $E$ and pitch | 50            | Improved tracker                                        | 30            | Tracker             |                        |
|               |               | Precise storage ring simulations                        |               |                     |                        |
| Total         | 180           | Quadrature sum                                          | 70            |                     |                        |

# Systematics on $\omega_p$

| Category                                | E821<br>[ppb] | Main E989 Improvement Plans                                                                                                                               | Goal<br>[ppb] |
|-----------------------------------------|---------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------|---------------|
| Absolute field calibration              | 50            | Special 1.45 T calibration magnet with thermal enclosure; additional probes; better electronics                                                           | 35            |
| Trolley probe calibrations              | 90            | Plunging probes that can cross calibrate off-central probes; better position accuracy by physical stops and/or optical survey; more frequent calibrations | 30            |
| Trolley measurements of $B_0$           | 50            | Reduced position uncertainty by factor of 2; improved rail irregularities; stabilized magnet field during measurements*                                   | 30            |
| Fixed probe interpolation               | 70            | Better temperature stability of the magnet; more frequent trolley runs                                                                                    | 30            |
| Muon distribution                       | 30            | Additional probes at larger radii; improved field uniformity; improved muon tracking                                                                      | 10            |
| Time-dependent external magnetic fields | –             | Direct measurement of external fields; simulations of impact; active feedback                                                                             | 5             |
| Others †                                | 100           | Improved trolley power supply; trolley probes extended to larger radii; reduced temperature effects on trolley; measure kicker field transients           | 30            |
| Total systematic error on $\omega_p$    | 170           |                                                                                                                                                           | 70            |

# How to obtain a more precise measurement: Summary.

## Systematic Uncertainties: Improvements Over E821

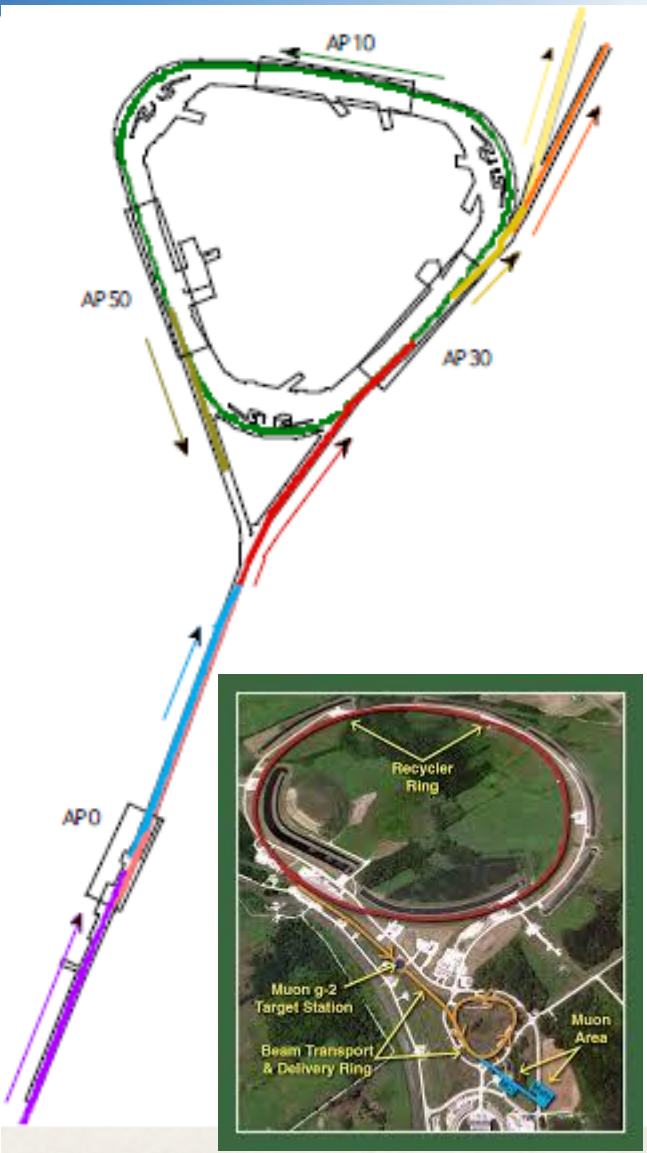
Reduce  $\omega_a$  systematic uncertainties by a factor of 3

| E821 Error                     | Size (ppb) | E989 Improvements                                                                        | Goal (ppb) |
|--------------------------------|------------|------------------------------------------------------------------------------------------|------------|
| Gain Changes                   | 120        | Better laser calibration; low-energy threshold, temperature stability, no hadronic flash | 35         |
| Lost Muons                     | 90         | Less scattering due to material at injection; muons reconstructed by calorimeters        | 30         |
| Pileup                         | 80         | Low-E samples recorded; calo segmentation; trackers cross-calibrate pileup efficiencies  | 30         |
| Coherent Betatron Oscillations | 70         | Higher n-value, straw trackers to determine parameters                                   | 10         |
| E-field/pitch                  | 60         | Straw trackers to reconstruct muon distribution, better collimators, better kick         | 30         |
| Diff. Decay                    | 50         | Better kicker, tracking simulation                                                       | 20         |
| <b>Total</b>                   | <b>200</b> |                                                                                          | <b>70</b>  |

Reduce  $\omega_p$  systematic uncertainties by a factor of 2.5

| E821 Error                | Size (ppb) | E989 Improvements                                                       | Goal (ppb) |
|---------------------------|------------|-------------------------------------------------------------------------|------------|
| Field Calibration         | 50         | Dedicated test solenoid, more probes, better electronics                | 35         |
| Trolley Measurements      | 50         | Reduced rail irregularities, field gradients                            | 30         |
| Fixed Probe Interpolation | 70         | More trolley runs, fixed probes; better temperature stability of magnet | 30         |
| Muon Convolution          | 30         | Improved field uniformity, muon tracking                                | 10         |
| Time-Dependent Fields     | –          | Direct measurements of external fields, active feedback                 | 5          |
| Others                    | 100        | Improved electronics, reduced temperature dependence, kicker transients | 50         |
| <b>Total</b>              | <b>170</b> |                                                                         | <b>70</b>  |

# Why Fermilab?



Fermilab is able to produce many more muons than Brookhaven

- ~ 20 times more statistics in the experiment.

Fermilab produces “better” muons

- much less pion contamination.

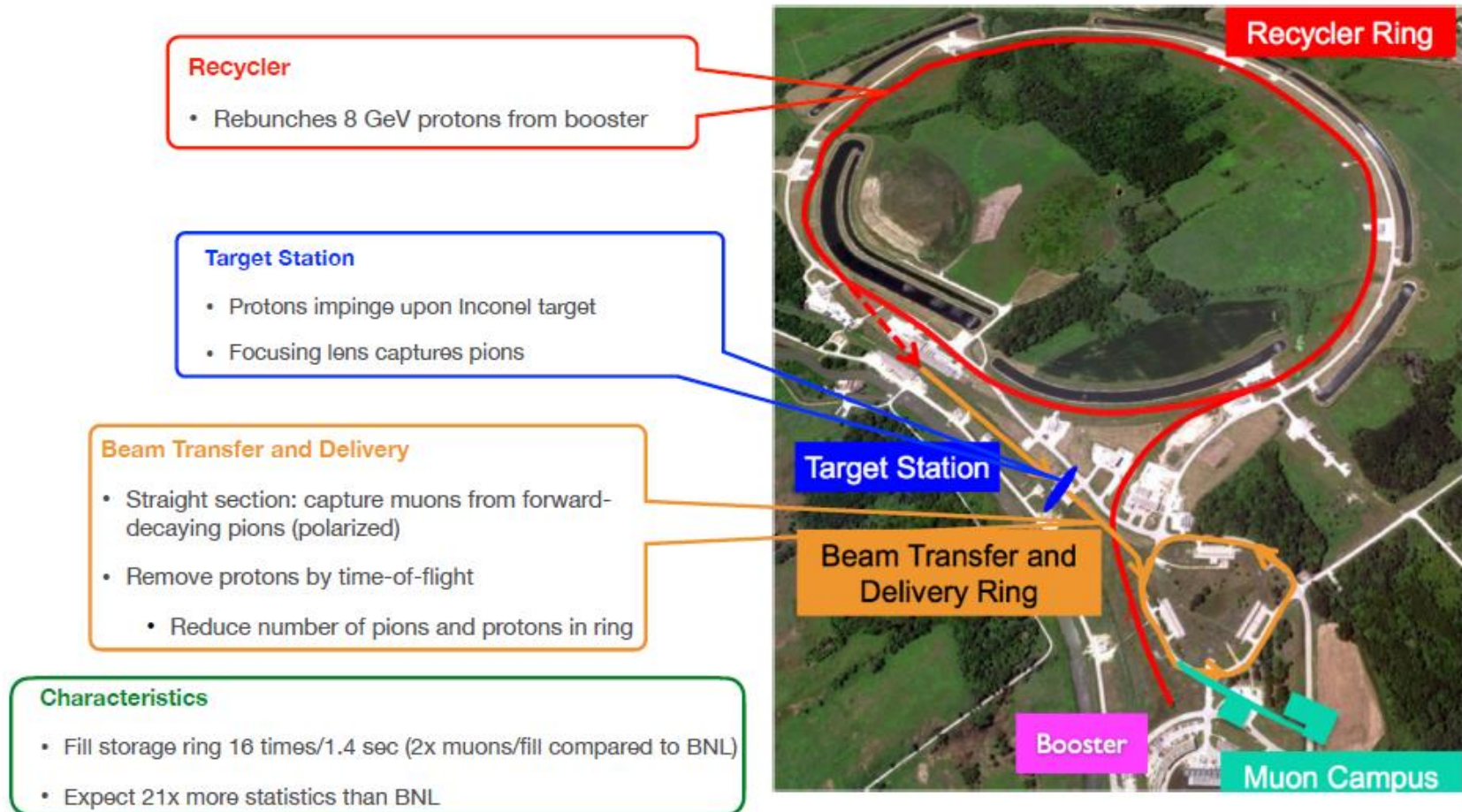
Coupled with improvements in the experiment design:

- will measure  $a_\mu$  to 0.14 ppm.

If the discrepancy persists should provide an  $\sim 7\sigma$  disagreement with the Standard Model.

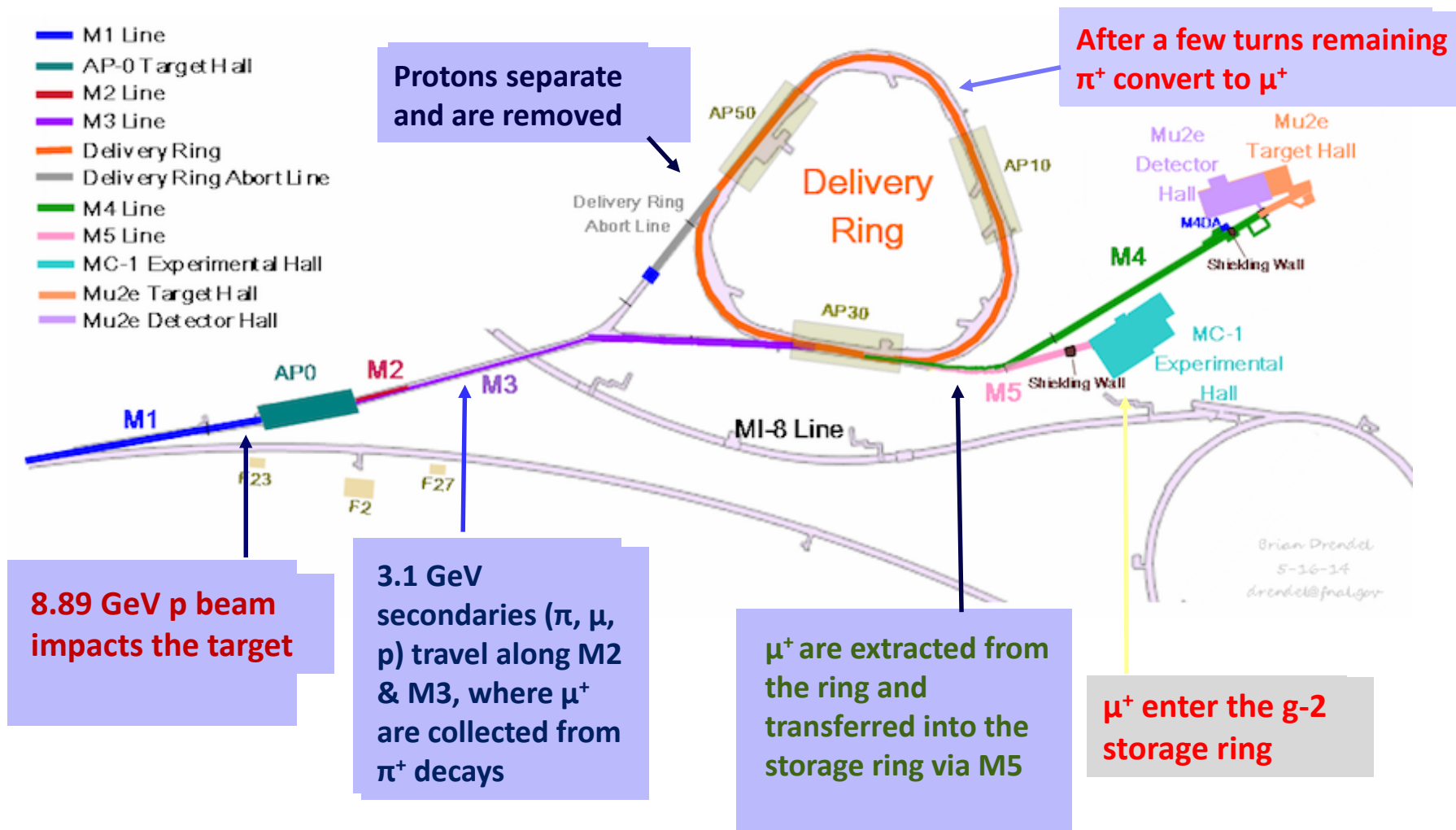


## Muon Beam: From Protons to Muons





# Fermilab beamline decays away most of the pions.





**μ enter storage ring  
(220 muons/fill achieved)**



# Fermilab Muon g-2 Collaboration ...



## US Universities

- Boston
- Cornell
- Illinois
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- Northern Illinois
- Regis
- Texas
- Virginia
- Washington

## National Labs

- Argonne
- Brookhaven
- Fermilab



## Italy

- INFN
  - LNF Frascati,
  - Naples
  - Pisa
  - Roma 2
  - Trieste
  - Lecce
- Udine
- Naples
- Trieste
- Rijeka
- Molise
- SNS Pisa



## England

Cockcroft Institute  
Lancaster  
Liverpool  
University College London



## Korea

KAIST  
CAPP



## Russia

Dubna  
Novosibirsk



## China

- Shanghai



## The Netherlands

- Groningen



## Germany

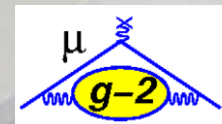
- Dresden (thy)



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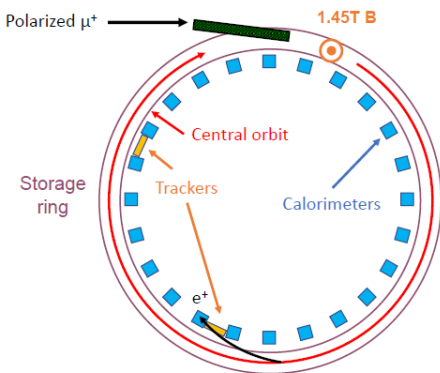
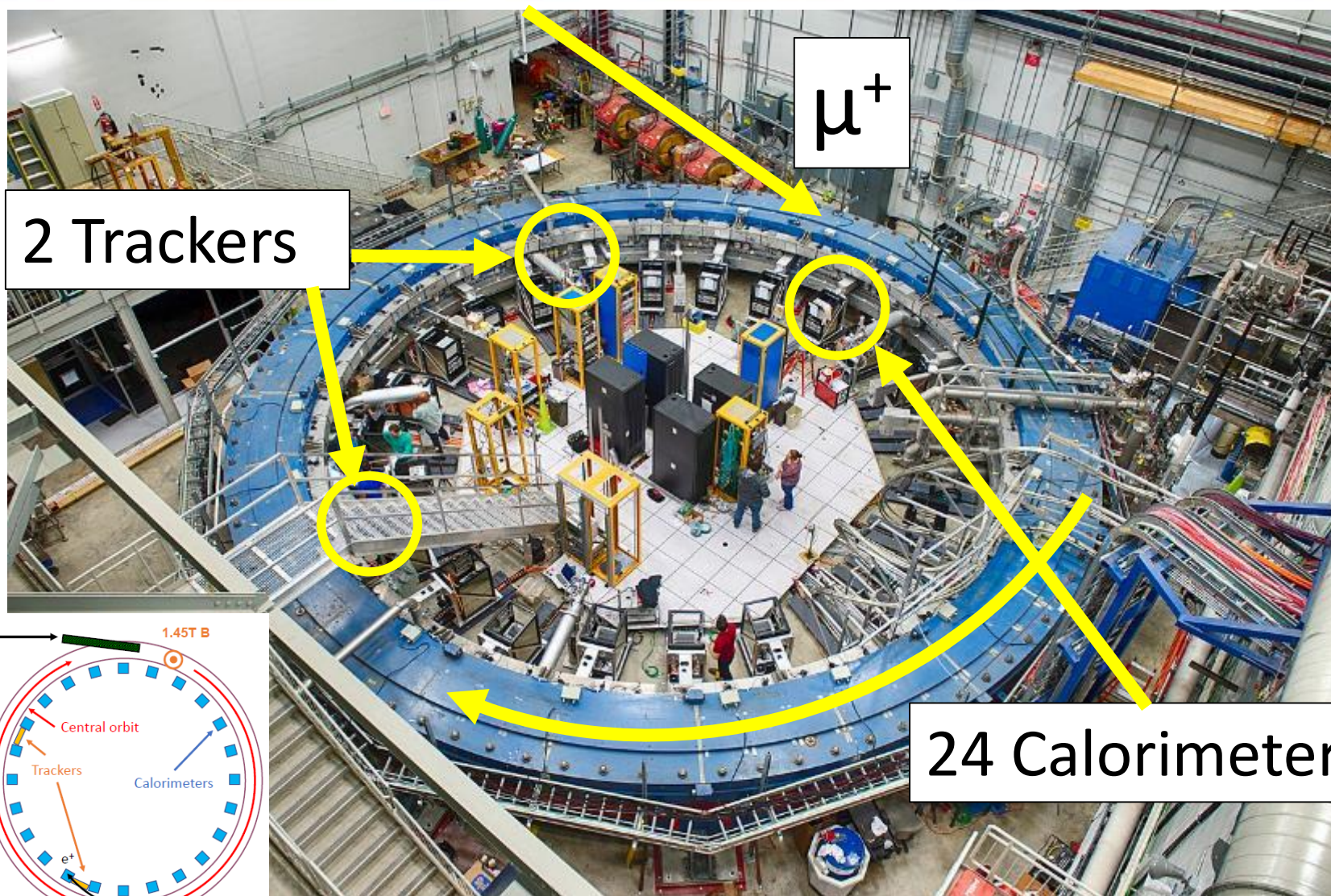
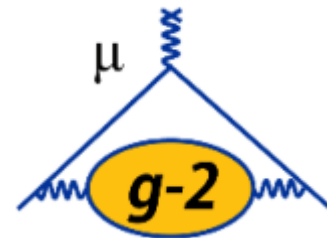
Fermilab





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# E989: The Fermilab g-2 Experiment.

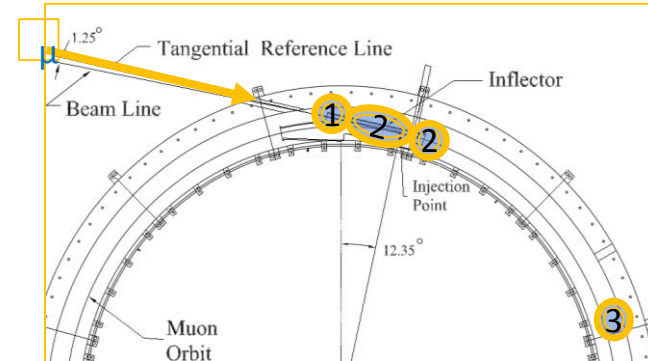
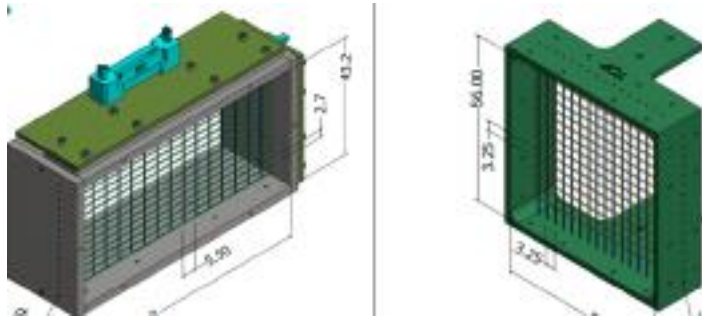


# IBMS: Beam monitors on entry to g-2 ring.



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Just upstream of the inflector:



3

3

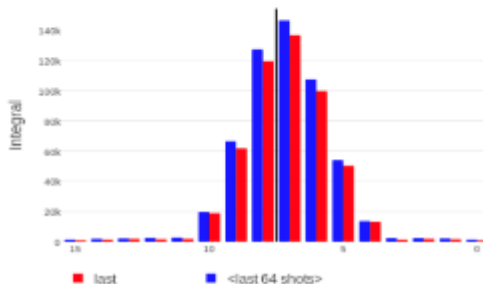


IBMS 1 BEAM PROFILE

RMS 1.2

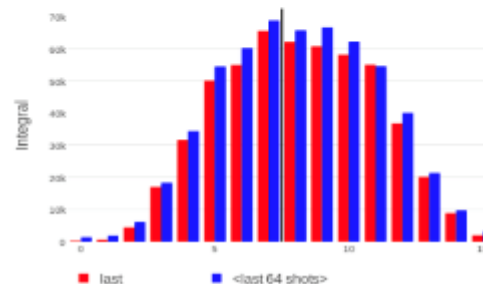
MEAN: 7.1 fiber, SIGMA: 1.6 fiber  
MEAN: -1.0 mm, SIGMA: 4.4 mm

Y Profile (0 up)



MEAN: 8.2 fiber, SIGMA: 2.8 fiber  
MEAN: 3.7 mm, SIGMA: 15.4 mm

X Profile (0 radially out)



Scintillators provide  
map of temporal and  
transverse beam  
profile.  
Gives guidance on  
muon beam tuning.

Beam X, Y profiles at Inflector Beam Profile Monitor 1

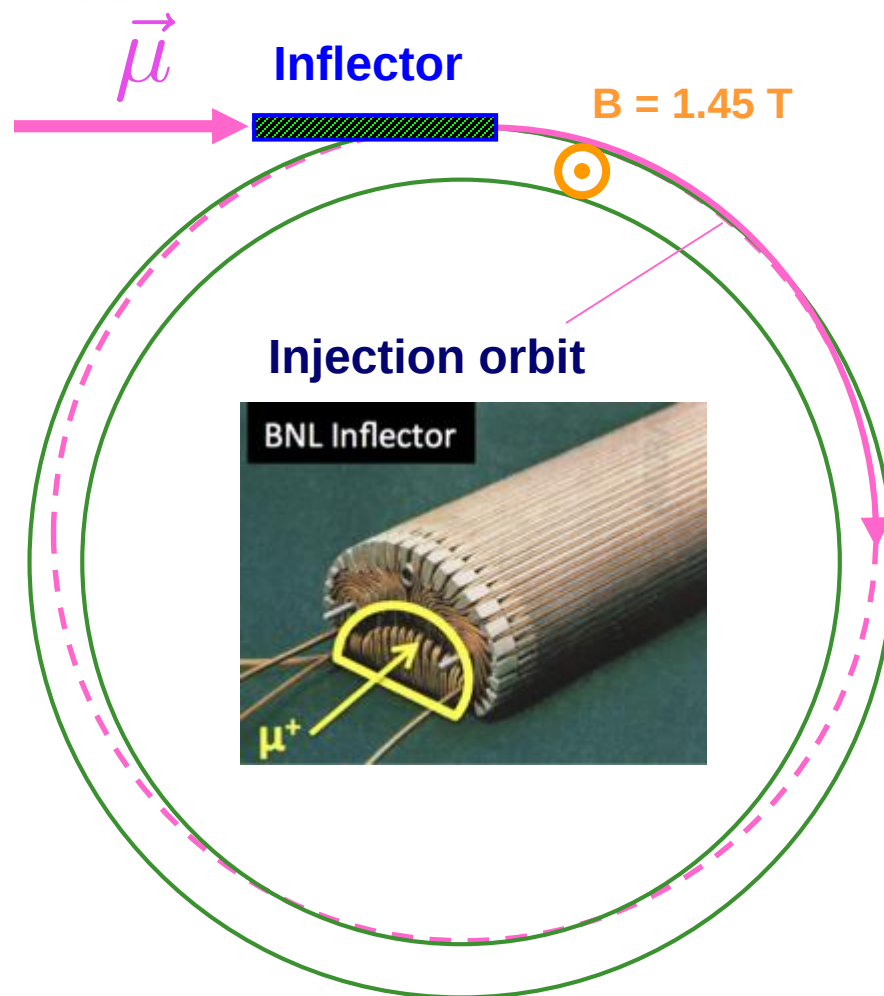
# Inflector.



$$\begin{aligned} B &= 1.45 \text{ Tesla} \\ R &= 7.112 \text{ m} \\ \tau_c &= 149 \text{ ns} \\ \gamma\tau &= 64.4 \mu\text{s} \\ \tau_a &= 4.37 \mu\text{s} \end{aligned}$$

- M5 magnetic quads do final focusing before injection into ring
- Inflector injects muons into ring while minimizing disturbance to B-field

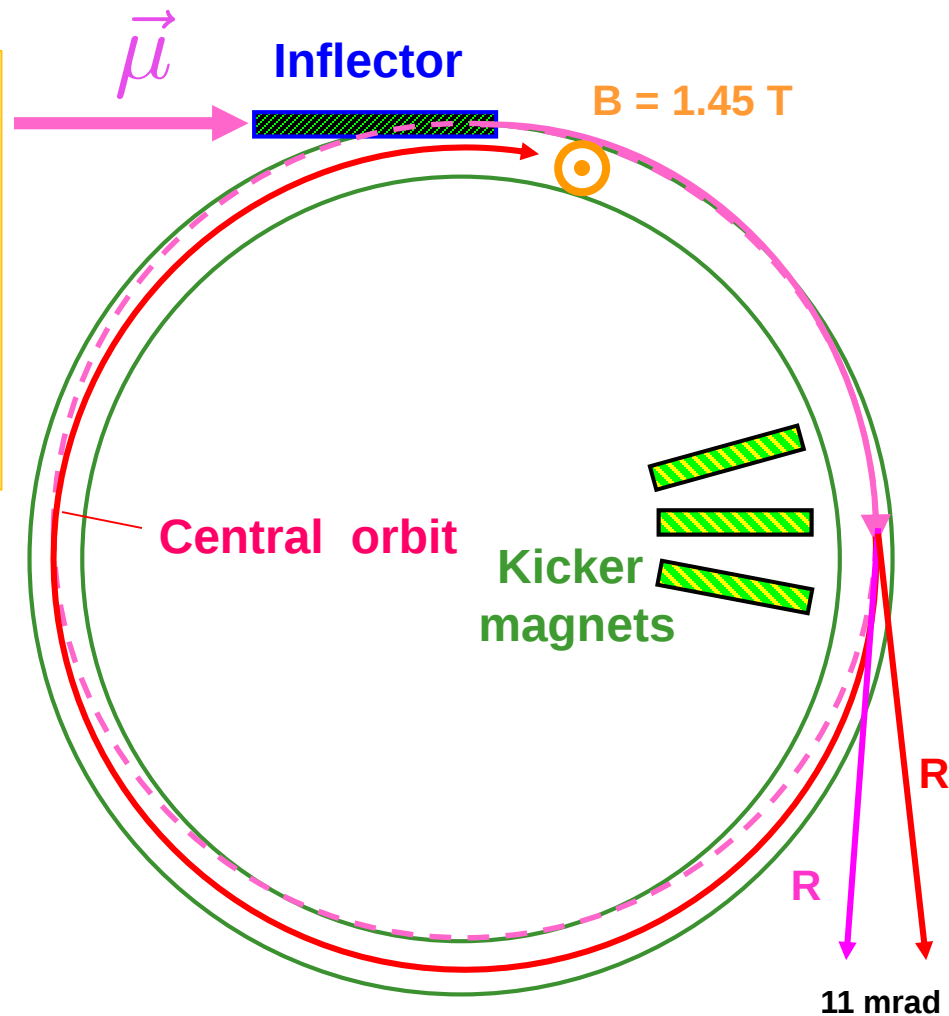
Provides nearly field free region for muons to enter the ring.  
Muons exiting the inflector take a circle 77mm outward than needed for storage.



# Kickers.

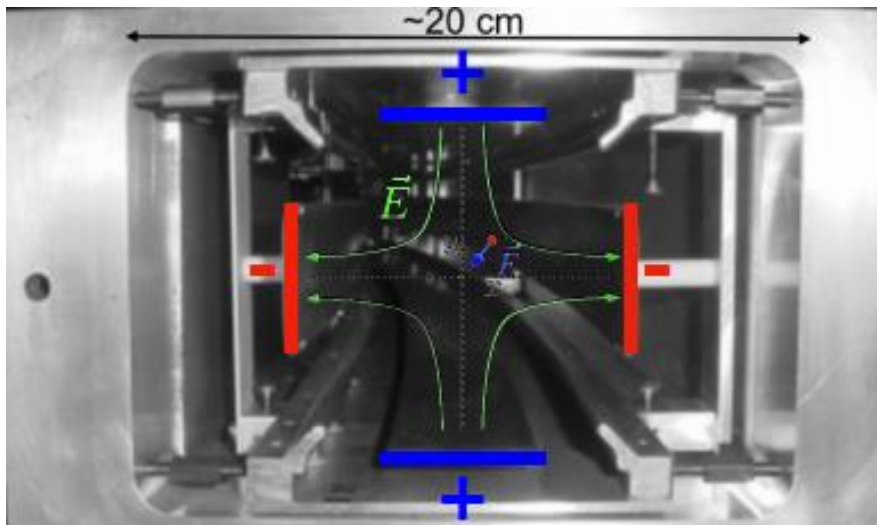
New 1.7m long, 3 kicker magnets are used to kick the muons back into ideal orbit. Kickers give a 11 mrad bend to the muon beam

The kicker pulse has to be shorter than the cyclotron frequency, which is  $\sim 149\text{ns}$

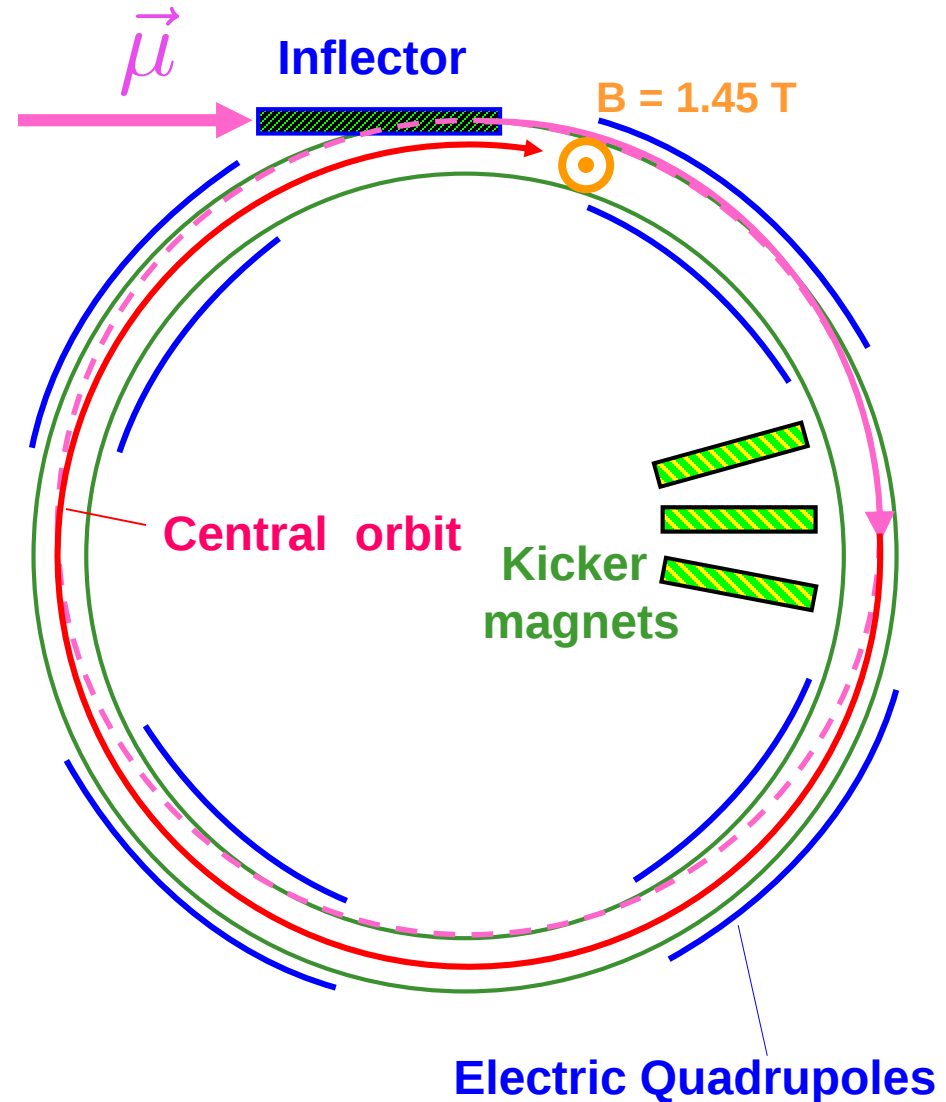


# Quadrupoles.

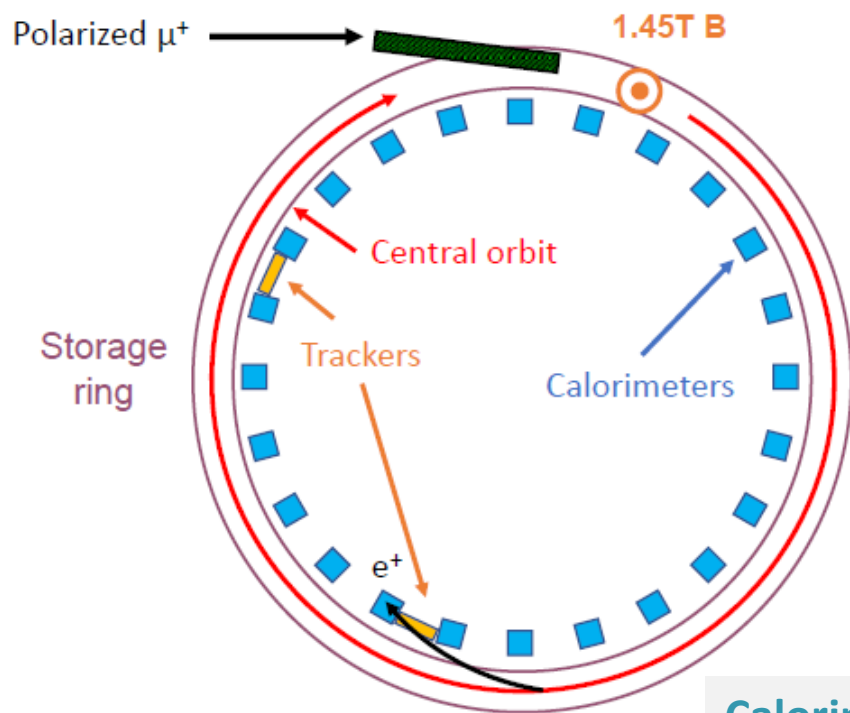
- Muons focused vertically with electrostatic quadrupoles



Quad Plates in Vacuum Chamber



# Calorimeters.



## Calorimeter Improvements:

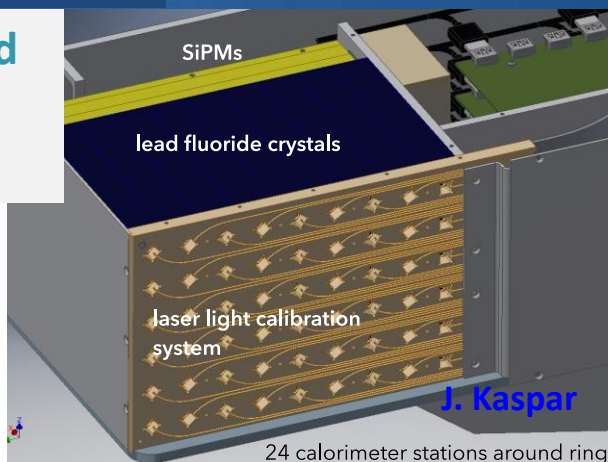
$6 \times 9$  segmented array of  $PbF_2$  crystals (reduces pileup from 2 close low energy positrons).

Laser calibration system to ensure gain stability.

**Better time synchronization with beam injection.**

# Segmented calorimeters provide spatial resolution that can be used to separate positron hits.

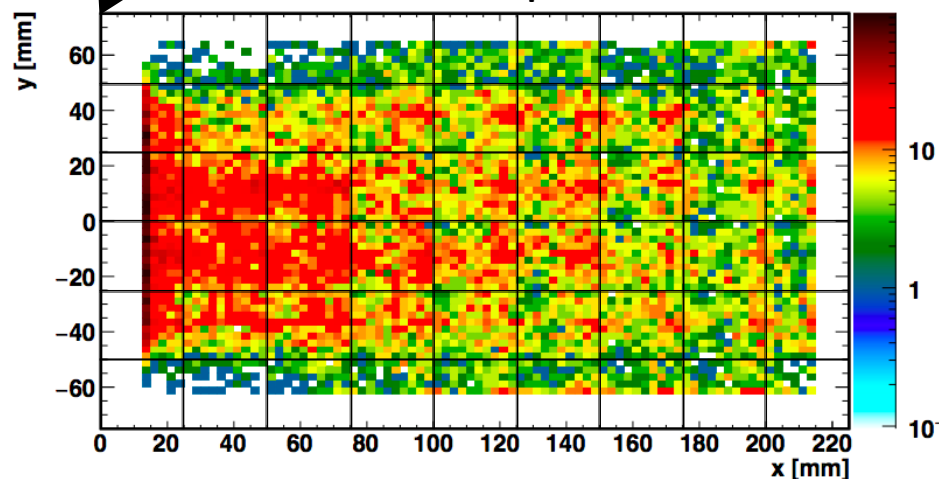
6 × 9 segmented array of  $PbF_2$  crystals.



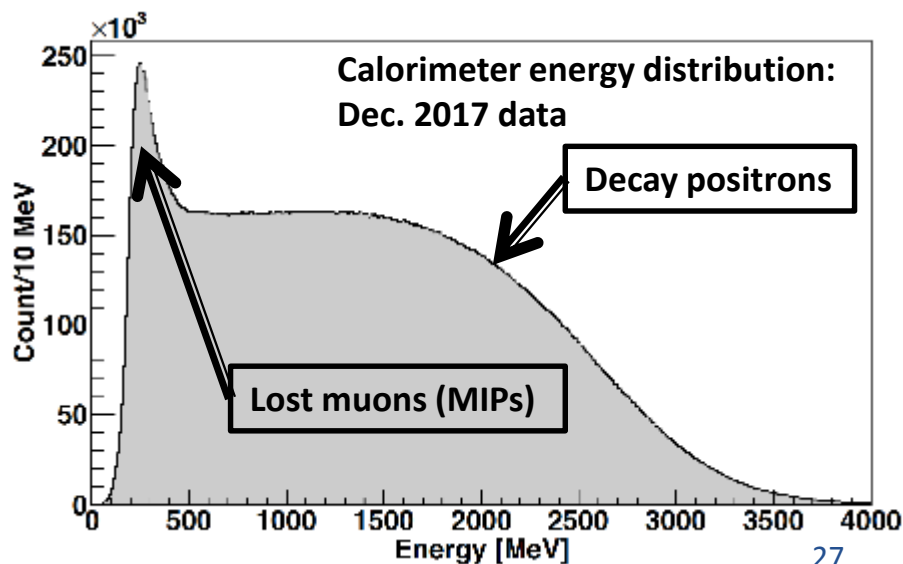
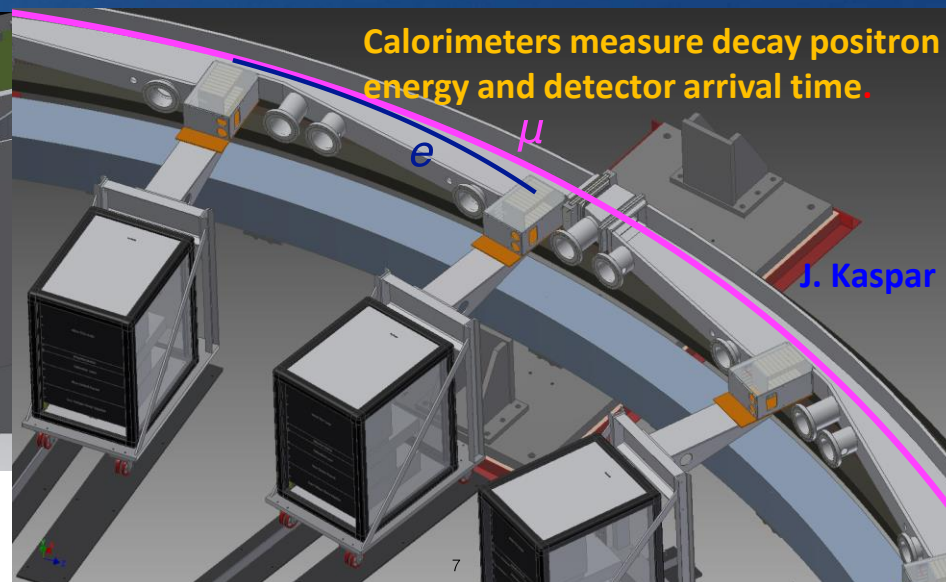
Crystals are 25×25×140 mm

Ring side of calorimeter

Calorimeter cluster spatial distribution



The above June 2017 commissioning data has large proton contamination: 60 p: 4  $\pi$ : 1  $\mu$





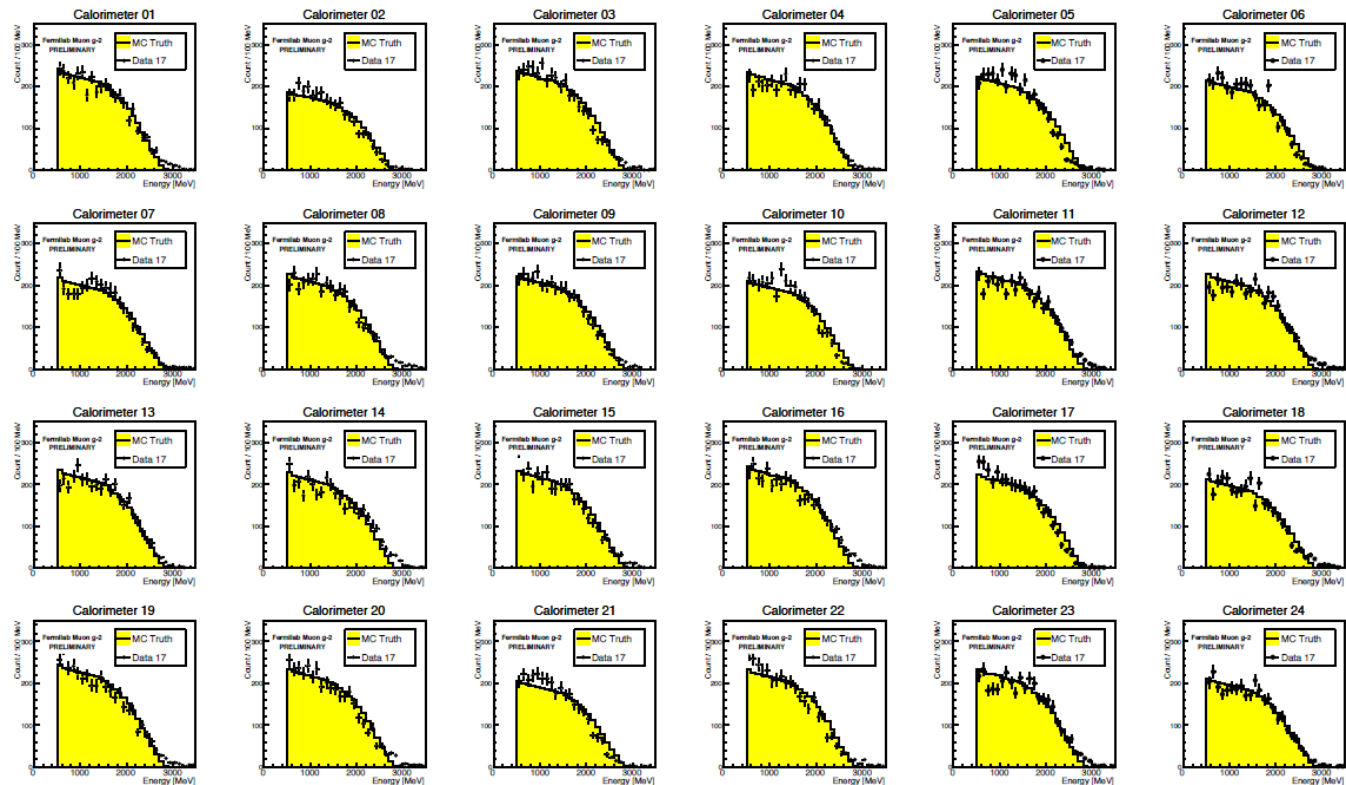
# Calorimeter Response.

Calorimeters well understood both in data and simulations.

Used as online monitors of # of stored muons.

Commissioning data provided opportunity to :

- search for and correct mapping error
- Determine timing offsets between crystals



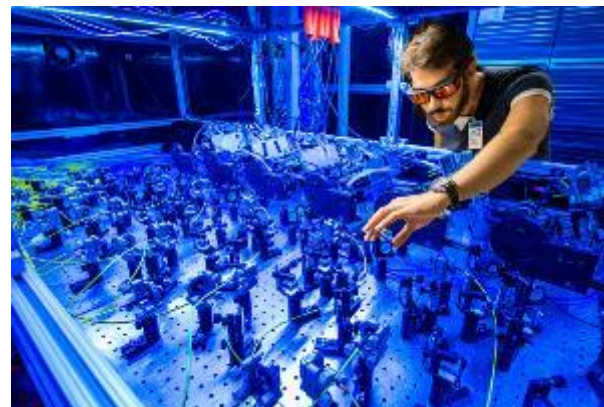


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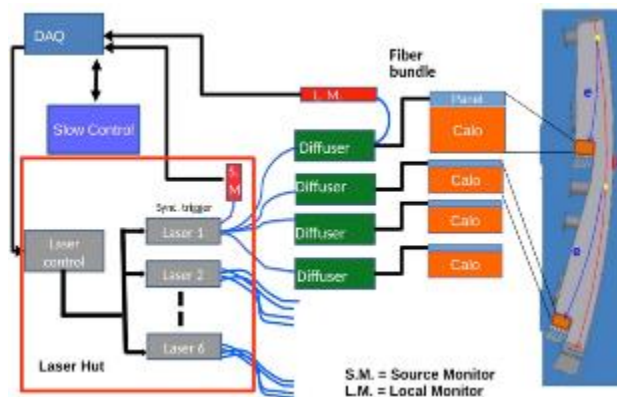
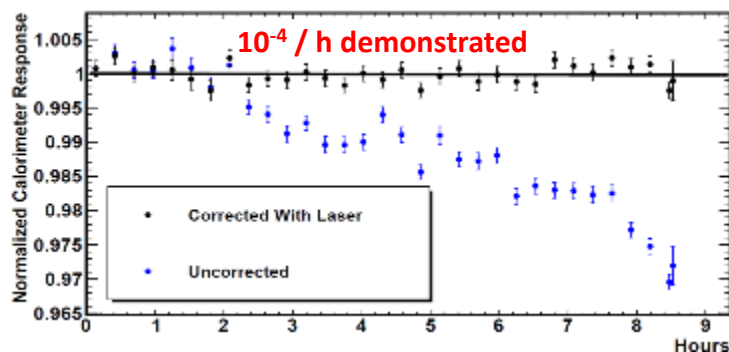
# Calorimeter gain stability established to $\sim \text{few} \times 10^{-4}$

Vital to ensure stability of the calorimeter response in order to avoid introducing varying acceptance as a function of time.

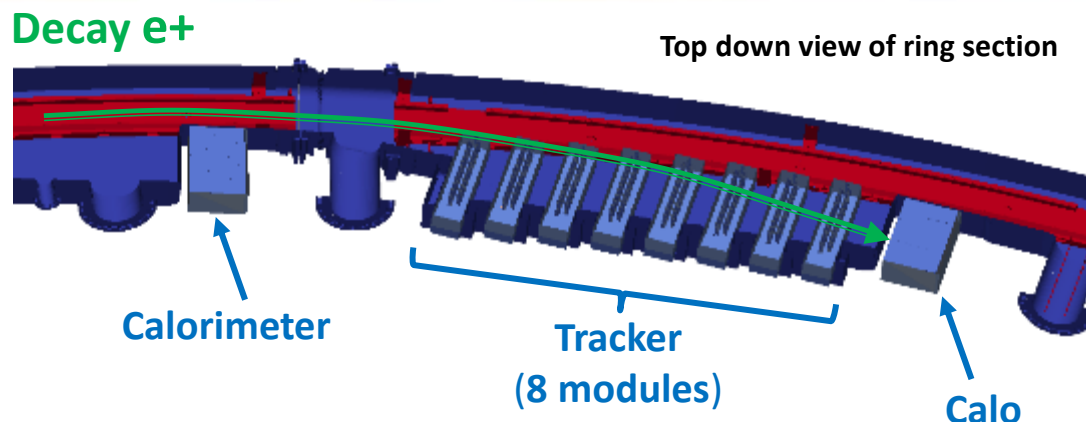
Achieved with a state-of-the-art laser-based calibration system.



Test Beam Data



# Straw Trackers.



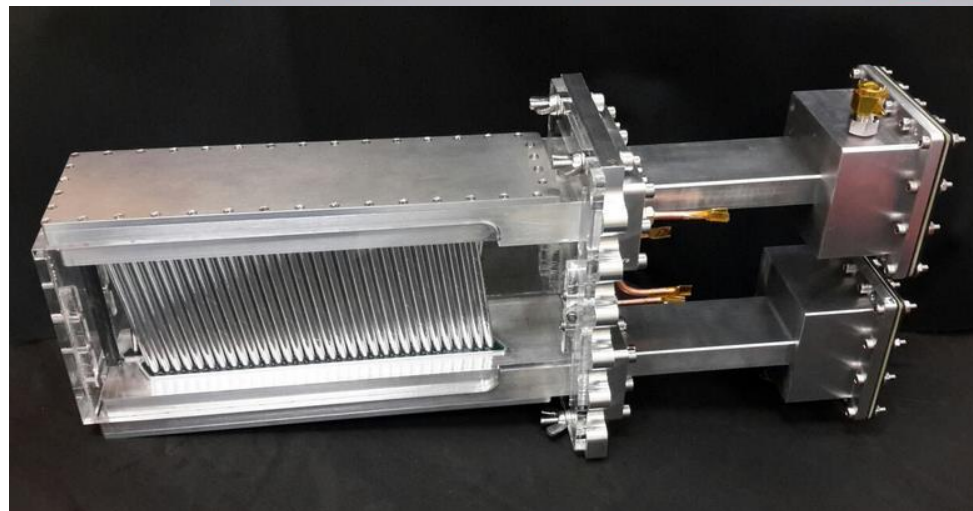
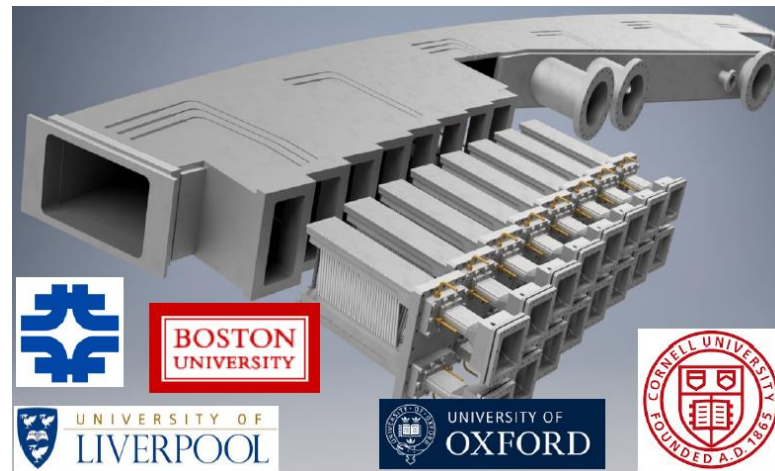
- Main tool for beam position measurements:
  - CBO frequency, envelope, amplitude vs muon momentum
  - Pitch correction
  - B-field convolution
- Provides complementary information to calorimeters:
  - Gain, efficiency, pile-up
  - E-field correction (both fast rotation and directly at late times)
  - Lost muon tagging

# Straw Trackers.

**3 Trackers were built in Liverpool for g-2.**  
**Each consists of 8 4-layer Straw Modules.**  
**Reconstruct trajectory and momentum of positrons from muon decays.**  
**Determine the muon decay point to reduce systematic errors on muon g-2 measurement.**  
**Tracker based muon EDM measurement.**



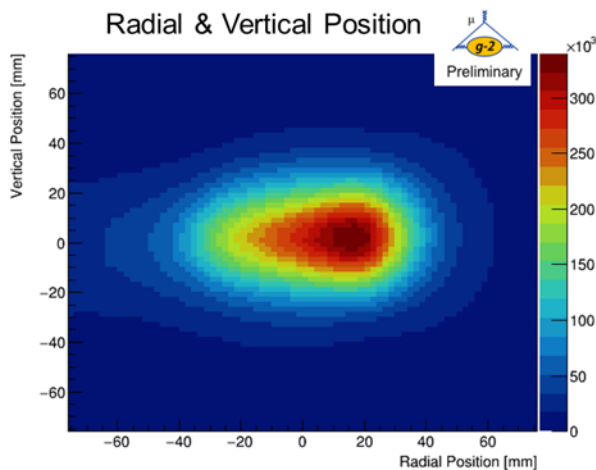
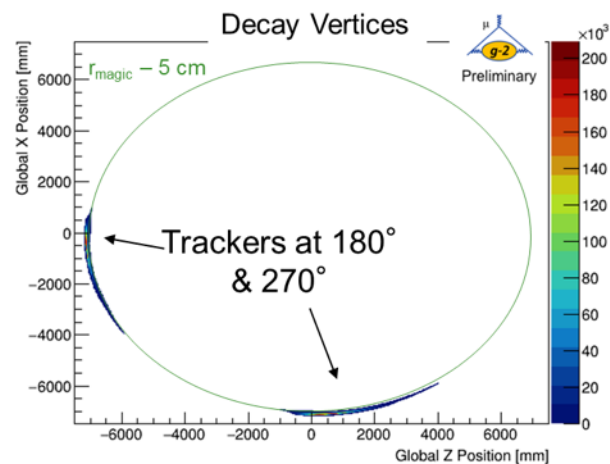
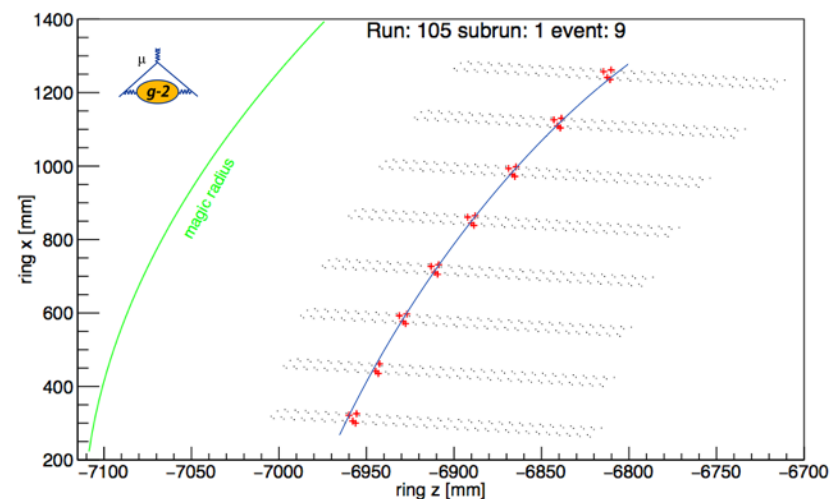
**Vacuum Tank + HV for Module Testing  
In Liverpool prior to shipping to FNAL.**



**4 layers of 32 straws, 7.5° stereo angle**

# Straw Trackers.

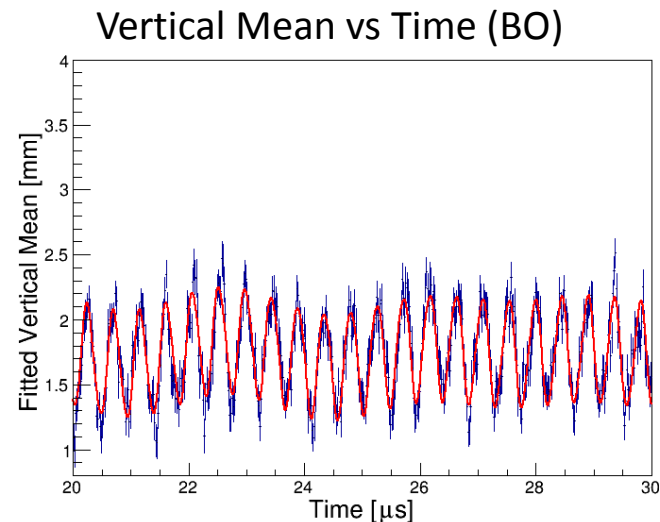
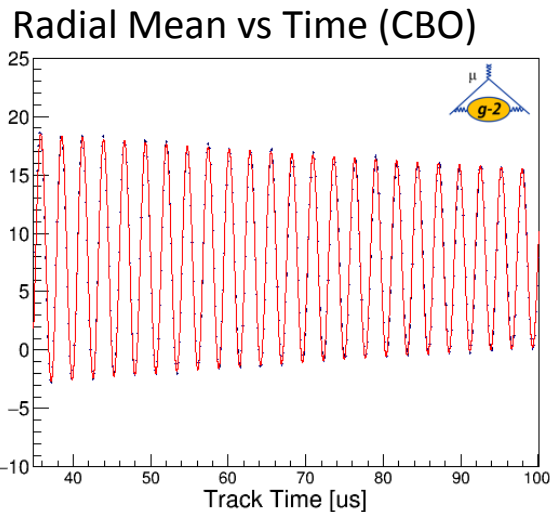
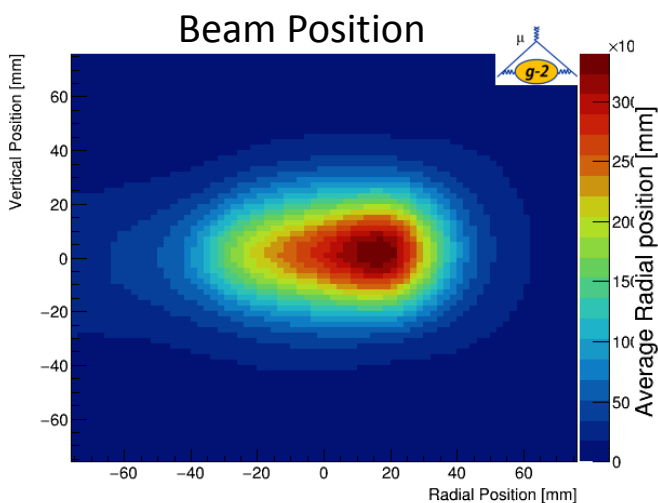
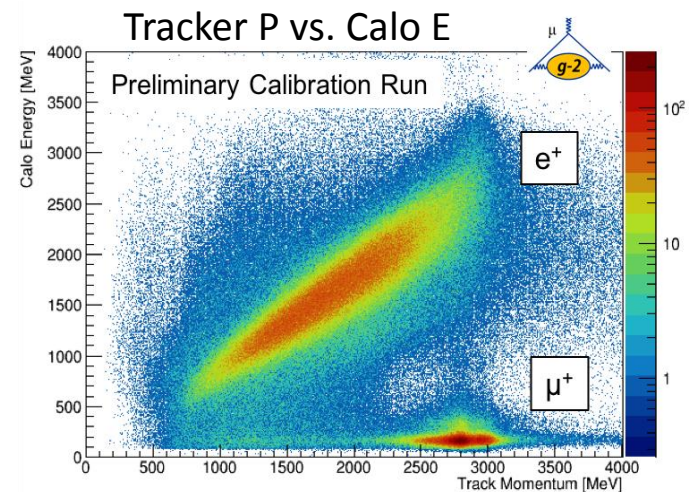
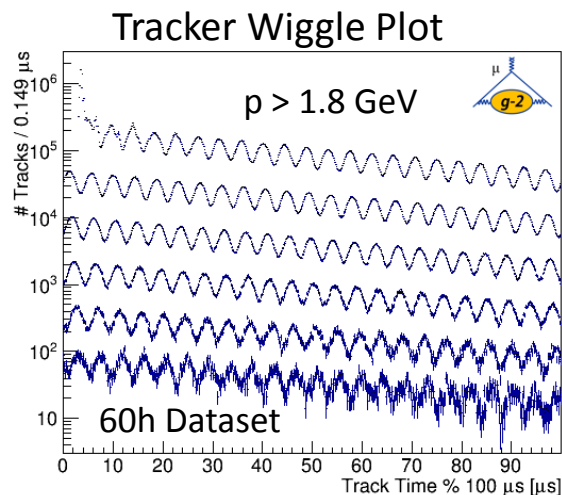
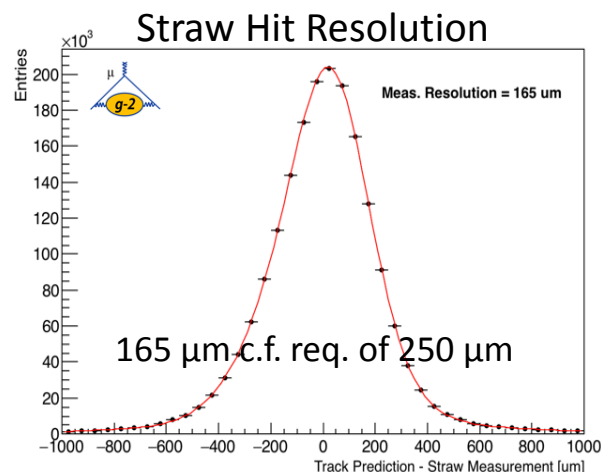
Muon's-eye view inside vacuum chamber



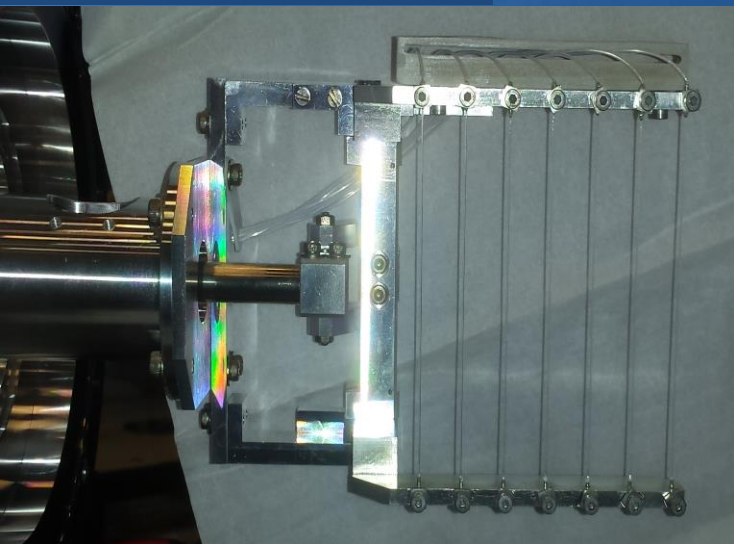
Beam profile is calculated in real time and available during data taking.

# Straw Trackers.

- Track finding & fitting work well:



# Fibre Harps also measure the beam profile.



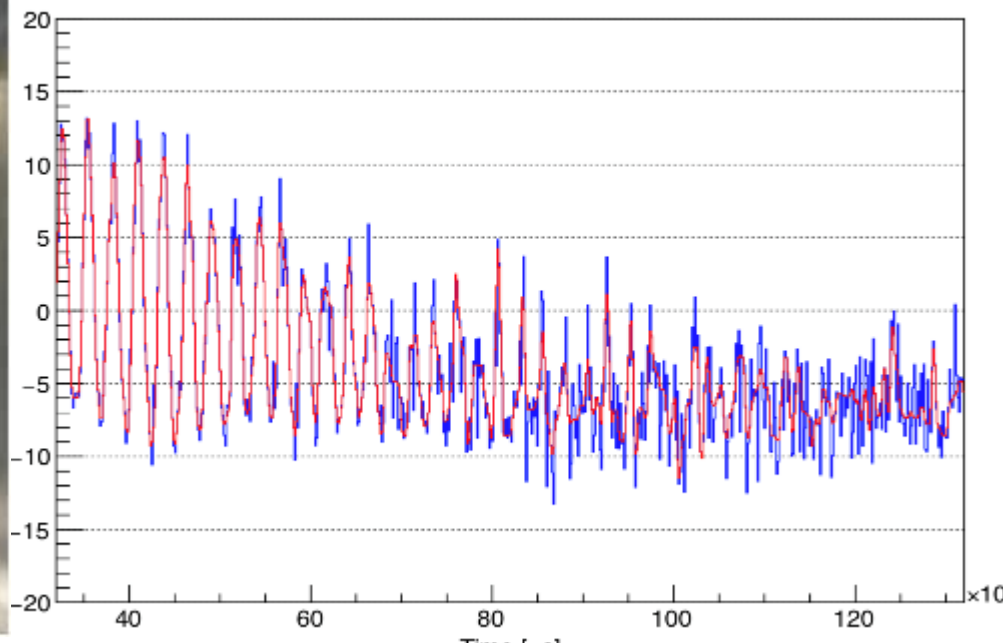
Consist of 7 parallel scintillating fibres at 180 and 270 degrees around the ring.

Horizontal and vertical detectors to measure radial and vertical beam profile.

Retractable since they interfere with the muon beam during normal data taking.



Smoothed centroid for run 8147: Kicker = 2.42/1.98/2.37, Inflector = 2784 A



# Achieving highly uniform magnetic field.

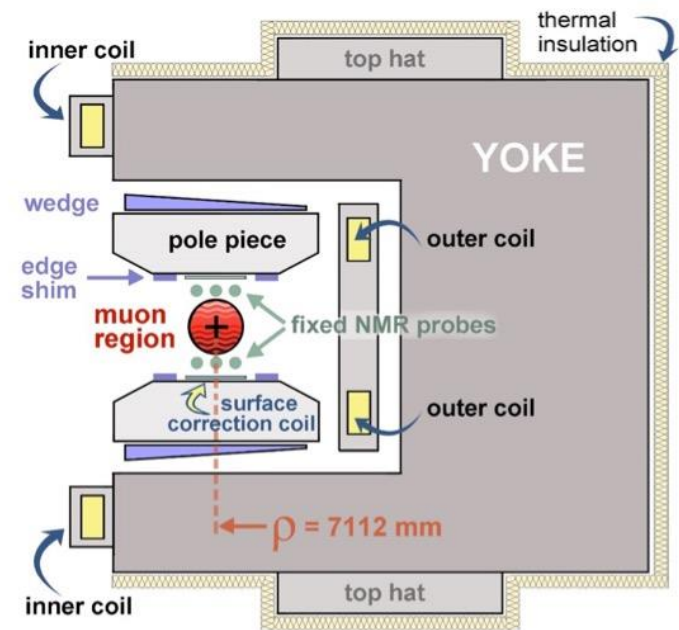


The magnet completed its epic journey from Brookhaven to Fermilab in 2014. It was then reassembled and on initial turn on had a field non-uniformity of  $\sim 1400$  ppm. Then began a period of magnet shimming that culminated in a uniformity of  $\sim 25$  ppm by Sept 2016.

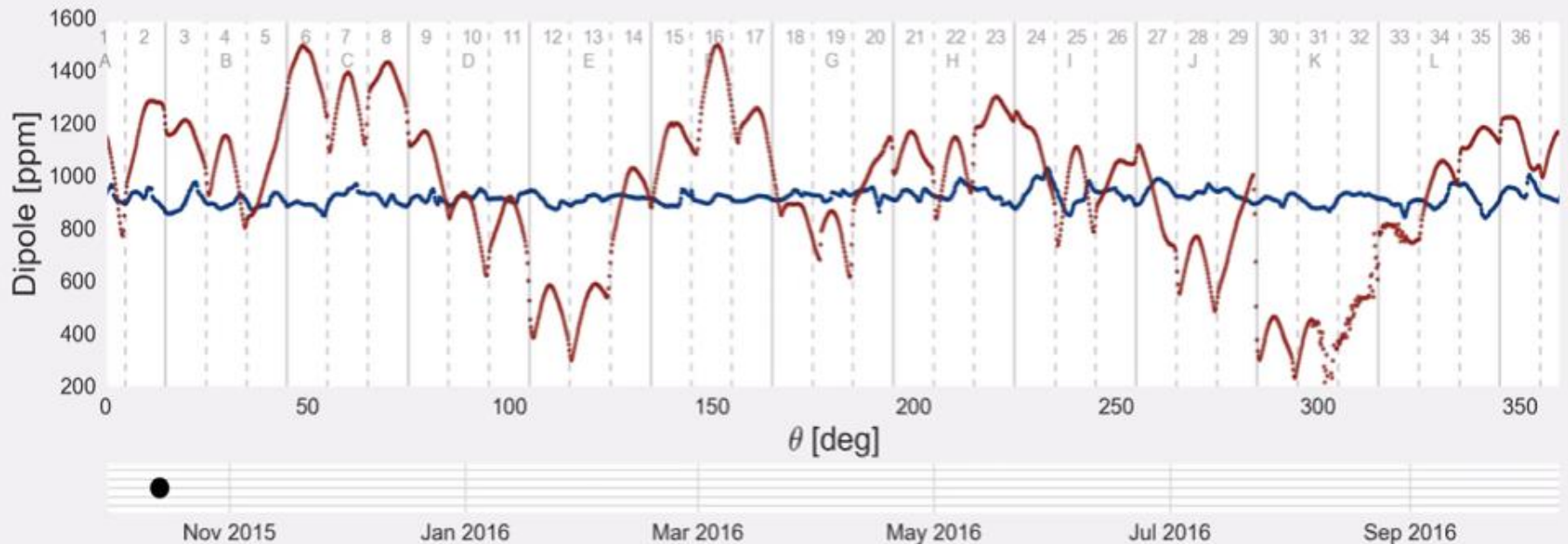
# First stage of shimming: pole surface adjustments



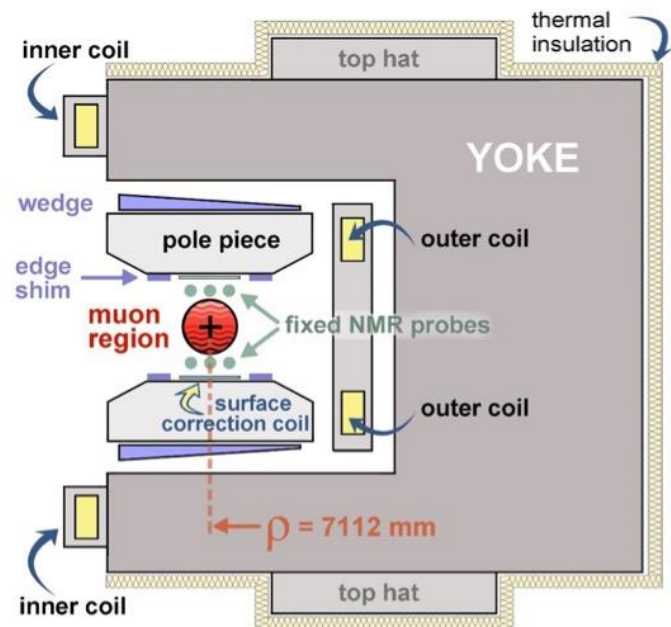
- Blue was shimmed field at Brookhaven
- Red was starting point at Fermilab



g-2 Magnet in Cross Section

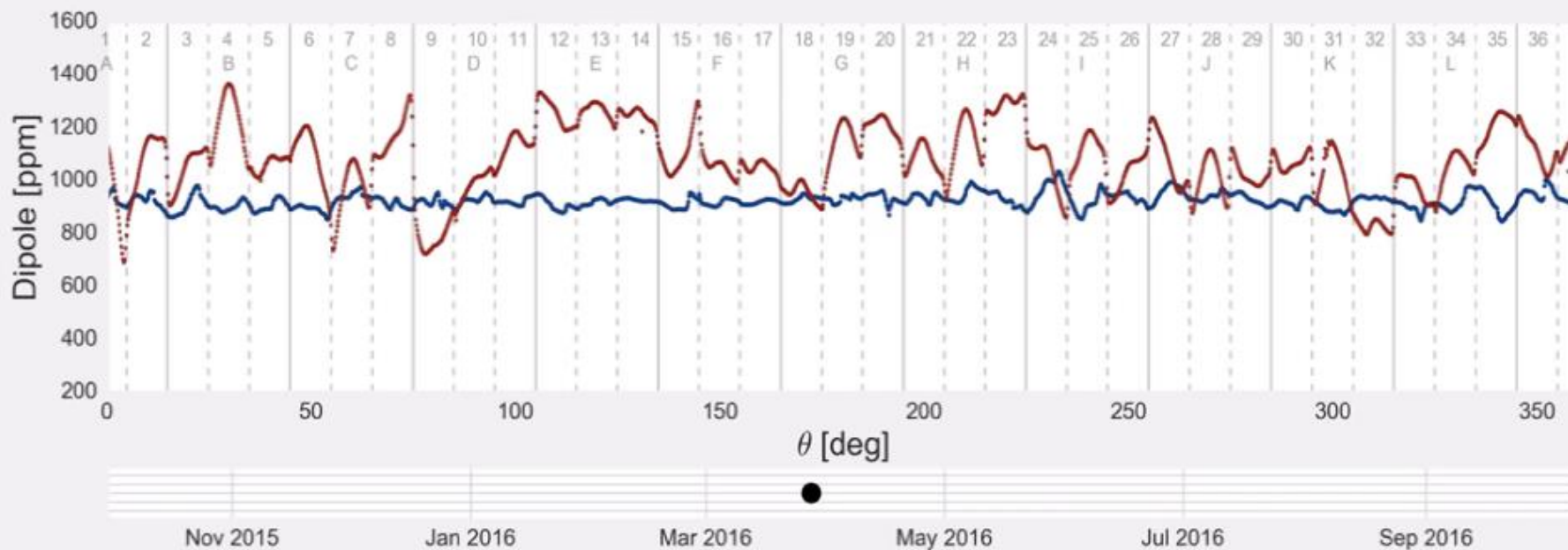


# Next: “top hats” and wedge shims



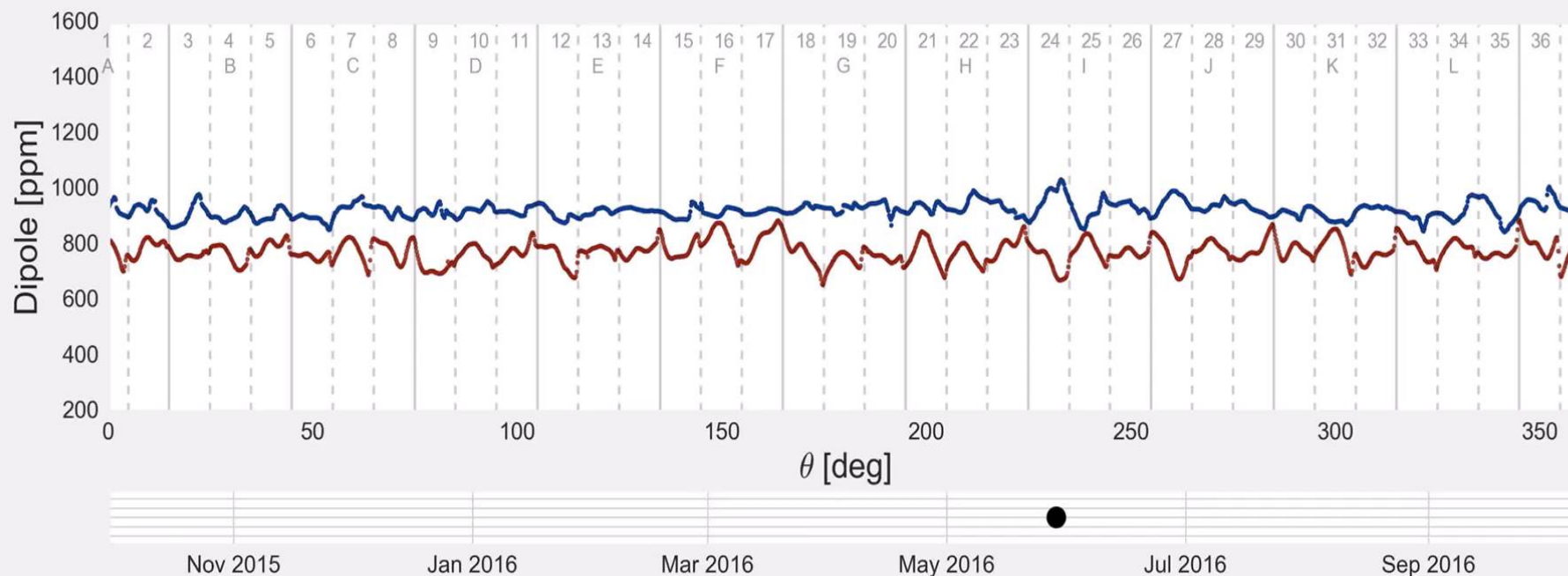
**g-2 Magnet in Cross Section**

**Blue: Brookhaven**   **Red: Fermilab**



leaving azimuthal uniformity comparable  
to Brookhaven.

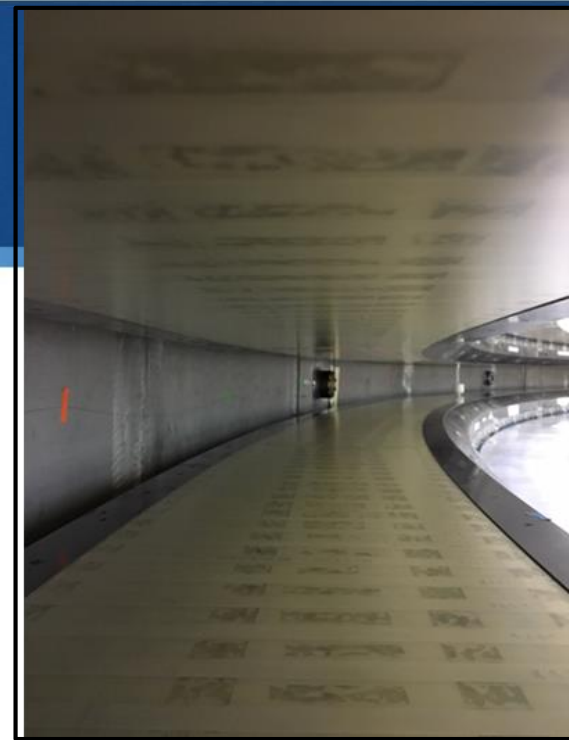
Blue: Brookhaven Red: Fermilab



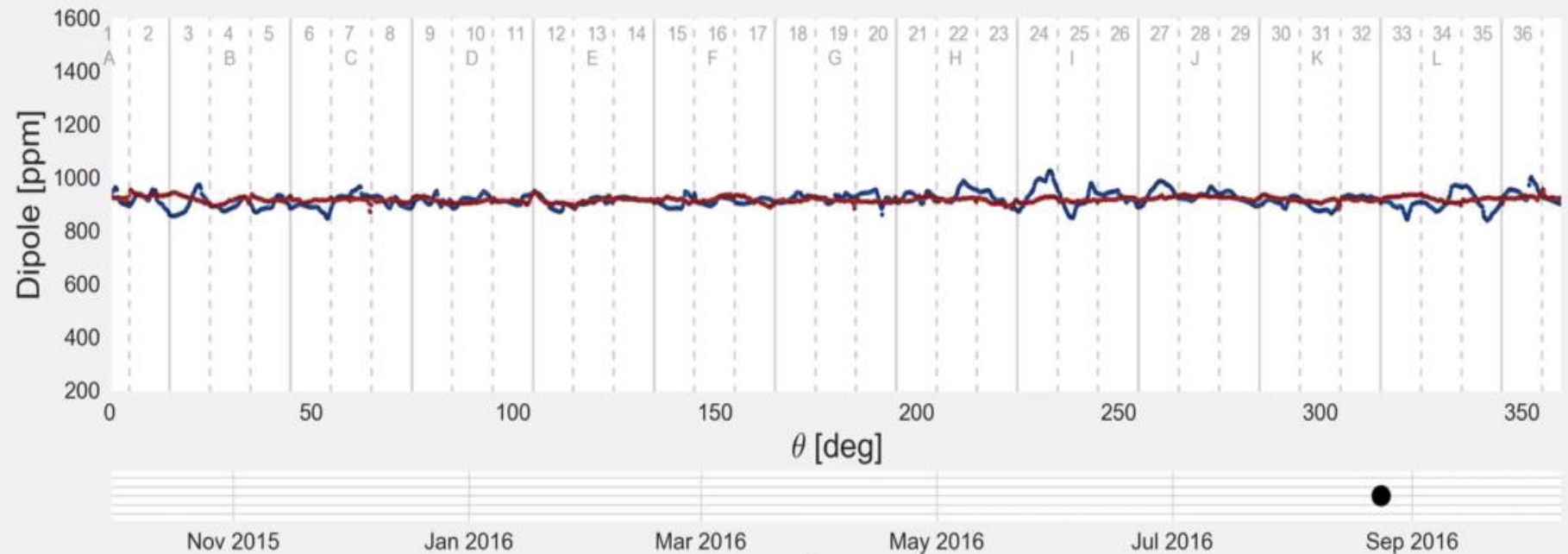
# Final step: iron foil laminations



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**Blue: Brookhaven**    **Red: Fermilab**

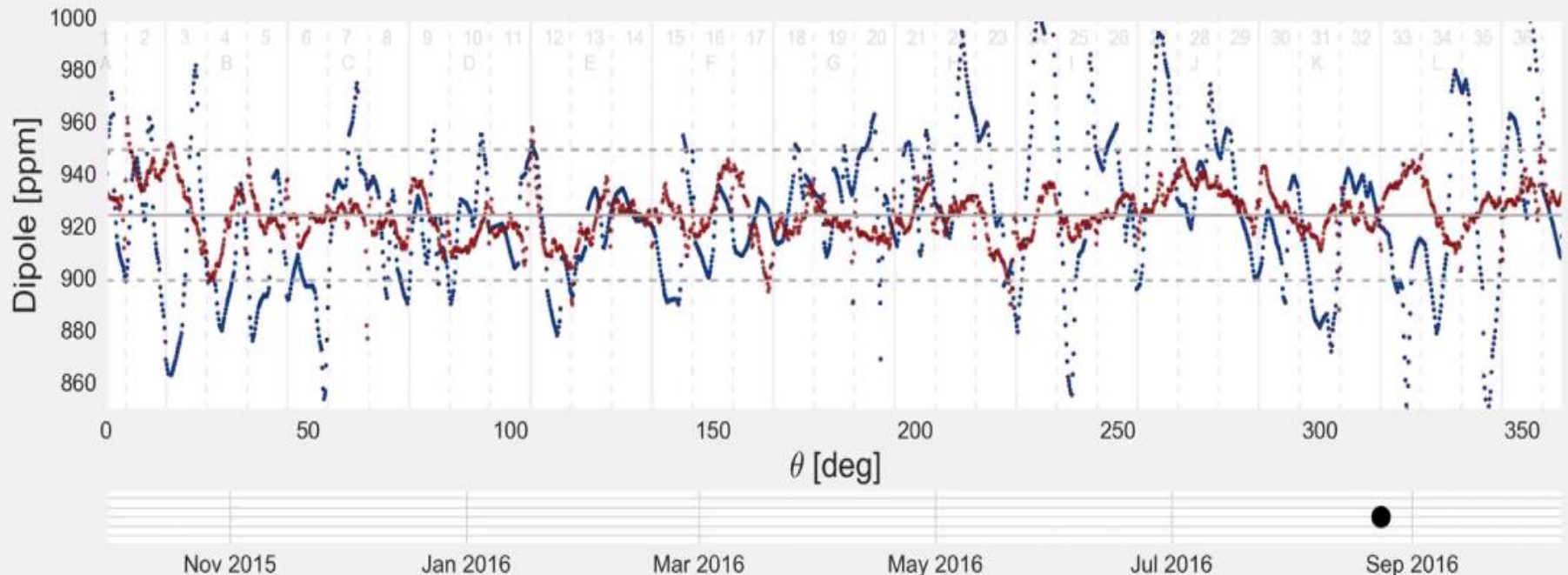
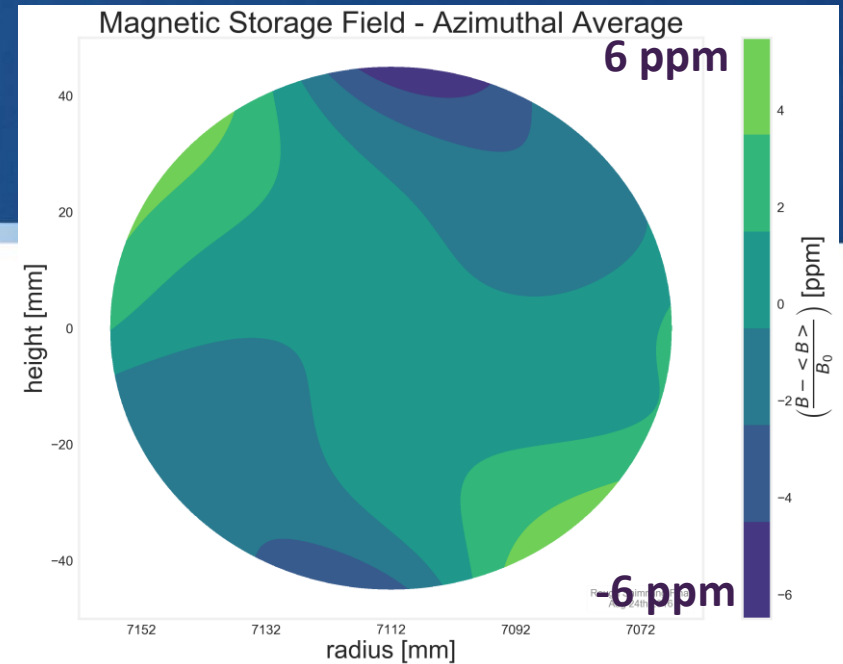




requiring a different  
scale for the graph.

8000 iron shims inserted to achieve a  
uniformity of +/- 25ppm. (Sept 2016).

Blue: Brookhaven Red: Fermilab

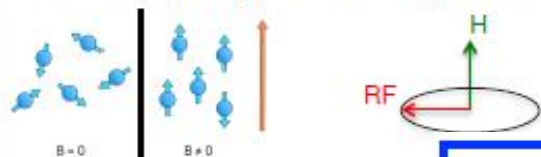


# Magnetic Field measured with NMR.

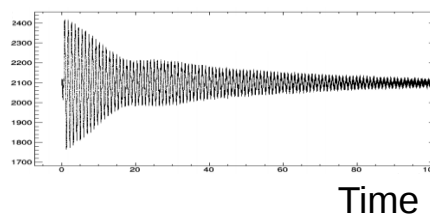
## Pulsed NMR



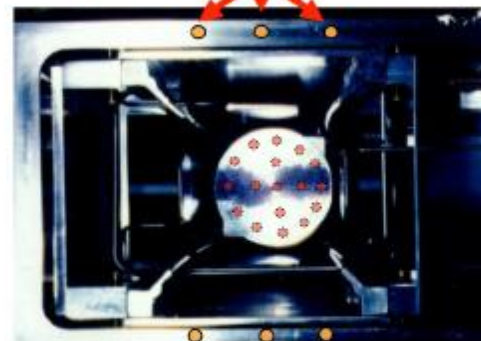
- Sample: petroleum jelly
- Deliver  $\pi/2$  pulse to probe, induce & record the free-induction decay (FID)
- Extracted frequency precision: 10 ppb/FID



## Free-proton spin precession frequency $\omega_p$



## Fixed probes on vacuum chambers



- Measure field while muons are in ring — 378 probes **outside** storage region

## Trolley matrix of 17 NMR probes

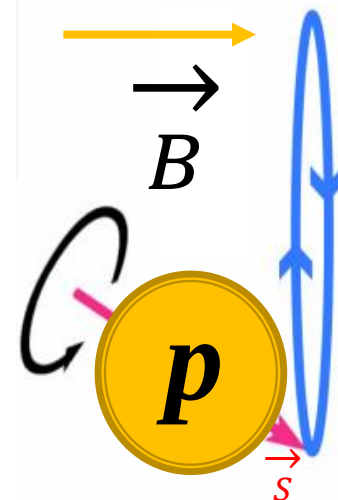


Electronics,  
Microcontroller,  
Communication

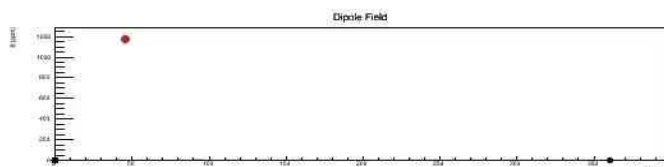
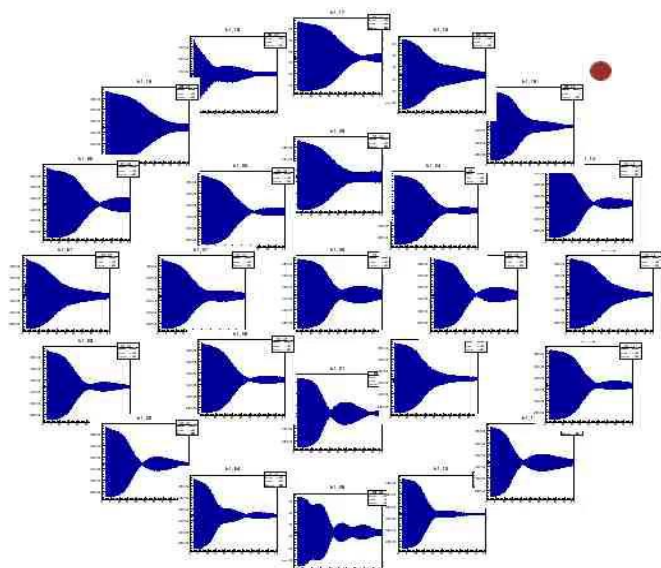
Position of NMR probes

- Measure field in storage region during **specialized runs** when **muons are not being stored**
- Map the field every 3–4 days

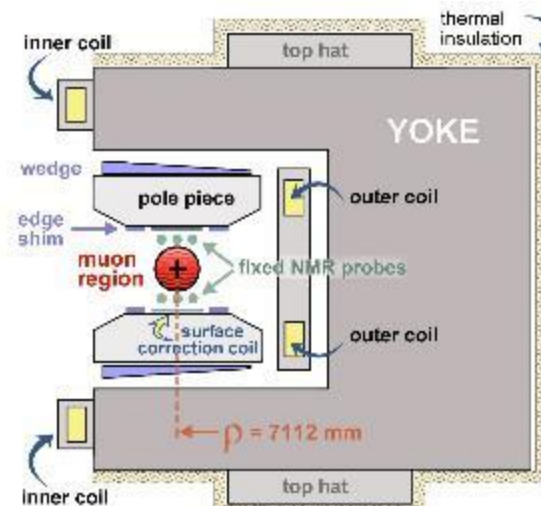
Trolley can be pulled around storage ring when beam is not being delivered.



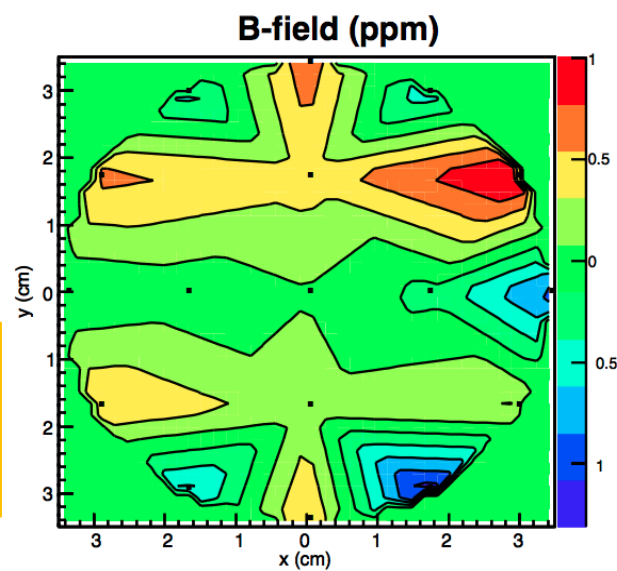
# Magnetic Field Determination.



Field map from March 2018  
(averaged over azimuth)  
Good to 1 ppm.



**g-2 Magnet in Cross Section**

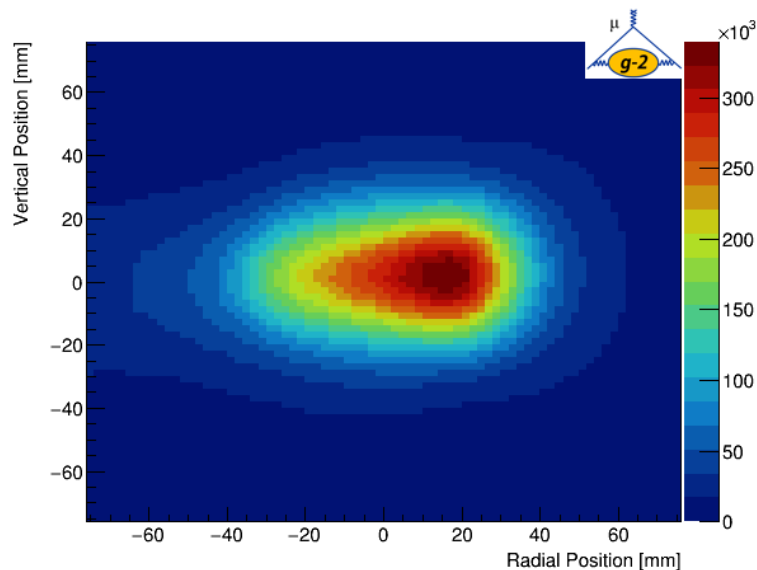


|      | Norm  | Skew |
|------|-------|------|
| Quad | -0.19 | 0.28 |
| Sext | 0.05  | 0.27 |
| Octu | -0.07 | 0.25 |
| Decu | 0.23  | 0.07 |

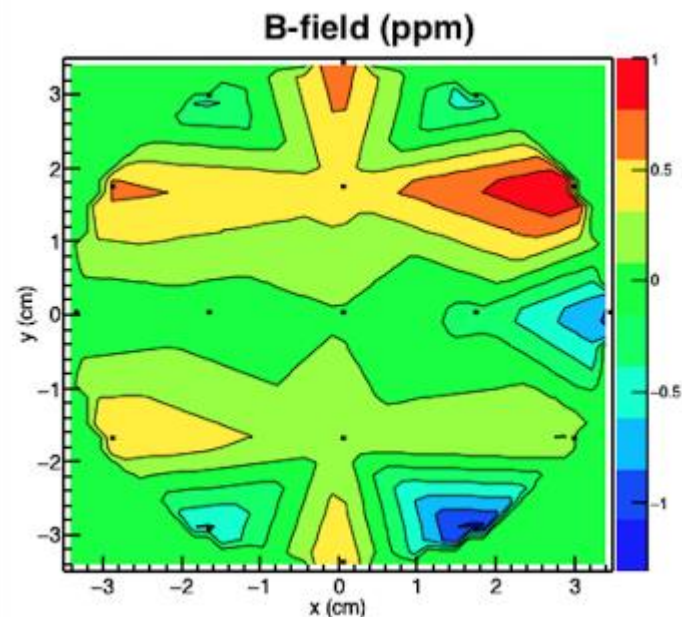


# Determination of B field actually seen by the muon beam.

Obtain the muon beam distribution from the Straw Trackers.



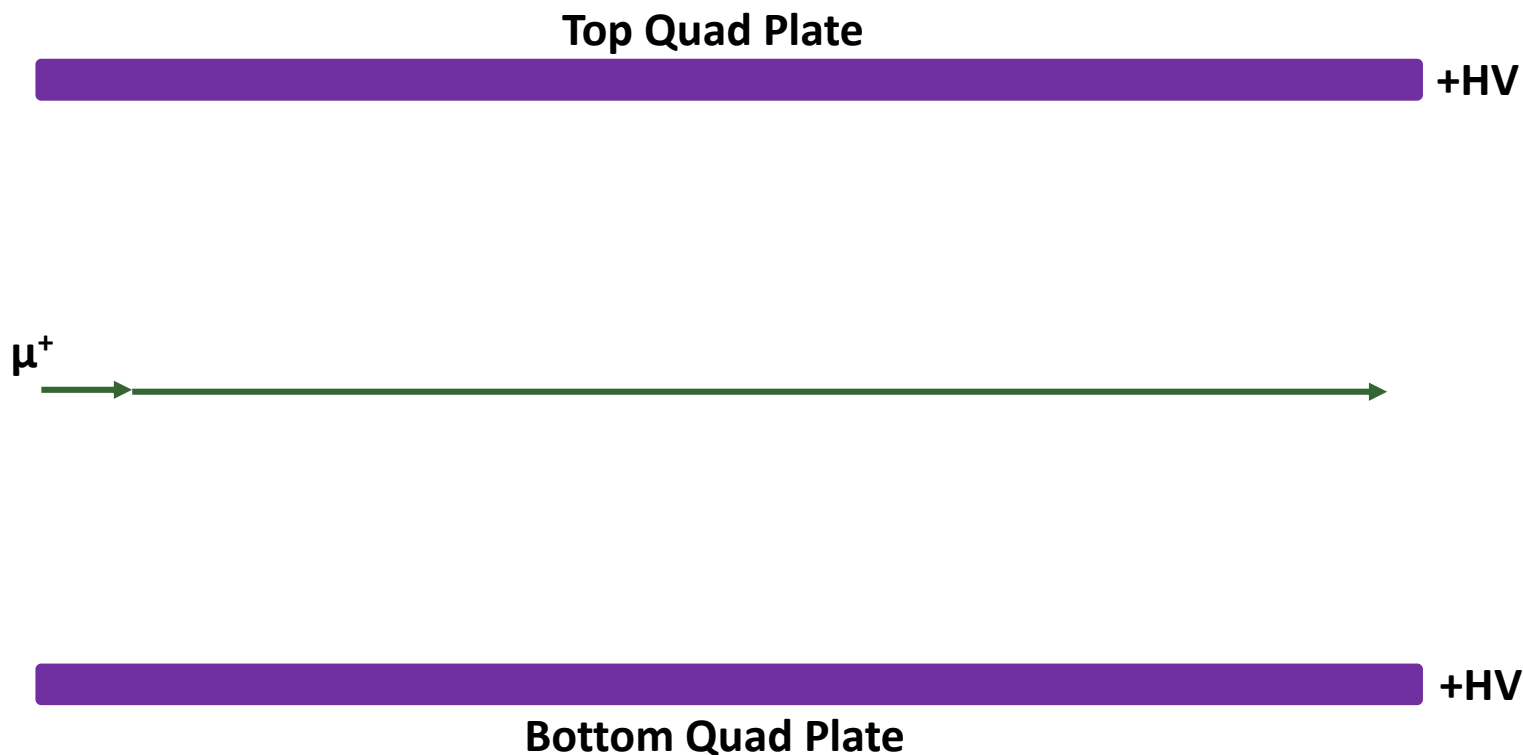
Obtain the B field from NMR measurement probes.



Combine to obtain the actual magnetic field experienced by the muons.

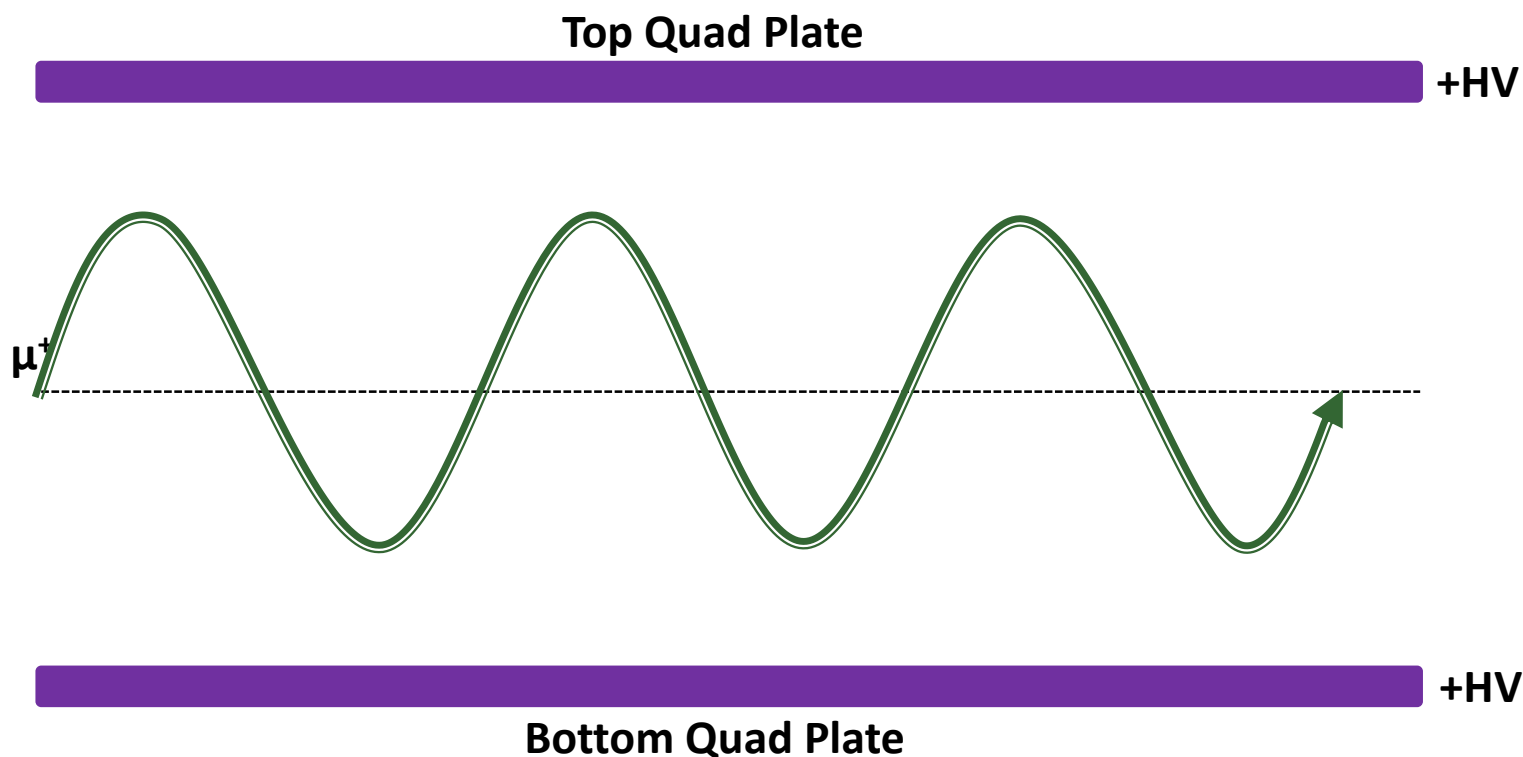
# Example of an $\omega_a$ systematic: Betatron Oscillations.

- Imagine that we could inject all our muons into the ring at  $y = 0$  with no vertical momentum at all
- The muon stays perfectly horizontal until it decays:



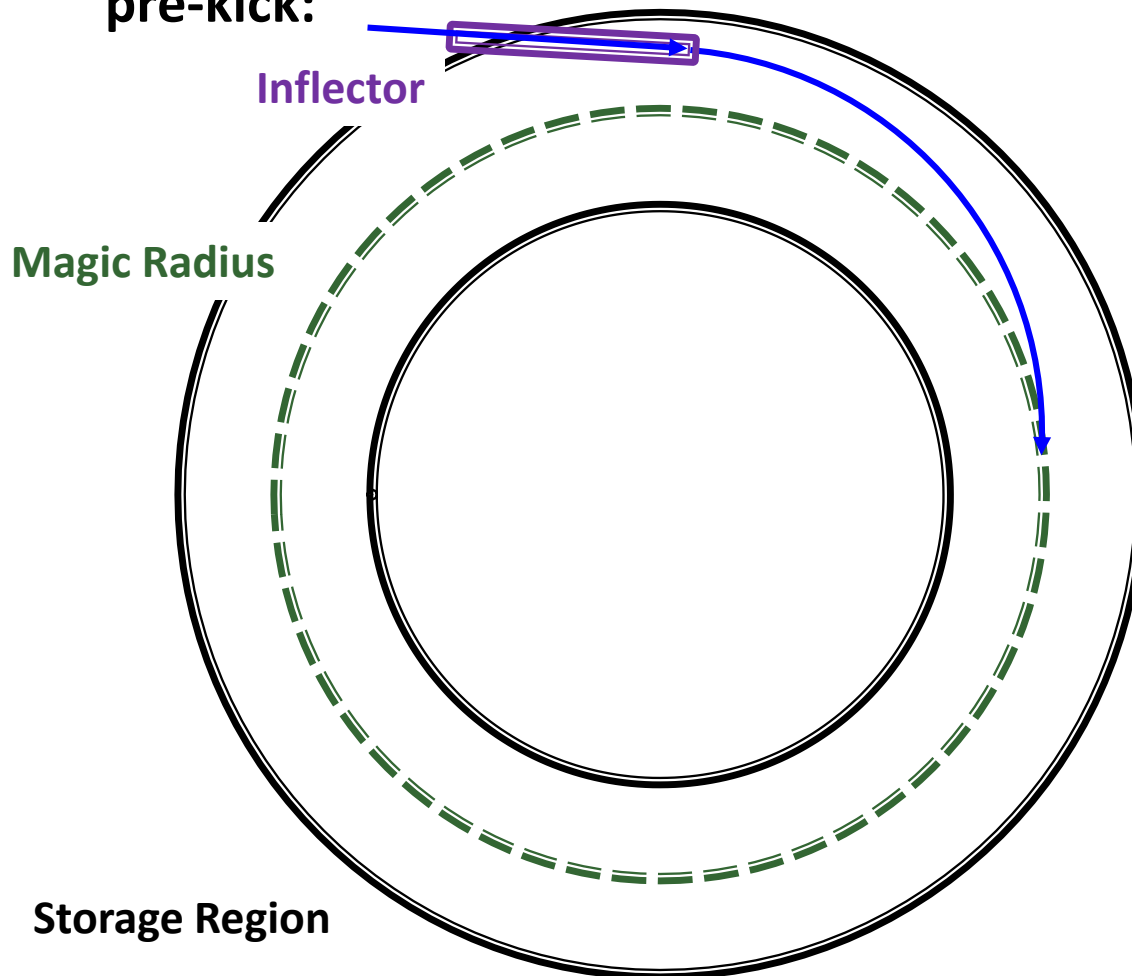
# Vertical Betatron Oscillations:

- If we inject with a non-zero vertical momentum, the particle will oscillate due to the restoring force from the quad field
- Amplitude is related to incoming direction (momentum)



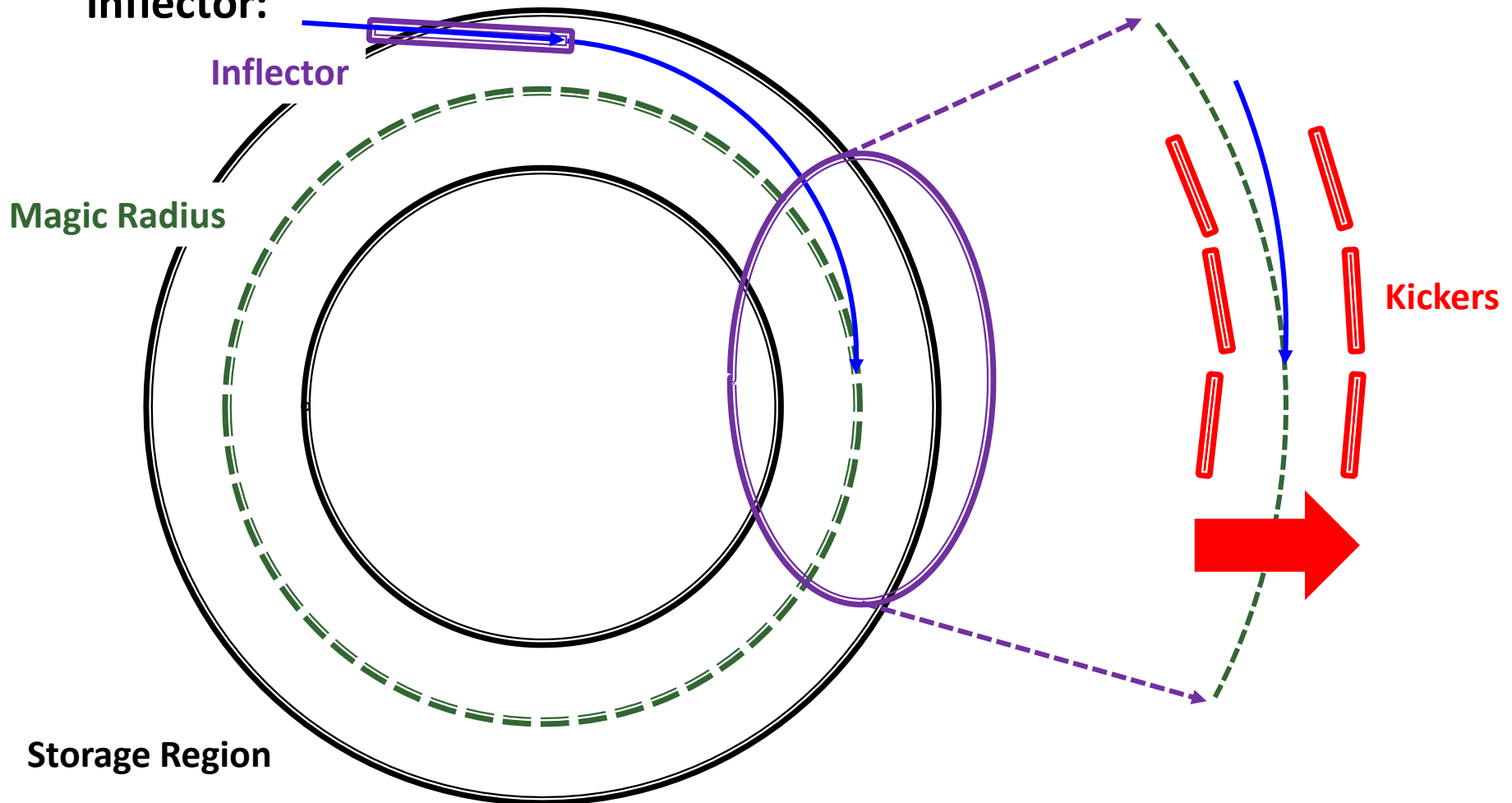
# Betatron Oscillations: Radial Case

- Radial case is a bit more complicated. Start with a horizontal muon pre-kick:



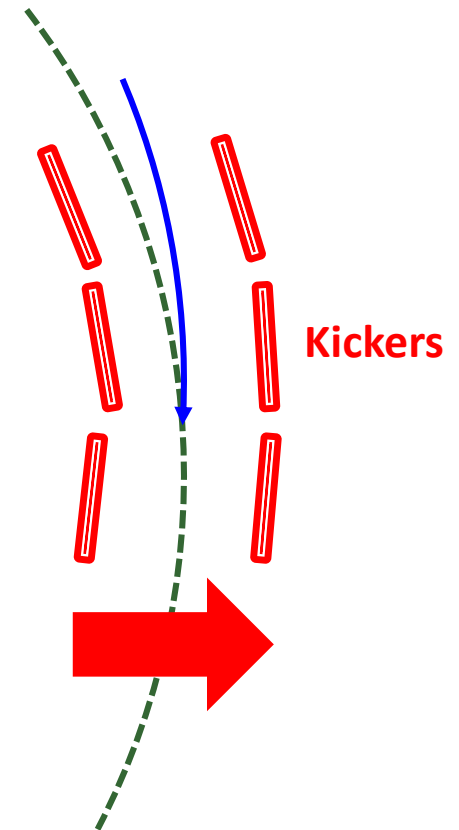
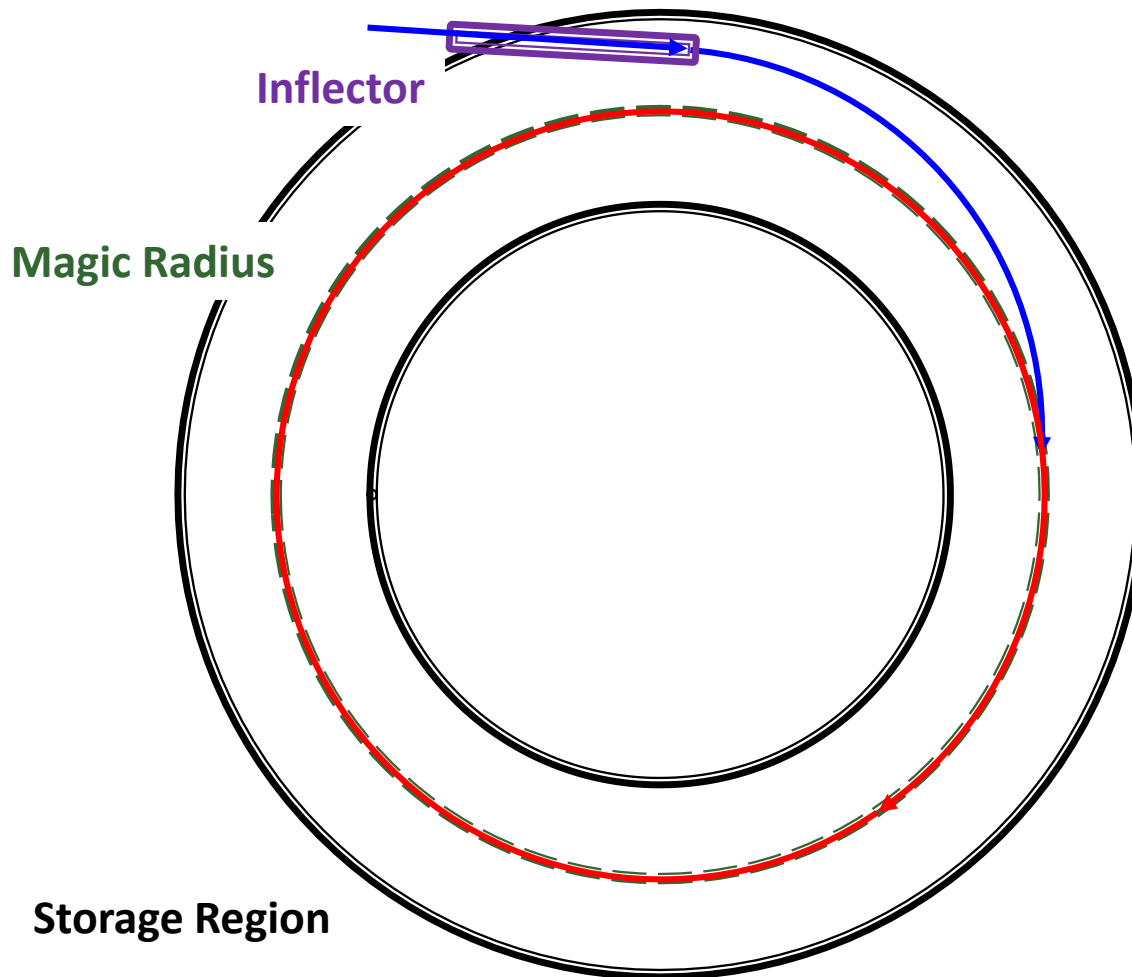
# Betatron Oscillations: Radial Case

- We need to kick the particle to stop it coming back round into the inflector:



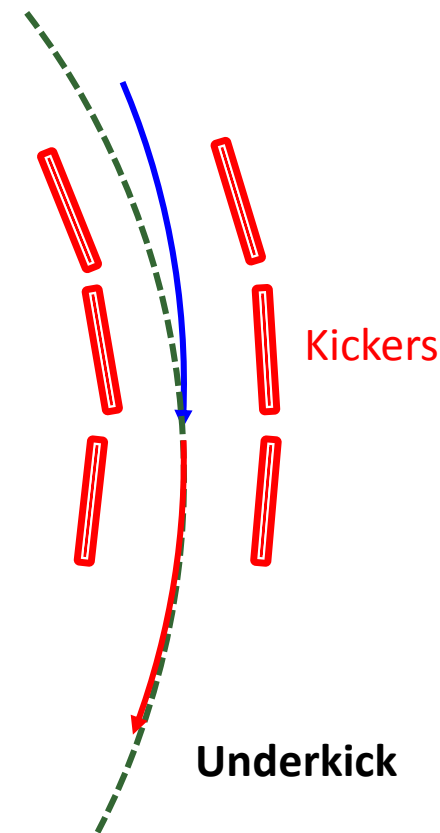
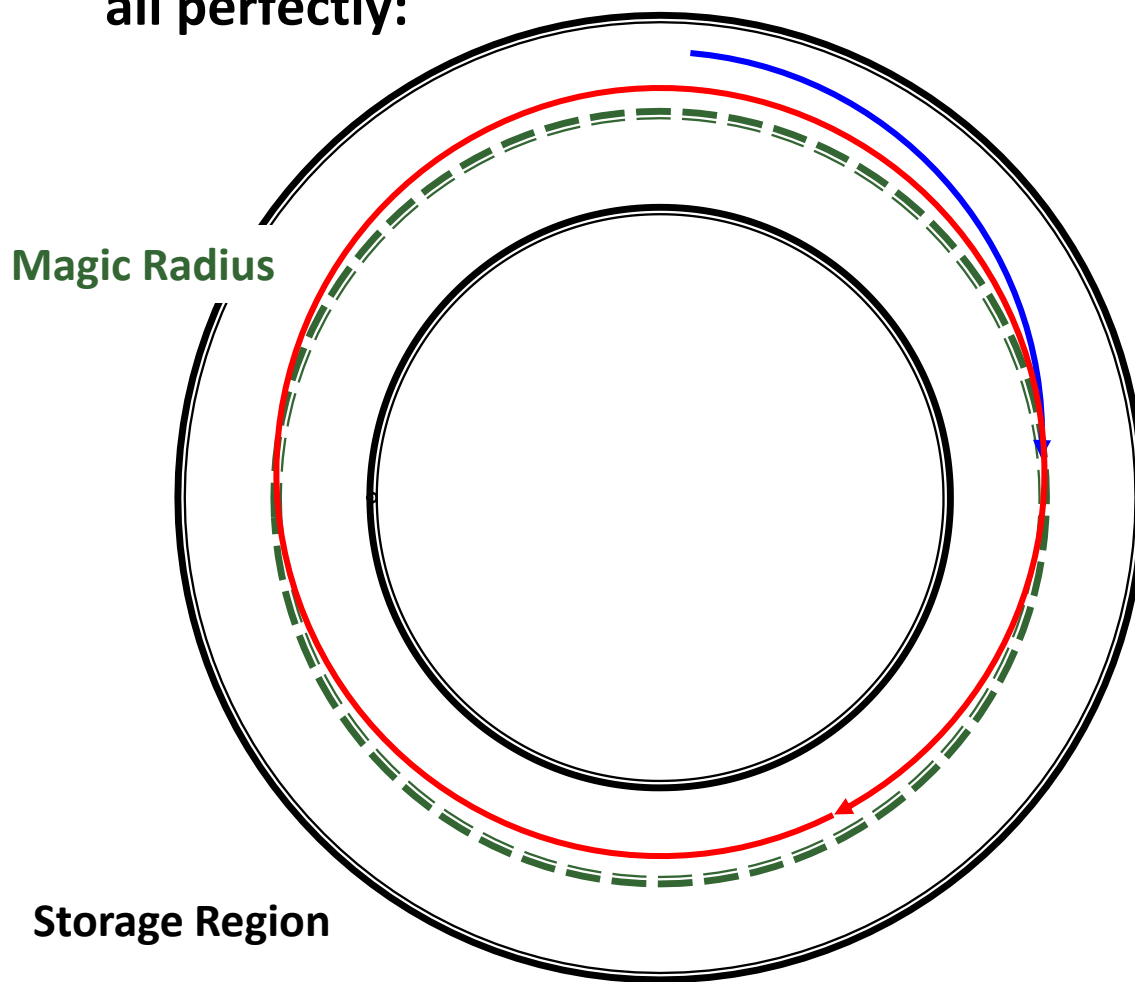
# Betatron Oscillations: Radial Case

- If kick is perfect, we end up on the magic orbit with no radial motion:



# Betatron Oscillations: Radial Case

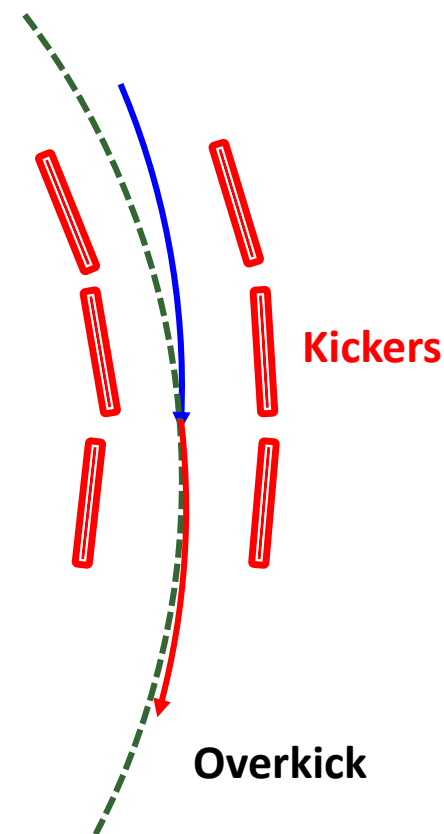
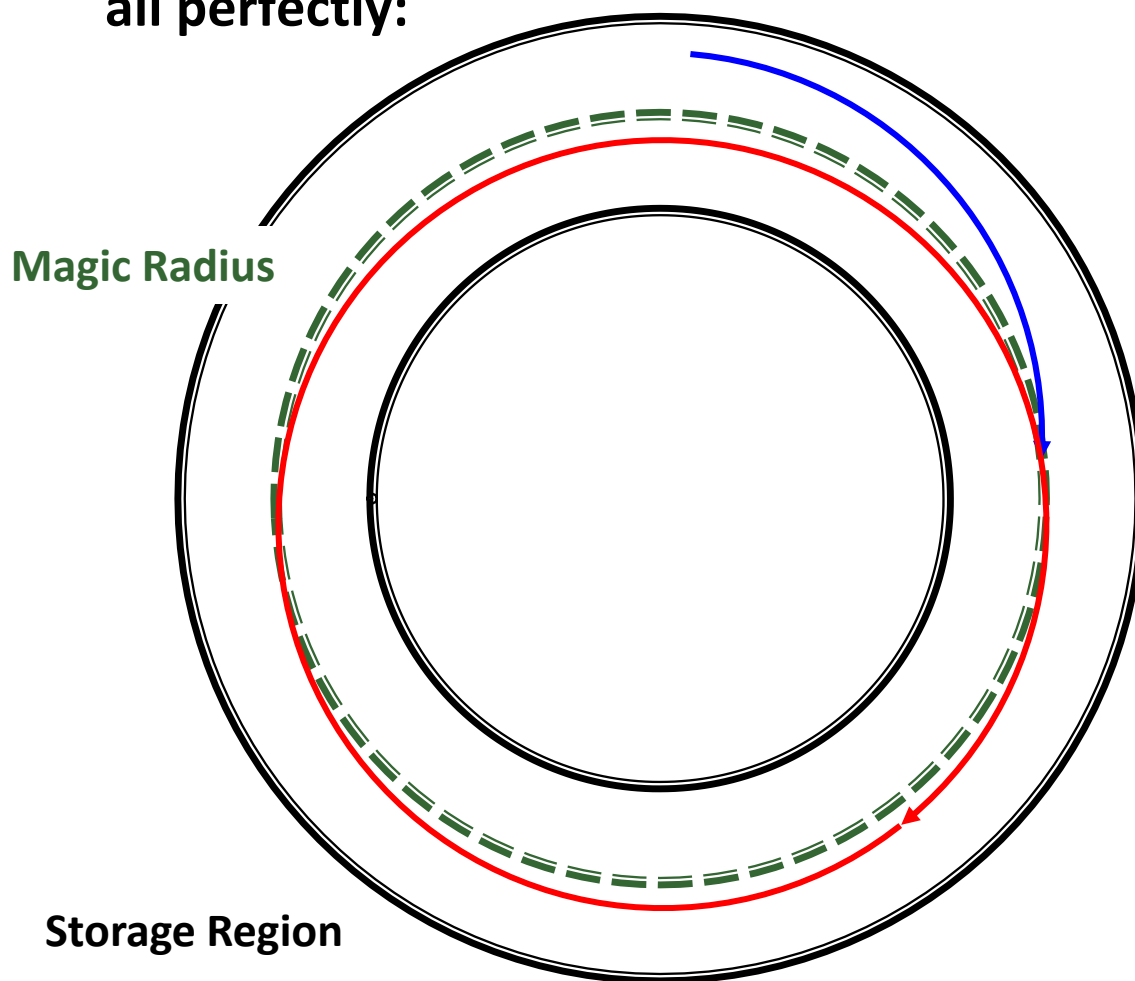
- But we have many muon directions/momenta and we can't kick them all perfectly:



Muons oscillate radially in/out

# Betatron Oscillations: Radial Case

- But we have many muon directions/momenta and we can't kick them all perfectly:



Muons oscillate radially in/out

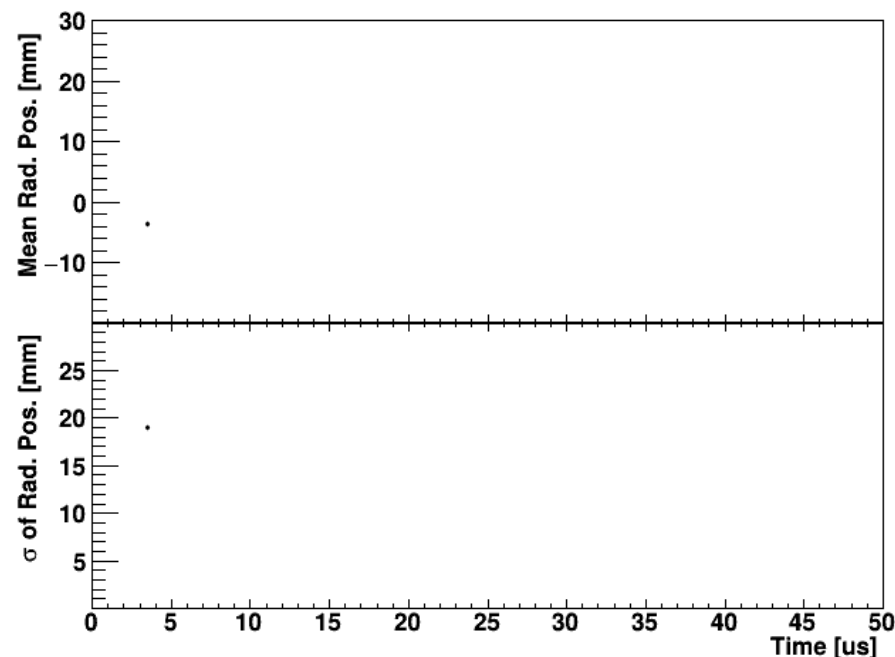
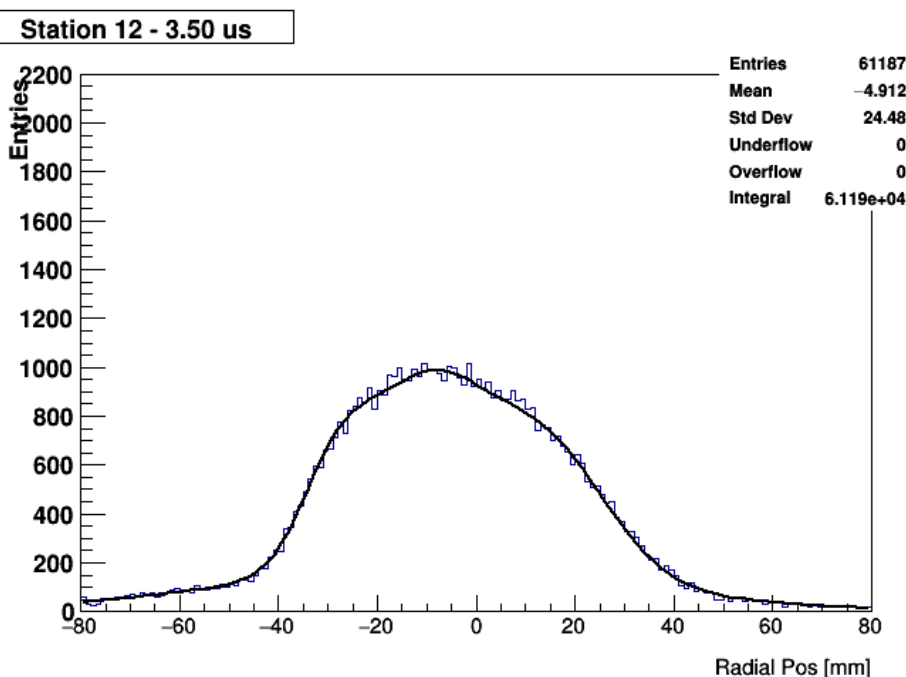
# What is CBO?



- Coherent **B**etatron **O**scillation – movement of all muons together
- Muons all started at **similar position** (as they came through inflector)
- They have **same betatron frequency**, so there's a coherent movement back and forth on average
- **Smeared out** by **different kicks** that each particle gets
- This is **washed out** over time due to the different **cyclotron frequencies** of different momenta (as with fast rotation)
- This is caused by both imperfect kick and because we can't fill entire phase-space of ring at injection

# But does this really happen?

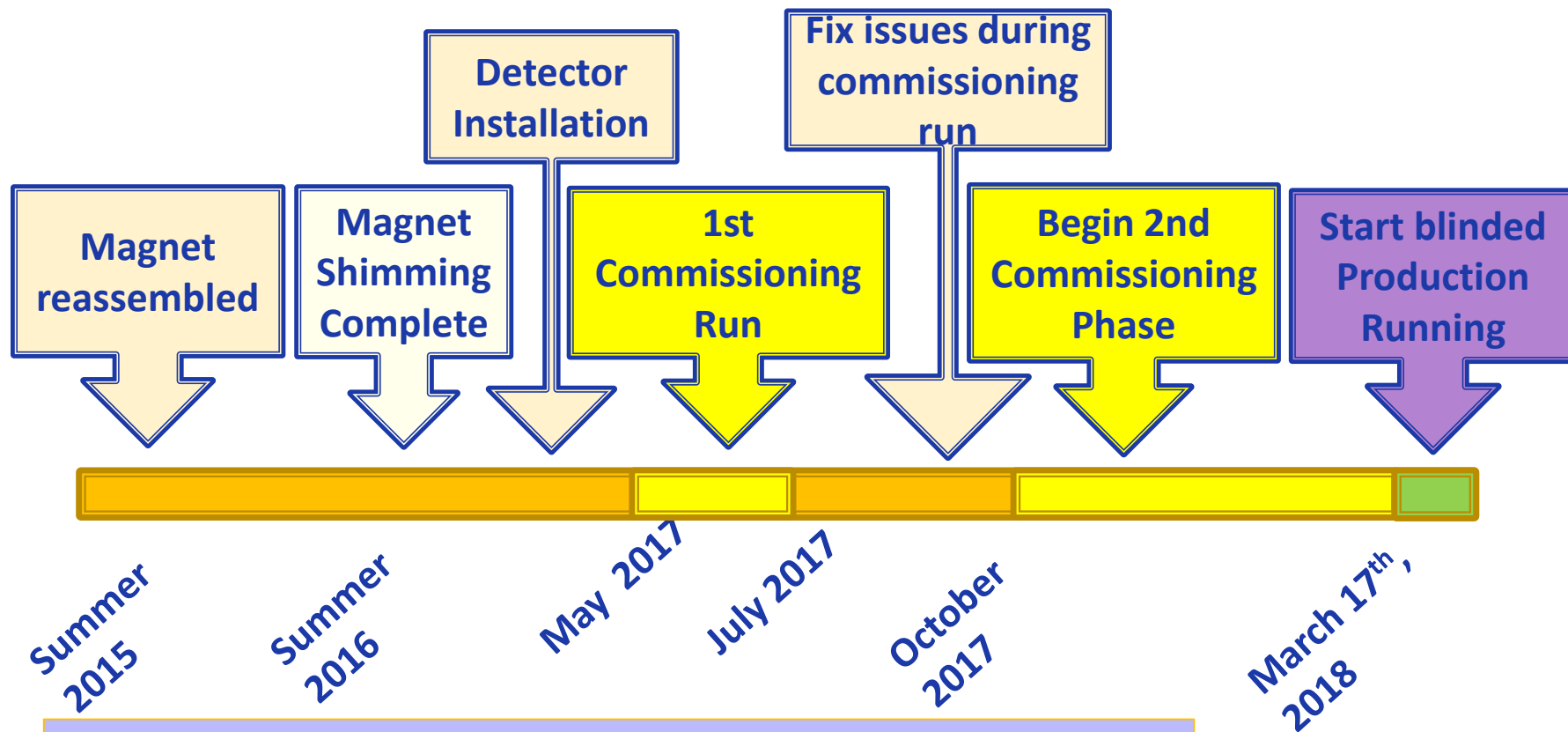
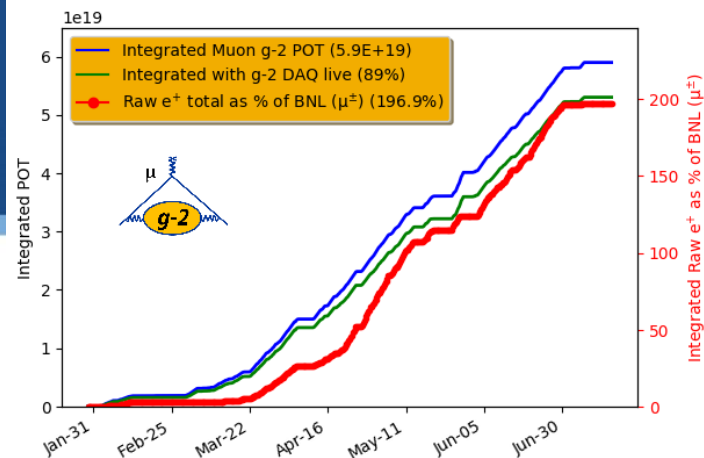
- Yes! Here's some data showing the radial CBO in a tracker:



Why do we care? We will see that the wiggle plot is affected.

# The data so far.

The recent physics run ended on July 7<sup>th</sup>.

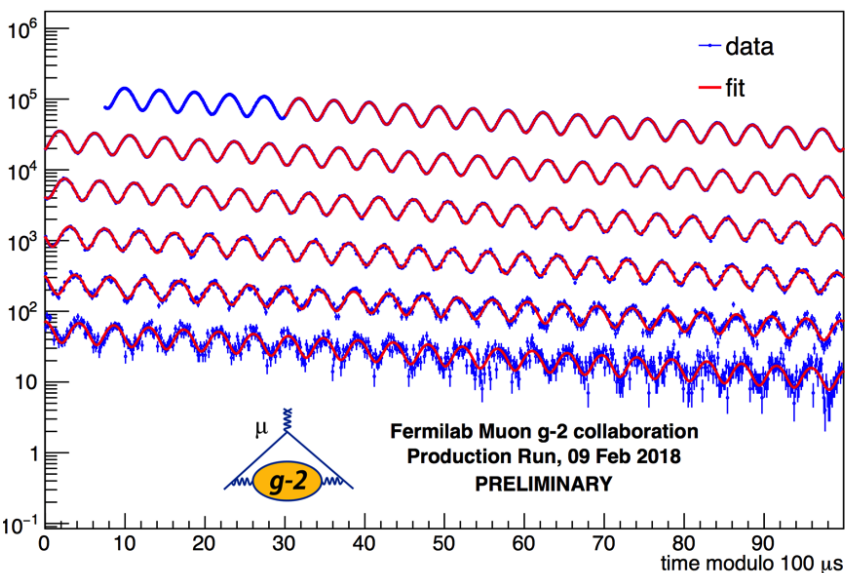


Approximately twice the BNL dataset collected.

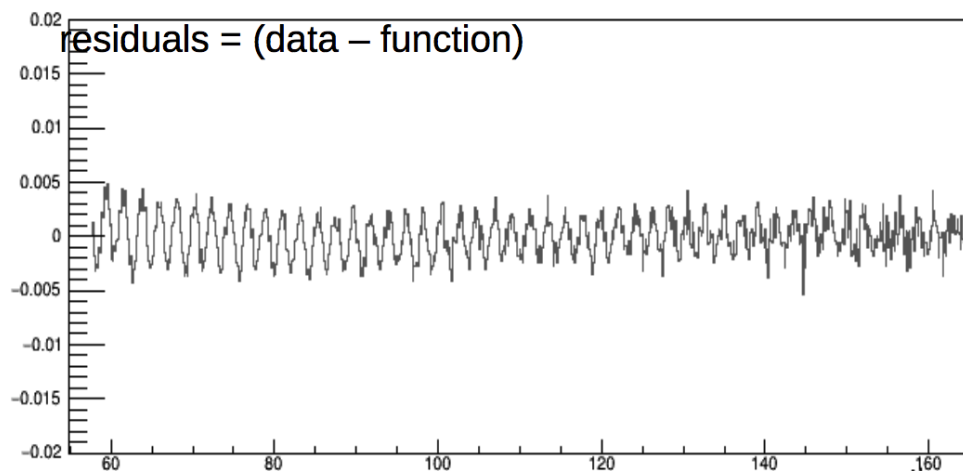
# Measurement of $\omega_a$

In principle, we perform a 5 parameter fit to the wiggle plot to extract  $\omega_a$ . The analysis is blinded – I don't know the result!

$$dN / dt = N_0(t) e^{-\frac{t}{\tau}} [1 + A(t) \cos(\omega_a t + \phi_a(t))]$$



**Residuals to the fit highlight the effects of systematics such as the CBO discussed earlier.**



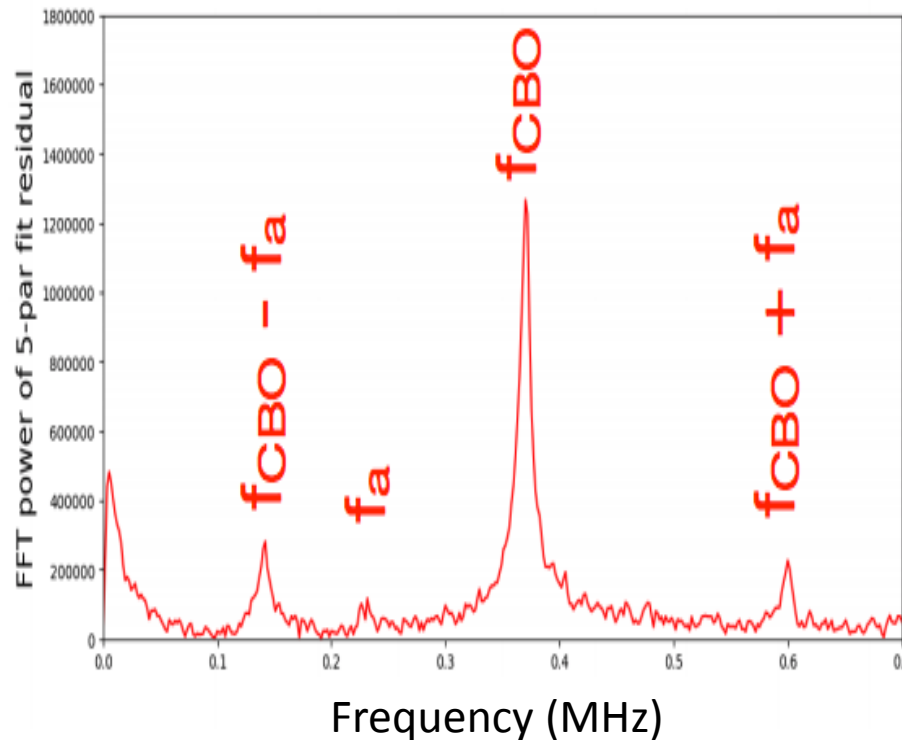
# Why do we care about CBO and other systematics?



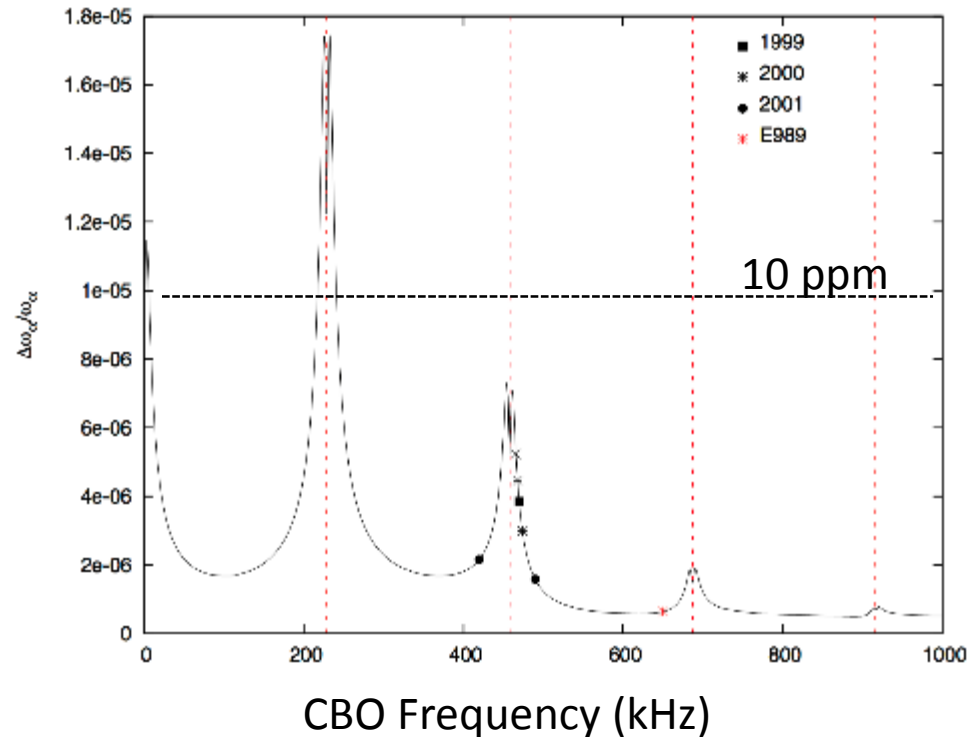
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- Fraction of decay  $e^+$  at detectors (acceptance) changes with CBO affecting  $A(t)$  term. (Instability in the calorimeter gain would as well.)
- This shows up the wiggle plot and pulls our result for  $\omega_a$ :

FFT of Residuals to 5-par fit



$\Delta\omega_a$  if CBO uncorrected



# Why are Early/Late effects important?

Anything leading to early/late variations in  $A(t)$  and  $\phi(t)$  have to be kept under control as they lead to a pull on  $\omega_a$

$$\begin{aligned}\cos(\omega_a t - \phi) &= \cos \left[ \omega_a t - \phi_0 - \frac{d\phi}{dt} t + \mathcal{O}\left(\frac{d^2\phi}{dt^2}\right) \right] \\ &= \cos \left[ \left( \omega_a - \frac{d\phi}{dt} \right) t - \phi_0 + \mathcal{O}\left(\frac{d^2\phi}{dt^2}\right) \right] \\ &= \cos \left[ \omega'_a t - \phi_0 + \mathcal{O}\left(\frac{d^2\phi}{dt^2}\right) \right]\end{aligned}$$

Things that might change  $f(t)$ :

- Gain change.
- Pileup contamination (mixture of e+ having different average phases)
- Muon Loss with different average phases
- CBO (radial and vertical)
- Rate dependent energy and time reconstruction



# Modulation of $N_0$ , $A$ , $\phi$ with $f_{cbo}$

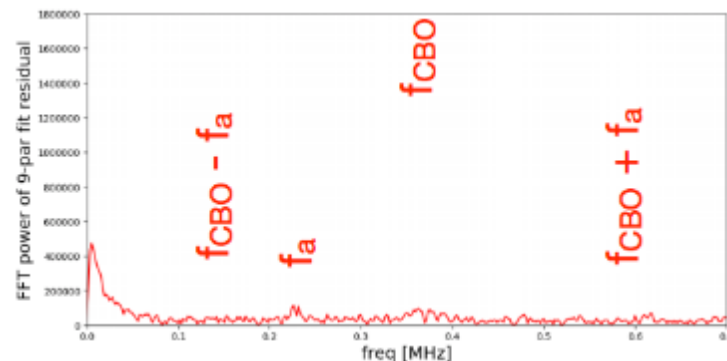
$$dN / dt = N_0(t) e^{-\frac{t}{\tau}} [1 + A(t) \cos(\omega_a t + \phi_a(t))]$$

$$N_0(t) = N_0 \left[ 1 + A_N e^{-\frac{t}{\tau_{cbo}}} \cos(2\pi f_{cbo} t + \phi_N) \right]$$

$$A(t) = A \left[ 1 + A_A e^{-\frac{t}{\tau_{cbo}}} \cos(2\pi f_{cbo} t + \phi_A) \right]$$

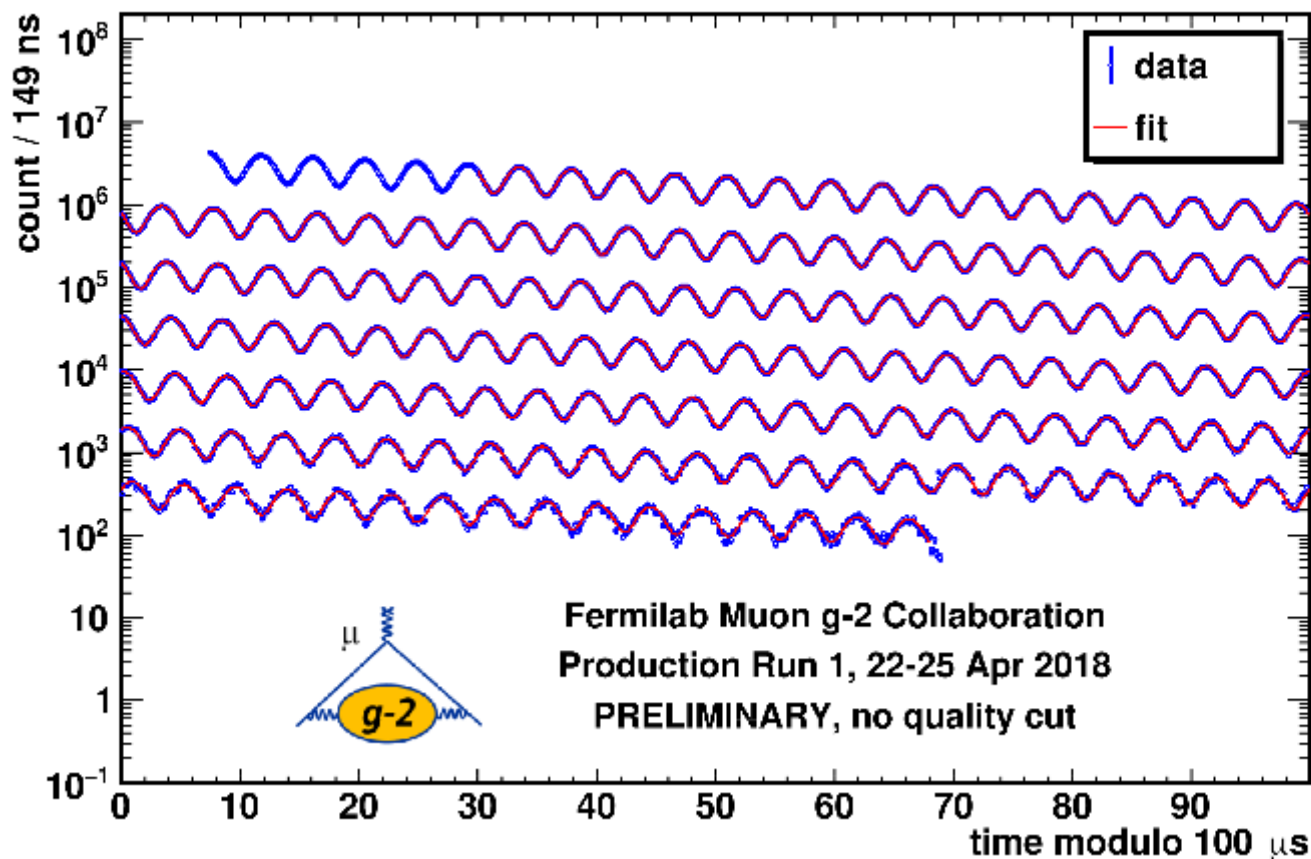
$$\phi_a(t) = \phi_a + A_\phi e^{-\frac{t}{\tau_{cbo}}} \cos(2\pi f_{cbo} t + \phi_\phi)$$

FFT of Fit Residuals  
including BCO in fit.



# The analysis is in full flow .....

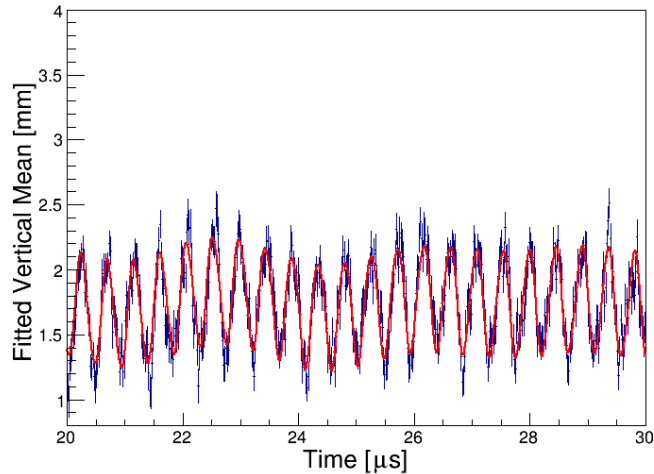
We are busy analysing  $\sim 9 \times 10^9$  recorded muon decays.



$\sim 60$  hours of data yielding  $\sim 0.95$  billion decay positrons

Final E989 goal is  $\sim 2 \times 10^{11}$  muon decays.

# Pitch Correction for vertical oscillations..



Also important to measure vertical beam oscillations in the straw trackers. They contribute another term to  $\omega_a$  if the dot product  $(\beta \cdot B)$  is not zero :

$$\omega_a = \frac{e}{m} \left\{ a_\mu B - a_\mu \left( \frac{\gamma}{\gamma+1} \right) (\beta \cdot B) \beta \right\}$$

We will add a small correction for this to the fitted  $\omega_a$

$$\frac{\Delta\omega}{\omega_a} = - \frac{\langle \psi^2 \rangle}{2} = - \frac{\langle \psi_0^2 \rangle}{4} = - \frac{n \langle y^2 \rangle}{2R_0^2}$$

There is a similar small correction for muons that are off the magic momentum and are subject to the electric field from the quadrupoles.

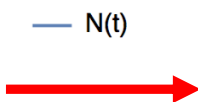
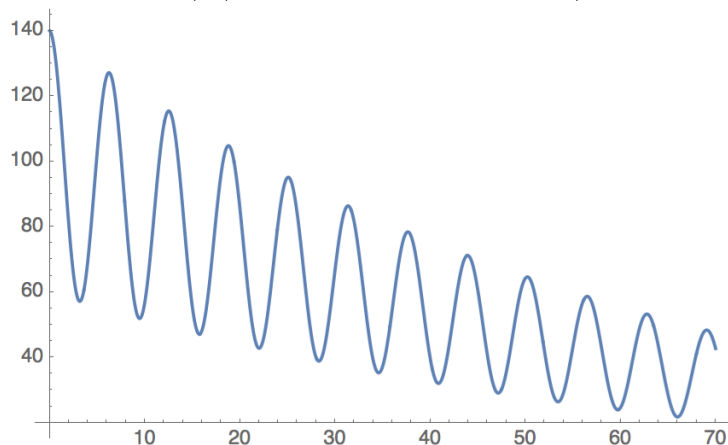
Important to measure the momentum distribution and mean radius of the muon orbits. Again the Trackers are vital for this. Aim to keep uncertainty arising from each of these effects to < 30 ppb.



# The Ratio Method for $\omega_a$

## How the ratio method works:

$$N_5(t) = N_0 e^{-t/\tau} (1 + A \cos(\omega_a t + \phi))$$



$$u_+(t) = N_5(t + T/2)/4$$

$$u_-(t) = N_5(t - T/2)/4$$

$$v_1(t) = v_2(t) = N_5(t)/4$$

Randomly split positron time spectra into 4 sets, two with time spectra shifted up and down by half a g-2 period, and two unchanged. (Equal weighting corresponding to  $\frac{1}{4}$  factors.)

$$N_5(t \pm T/2) = N_0 e^{-t/\tau} e^{\mp T/2\tau} (1 + A \cos(\omega_a t \pm \omega_a \frac{T}{2} + \phi)) \quad T \approx \frac{2\pi}{\omega_a}$$



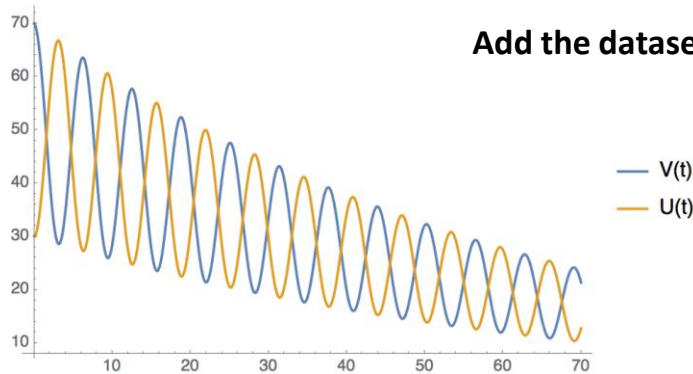
# The Ratio Method for $\omega_a$

Add the datasets separately:

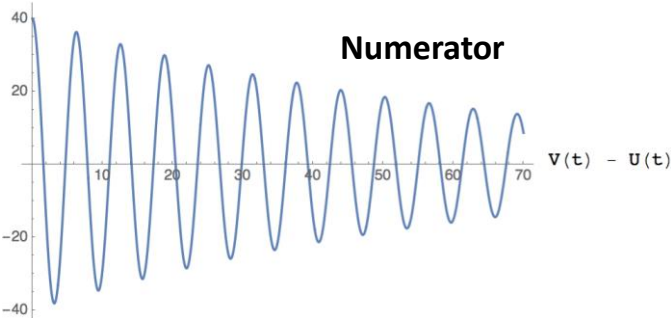
$$U(t) = u_+(t) + u_-(t)$$

$$V(t) = v_1(t) + v_2(t)$$

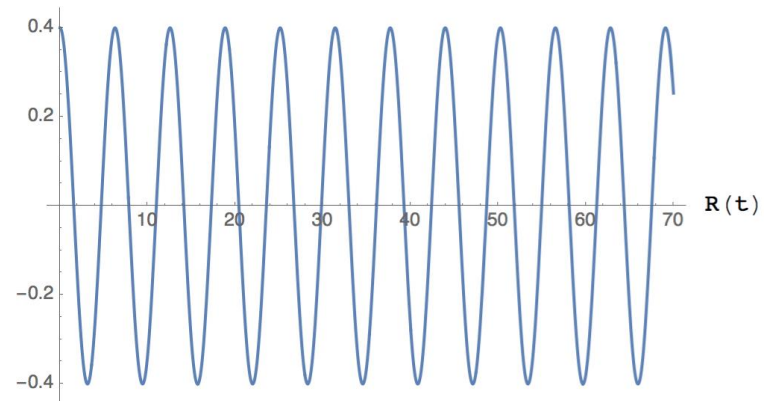
$$R(t) = \frac{V(t) - U(t)}{V(t) + U(t)}$$



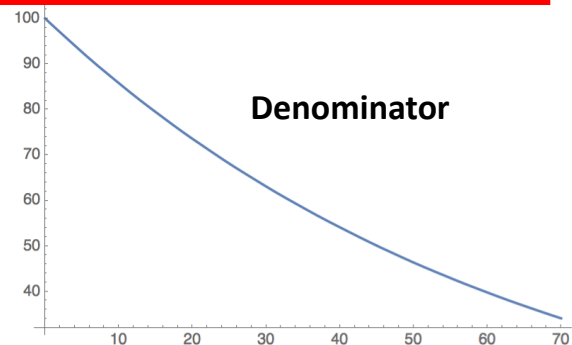
Numerator



=



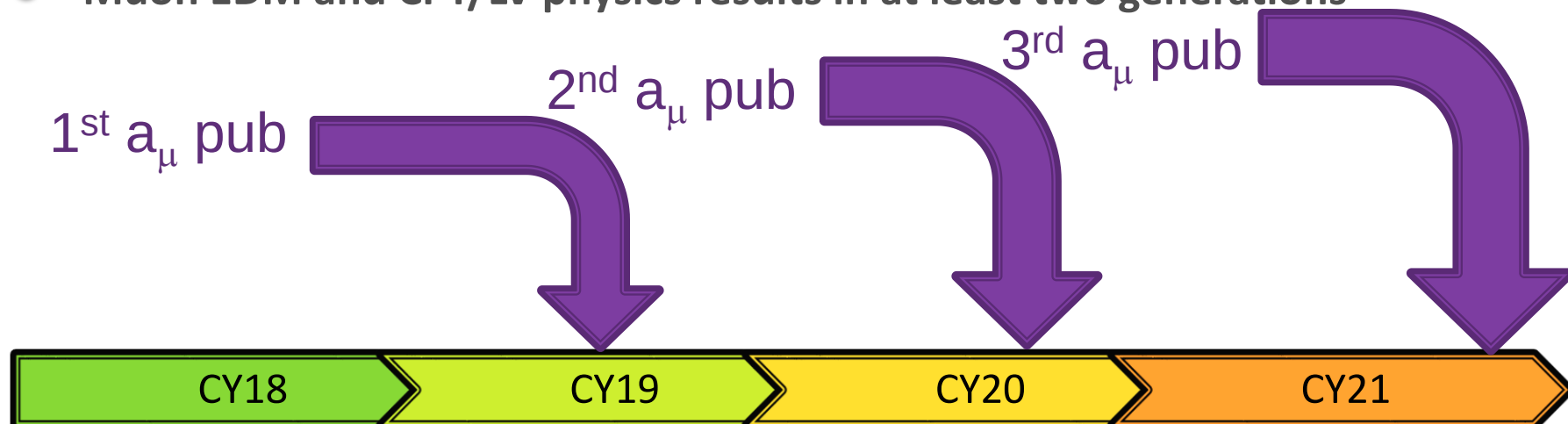
Denominator



$$R(t) = A \cos(\omega_a t + \phi) - \frac{1}{16} \left( \frac{T}{\gamma \tau} \right)^2 + (h.o.)$$

Exponential gets divided out – fit is now down to 3 parameters.  
Less sensitivity to slow effects which divide out.

- Planning on three generations of  $a_\mu$  publications
  - 1-2 x BNL ( $\sim 400$  ppb) collected in FY18 and aiming for publication by Summer 2019 conferences
  - 5-10 x BNL ( $\sim 200$  ppb) collected over FY18+FY19 with publication by end of 2020...caveat that we now enter unknown regime
  - 20+ x BNL ( $\sim 140$  ppb) collected by end of FY20 with final publication at end of 2021 or early 2022
- Muon EDM and CPT/LV physics results in at least two generations

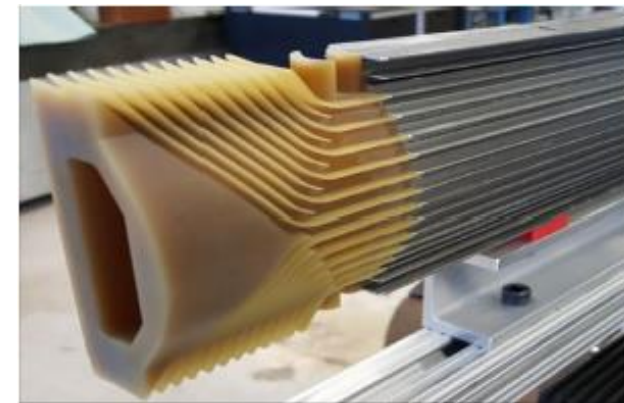




# Summer Upgrades



- Several improvements foreseen for this summer, each contributing to increase the stored muons by 10-30%
- **Accelerator upgrades**
  - faster switching between MuonCampus-BeamTest
  - New target
  - Add wedges for beam momentum compaction
- **Ring upgrades**
  - Kicker : key upgrade for improving quality of stored beam.
  - Quads : fix instabilities which cause Quads to run at HV lower than BNL (20kV vs 25kV)
  - Inflector : install new inflector.



# Conclusions.

Fermilab experiment finished 1<sup>st</sup> physics data run July 7<sup>th</sup>.

Fermilab 1<sup>st</sup> physics data set is  $\sim 2 \times$  BNL data set with a goal of publishing in 2019.

Fermilab experiment has the ultimate goal of measuring muon  $g-2$   $\sim 4$  times more precisely than the BNL experiment. Work is ongoing to drive down the systematics exploiting the improved detector.

Detector improvements taking place over the summer ready for next physics run.

Work continues on improving the precision of the SM muon  $g-2$  prediction.

